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Mathematics Teacher Guide Grade 5
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Authors: Piet Human, Alwyn Olivier, Heather Collins, Carol MacDonald, Ema Lampen, Amanda le Roux, Andrew Hofmeyr, Manare Setati, Peter Moodie, John Laurie, Chris Human, Paul van Koersveld, Annette Nell

Layout and typesetting: The authors and the Ukuqonda Institute
Illustrations and computer graphics: The authors; the Ukuqonda Institute; Lisa Steyn (p. 255)
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IT solution and support for file sharing: Menge Media
Cover design and illustration: Leonora van Staden and Piet Human


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**CAPS time allocation**
2 hours

**CAPS page references**
13 to 15 and 125 to 126

**Mathematical background**

Although a number symbol such as 357 is formed by writing the three digits 3, 5 and 7, the number represented by the symbol 357 is not “three five seven” or “3 and 5 and 7”, but 300 + 50 + 7. This is what is meant by “understanding place value”. It should be made clear from the outset and emphasised whenever possible. Language constructions such as “break down a number into its place value parts” and learning aids such as place value cards were invented and are prescribed to promote understanding of place value.

There is a difference between number symbols, which are composed of digits, and the numbers as ideas, which are composed of units, tens, hundreds, etc. Probably the most dangerous misconception that learners can form about whole numbers is that numbers are composed of digits, for example that the number 357 is made up of the digits 3, 5 and 7.

A distinction can be made between the “face value” of a digit in a number symbol, the “numerical value” or number (place value part) represented by the digit, and the place value of the position occupied by the digit. For example, in 357 the face value of the symbol “5” is 5. However, the symbol “5” represents the number 50, hence its numerical value is 50. The symbol “5” is in the tens position, a fact that is sometimes expressed by saying that the place value of the digit (actually the place value of the position it occupies) is tens (note the plural).

**Resources**

Two resources are absolutely critical for the work in this unit:

- Counting apparatus: wooden or plastic cubes and rods, or sticks and stick bundles
- Place value cards, all of the same colour, for units, tens, hundreds and thousands, and preferably for ten thousands too.

Each learner should have their own set of counters (cubes/rods or sticks/bundles) and their own set of place value cards.

In addition, you should have a set of large place value cards for demonstration purposes.

Master copies for place value cards are provided in the Addendum at the back of this Teacher Guide (see pages 394 to 411).
1.1 Counting

Critical knowledge and skills

There is a huge difference between

A. saying the number names in sequence: “one, two, three, four, five, six, seven, eight …”, and

B. establishing how many objects there are in a given collection.

However, the ability to say the number names in sequence is a prerequisite for establishing the number of objects in a collection.

It is critical that learners understand counting not only as counting objects one by one, but also as structured counting in groups of ten, hundred, thousand, and so on.

Counting structured collections such as those on pages 4 to 7 (and similar pages in the Grade 4 and 6 Learner Books) can promote understanding of the base-ten positional number system (place value).

Teaching guidelines

Observe how learners approach question 1. Learners who try to count one by one need support, such as that described on the next page. Suggest to learners that they should consider how many stripes there are in each of the columns, and how many columns there are.

Notes on questions

Questions 3 to 5 are specifically designed to promote structured counting.

Answers

1. 100
2. 3
3. (a) 30 (b) 300 (c) 100 (d) 3 000
4. 6 000
5. (a) 10 000 (b) 100 (c) 1 000
6. 9 000
Teaching guidelines

Learners may fail to notice the structure of the array: that it consists of columns of 10 stripes each, with 10 such columns in a row (i.e. 100 stripes in a row), and 10 such rows from top to bottom.

One way in which you can help learners is to ask them to find a group of 10 stripes that are close together anywhere on the page. Ask them to point at such a group with a finger. Then ask them to point out another group of 10 stripes. Then ask how many such groups there are on the page as a whole.

It may also help learners if you introduce the ideas of rows and columns. You could make a drawing such as the one below on the board to serve as a reference for this.

```
\|\|\|\|\|\|\|
\|\|\|\|\|\|\|
\|\|\|\|\|\|\|
```

Explain to learners that you have drawn three rows of 10 lines each. To help them to pay attention to what you have explained, ask them to make a drawing with four rows of six lines each in their exercise books. Monitor their work.

Use your drawing on the board to show learners what a column is. Ask them how many lines there are in each of the columns on the board (three). Ask them how many lines there are in each of the columns in the drawing they have made (four). You may also ask them how many columns of three lines each you have drawn on the board (ten).

Additional questions you may ask
1. How many stripes would there be on two pages like this?
2. How many stripes would there be on five pages like this?
3. How many stripes would there be on ten pages like this?
4. How many stripes would there be on $1\frac{3}{4}$ pages like this?
**Teaching guidelines**

In Array B the stripes are grouped in 30s with ten groups in one row.

Some learners may still feel safer to count in 10s, while others may try to count in 30s.

Learners with a well-developed number concept will be able to see almost immediately that there are 3 000 stripes on the page.

The stripes in Array C on the next page are arranged in 60s and again there are ten groups in a row. If learners reason about the situation, they should realise that Array C has exactly double the number of stripes as Array B.

**Additional questions you may ask**

1. How many stripes would there be on two pages like this?
2. How many stripes are there in six of the ten rows?
3. How many stripes are there in six of the ten columns?
4. How many stripes would there be on three pages like this?
5. How many stripes would there be on $\frac{13}{2}$ pages like this?
**Additional questions you may ask**

1. How many stripes are there in two of the ten rows?
2. How many stripes are there in three of the ten columns?
3. How many stripes would there be on two pages like this?
4. How many stripes would there be on $1\frac{3}{5}$ pages like this?
5. An array consists of 100 groups of 500 stripes each. How many groups of 250 stripes each will be the same number of stripes in total?
**Additional questions you may ask**
Learners can subtract mentally or count backwards in multiples to find the answers.

1. How many stripes will there be if three rows of stripes are removed from the array?
2. How many stripes will there be if four columns are removed?
3. How many stripes will there be if ten groups of 100 stripes are removed?
4. How many stripes will there be if four groups of 100 stripes are removed?
5. How many stripes will there be if five stripes are removed?

**Additional counting activities**
1. Count the stripes on this page by counting in 100s.
2. Count the stripes on this page by counting aloud in 200s.
3. Count backwards from 10 000 to 0 in 1 000s.
4. Count backwards from 1 000 to 0 in 500s.
Answers
7. (a) 4 264
   (b) 736

Additional questions you may ask
1. How many more stripes are needed to fill this page up to 8 000?
2. How many more stripes are needed to fill this page up to 10 000?
3. How many more stripes are needed to fill this page up to 7 500?
1.2 Place value

Teaching guidelines

Although pictures of place value cards are provided on many pages of the Learner Book, it is critical that each learner has their own set of place value cards like those given in the Addendum on pages 394 to 397. They also need place value apparatus such as wooden or plastic cubes and rods, or sticks and bundles of sticks. These concrete materials are indispensable supports for the development of number concept, and contribute to the understanding of place value.

Although a number symbol such as 357 is written (formed) by writing the three digits 3, 5 and 7, the number represented by the symbol 357 is not “three five seven”, but $300 + 50 + 7$. This should be made clear from the outset and emphasised whenever possible. **Numbers are ideas; number symbols and number names are marks on paper or words and sounds.** The reading of a number symbol by saying the digits should be discouraged: numbers should be read by saying the full number names. A simple but powerful classroom activity is to write a number symbol on the board and ask learners to read it aloud. Such oral work may be extended by asking questions such as: “How many tens are in 67?”, “How many hundreds are in 368?”

Place value cards are an indispensable tool to help learners to distinguish, in their own minds, between number symbols and the numbers themselves. It is important to use place value cards correctly. The basic place value card activity is to ask learners to “show” a number with cards. When learners are asked to show a number, for example 357, they should select and hold up the 300, 50 and 7 cards, not the 3, 5 and 7 cards.

**Answers**

1. (a) 7 948  (b) 6 853  (c) 1 045  
   (d) 3 975  (e) 4 008  
2. (a) 1 000, 200, 70, 3  
   (b) 6 000, 500, 20, 5  
   (c) 3 000, 300, 50, 7  
   (d) 2 000, 10, 5  
   (e) 5 000, 40, 2  
   (f) 1 000, 500, 80, 9
**Possible misconceptions**
A major purpose of using place value cards is to protect learners against forming the misconception that a number itself is composed of the single-digit numbers represented by the digits when used separately. The 5 in 57 is something else than the 5 in 35 or in 5. The 5 in 57 represents 50, not 5. You should consistently keep in mind that there is a difference between number symbols, which are composed of digits, and the numbers as ideas, which are composed of units, tens, hundreds, etc. This is what is meant by “understanding place value”.

**Teaching guidelines**
Place value cards can be used to demonstrate the relationship between expanded notation and number symbols. The number 627 can be represented in two ways with place value cards, namely

as \[ \begin{array}{c}
600 \\
20 \\
7
\end{array} \]

and as \[ \begin{array}{c}
627
\end{array} \]

These two ways of arranging the place value cards correspond to the expanded notation and the number symbol.

**Answers**

3. (a) \[ 1000 + 200 + 70 + 3 \] (b) \[ 6000 + 500 + 20 + 5 \]  
   (c) \[ 2000 + 10 + 5 \]

4. (a) 6  
   (b) 4

5. (a) 4  
   (b) 8

6. (a) \[ 3758 \]  
   (b) \[ 1376 \]  
   (c) \[ 8206 \]  
   (d) \[ 8026 \]  
   (e) \[ 6040 \]  
   (f) \[ 6004 \]
### 1.3 Counting, ordering and comparing numbers

**Teaching guidelines**

As a “warm-up” for the activities in this section, you may ask learners to softly count (individually) in 500s from 500 up to 5 000 and write the number symbols as they go along.

You may also ask some of the following similar questions:

1. Count softly in 400s by yourself, starting at 0 and going up to 4 000. Write the number symbols as you go along.
2. Count softly in 400s by yourself, starting at 100 and going up to 4 100. Write the number symbols as you go along.
3. Count softly in 400s by yourself, starting at 200 and going up to 4 200. Write the number symbols as you go along.
4. Count softly in 400s by yourself, starting at 300 and going up to 4 300. Write the number symbols as you go along.

**Answers**

1. (a) 4 800  (b) 3 090  (c) 4 088  (d) 4 008  (e) 3 200  (f) 3 150

   Arranged from smallest to biggest: 3 090  3 150  3 200  4 008  4 088  4 800

2.  

<table>
<thead>
<tr>
<th>5 900</th>
<th>6 100</th>
<th>6 200</th>
<th>6 400</th>
<th>6 600</th>
<th>6 800</th>
</tr>
</thead>
</table>

3.  

<table>
<thead>
<tr>
<th>6 310</th>
<th>6 320</th>
<th>6 330</th>
<th>6 350</th>
<th>6 370</th>
<th>6 380</th>
<th>6 390</th>
</tr>
</thead>
</table>

4. (a) 3 250  3 255  3 260  3 265  3 270  3 275  3 280  3 285  3 290
    3 295  3 300
(b) 3 250  3 275  3 300  3 325  3 350  3 375  3 400  3 425  3 450
(c) 3 250  3 300  3 350  3 400  3 450
(d) 2 158  2 163  2 168  2 173  2 178  2 183  2 188
(e) 2 133  2 183  2 233  2 283  2 333
(f) 2 127  2 152  2 177  2 202  2 227  2 252  2 277  2 302  2 327
Answers

5. (a) 3 250 3 240 3 230 3 220 3 210 3 200 3 190 3 180 3 170 3 160 3 150
(b) 3 254 3 244 3 234 3 224 3 214 3 204 3 194 3 184 3 174 3 164 3 154 3 144
(c) 3 250 3 245 3 240 3 235 3 230 3 225 3 220 3 215 3 210 3 205 3 200
(d) 3 227 3 222 3 217 3 212 3 207 3 202 3 197 3 192 3 187 3 182 3 177
(e) 3 250 3 225 3 200 3 175 3 150 3 125 3 100
(f) 3 250 3 200 3 150 3 100 3 050 3 000

6. (a) 2 600 (b) 3 200 (c) 3 800 (d) 4 400 (e) 5 000 (f) 5 600 (g) 6 200 (h) 6 800
(i) 7 400 (j) 8 000

7. (a) 3 492 < 9 002 (b) 6 768 < 6 879 (c) 2 901 > 2 899 (d) 5 536 < 6 355

5. Write the numbers down as you go along in each counting task.
(a) Count backwards in tens from 3 250 down to 3 150.
(b) Count backwards in tens from 3 254 until you pass 3 150.
(c) Count backwards in fives from 3 250 down to 3 200.
(d) Count backwards in fives from 3 227 until you pass 3 180.
(e) Count backwards in twenty-fives from 3 250 down to 3 100.
(f) Count backwards in fifties from 3 250 down to 3 000.

6. Write down the numbers that should be in the blocks in the diagram. For example, the answer for (a) is 2 600.

7. In each case decide which is the bigger of the two numbers. Use the < or > sign to write your answers.
(a) 3 492 and 9 002 (b) 6 768 and 6 879
(c) 2 901 and 2 899 (d) 5 536 and 6 355
Grade 5 Term 1 Unit 2     Number sentences

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<td></td>
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**CAPS time allocation**  
3 hours

**CAPS page references**  
20 and 127 to 131

While providing opportunities to develop understanding of number sentences, the following questions also address the content specified in the Mental Mathematics section of the CAPS:

- question 5 in Section 2.1
- questions 9 to 12 in Section 2.2
- question 4 in Section 2.3.

Questions 11 and 12 of Section 2.2 may be regarded as enrichment. Learners who complete questions 1 to 10 faster than others can also engage with questions 11 and 12.

**Mathematical background**

A number sentence is a statement about **numbers**, for example $3 \times 12 + 5 \times 12 = 8 \times 12$.

A number sentence is a **sentence**; the verb is $=$, “equals”, “is equal to” or “is equivalent to”.

$3 \times 12 + 5 \times 12$ is an expression. It can be called a **calculation plan**, a description of the intention to perform certain calculations.

A number sentence with expressions on both sides of the equal sign, for example $3 \times 12 + 5 \times 12 = 8 \times 12$, is a **statement of equivalence**.

It states that the two different calculation plans will produce the same number, which in this case is 96.
2.1 State addition and subtraction facts

Mathematical notes

This section is about the concept of equivalence, and the conventions that are to be followed when writing and interpreting the calculation plans that form the building blocks of a symbolic statement of equivalence.

The fact that two different sets of calculations (calculation plans) with the same numbers produce the same answer can be expressed in the form of a number sentence. For example, the fact that \(3 \times 40 + 3 \times 8\) and \(3 \times (40 + 8)\) give the same answer can be expressed with the number sentence

\[3 \times (40 + 8) = 3 \times 40 + 3 \times 8\]

Such a number sentence is called a statement of equivalence.

Number sentences can be true or false, for example

\[5 \times (3 + 4) = 5 \times 3 + 4\] is false, but \[5 \times (3 + 4) = 5 \times 3 + 5 \times 4\] is true.

Teaching guidelines

You may use the tinted passage on page 13 of the Learner Book as a guideline for a presentation to explain what a statement of equivalence is.

Questions 1 and 2 are questions for learning, and are hence critical.

Question 1 provides learners with an opportunity to write statements of equivalence. Question 2 alerts learners to the difference between true and false statements.

Answers

1. (a) \[5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10 + 10\]
   (b) \[25 \times 8 = 4 \times 50\]
   (c) \[970 - 930 = 470 - 430\]

2. (a) False     (b) True     (c) True
   (d) True      (e) True      (f) False

When numbers are multiplied, any of the numbers can be taken first. The answer is the same.
Teaching guidelines

To be able to write and interpret statements of equivalence, learners need to know certain **basic conventions about order of operations** that are used in calculation plans. Without adhering to these conventions, different people may interpret the same calculation in different ways and confusion will result. This danger of confusion is demonstrated in the tinted passage.

You may do a presentation similar to the one in the tinted passage, or you could direct learners to read the tinted passage in their books, for example by asking: “Why do Richard and Thandi look so confused?” If learners have difficulties in reading the text, you may explain on the board why the two characters are so confused.

You may announce that while doing questions 3 to 7, they will learn about the agreements people have made to prevent such confusion. These five questions are interrelated and form a critical learning sequence. Ensure that learners read and understand the statements describing the different conventions, and illustrate these with more examples on the board.
Possible misconceptions

Poor understanding of the meaning of brackets can cause confusion and misconceptions. Brackets are used in calculation plans to indicate that if you follow the given calculation plan, you should do the calculations inside the brackets first.

For example, if you execute the calculation plan $45 \times (10 + 5 + 2)$, you first calculate $10 + 5 + 2$, get the answer 17, and then multiply this by 45.

But if you have to find out how much $45 \times (10 + 5 + 2)$ is, you are free to replace it with the equivalent calculation plan $45 \times 10 + 45 \times 5 + 45 \times 2$, which gives $450 + 225 + 90 = 765$. Of course $45 \times 17$ gives the same answer.

Answers

3. (a) 12 (b) 13 (c) 39 (d) 27

4. False:
   (a) $100 - 50 + 30 \neq 100 - 80$
   (b) $3 \times 10 + 5 \times 2 \neq 70$
   (d) $3 \times 3 + 5 \times 3 \neq 8 \times 6$

5. False:
   (a) $12 - (3 + 5) - 2 \neq 12 - 3 + 5 - 2$
   (b) $3 \times 30 + 5 \times 30 \neq 3 \times (30 + 5) \times 30$
   (d) $5 \times (20 + 3) \neq 5 \times 20 + 3$

Examples:

In $3 \times (4 + 6)$ the brackets are used to tell you that you must calculate like this:

$4 + 6 = 10$ followed by $3 \times 10 = 30$

The instructions $3 \times 4 + 6$ as well as $6 + 3 \times 4$ tell you that you should calculate like this:

$3 \times 4 = 12$ followed by $12 + 6 = 18$

$12 - (3 + 5) - 2$ means you have to do this:

$3 + 5 = 8 \quad 12 - 8 = 4 \quad 4 - 2 = 2$

5. Which of these number sentences are false?
   (a) $12 - (3 + 5) - 2 = 12 - 3 + 5 - 2$
   (b) $3 \times 30 + 5 \times 30 = 3 \times (30 + 5) \times 30$
   (c) $3 \times 30 + 5 \times 30 = (3 \times 30) + (5 \times 30)$
   (d) $5 \times (20 + 3) = 5 \times 20 + 3$
   (e) $5 \times (20 + 3) = 5 \times 20 + 5 \times 3$
   (f) $5 \times (20 + 3) = 5 \times 18 + 5 \times 5$
   (g) $5 \times (20 - 3) = 5 \times 20 - 5 \times 3$
   (h) $(20 + 3) \times 5 = 20 \times 5 + 3 \times 5$
Teaching guidelines
The associative property of addition forms the logical foundation for the statements of equivalence used in addition and subtraction, and you may alert learners to this at this stage. (Unit 3, which follows the current unit, is about addition and subtraction.)

Answers
6. None are false.
7. False:
   (c) $500 + 300 - 200 \neq 500 + 200 - 300$
   (f) $(60 - 7) + (10 - 3) \neq (60 - 10) + (7 - 3)$
8. The first, third and last actions produce the same result:
   $6 \times 1000 = 60 \times 100$
   $60 \times 100 = 600 \times 10$
   $600 \times 10 = 6 \times 1000$
9. The following actions will produce the correct answer, which is 2000:
   (a) $20 \times 100$
   (b) $20 \times 60 + 20 \times 3 + 20 \times 30 + 20 \times 7$
   (d) $20 \times 60 + 20 \times 40$
   Action (c) $20 \times 80 \times 3 + 20 \times 50 \times 7$ will not.
2.2 Solve and complete number sentences

**Mathematical notes**

Number sentences can be **open** or **closed**. The number sentence \(3 \times (7 + 4) = 3 \times 7 + 3 \times 4\) is a closed number sentence; all the numbers are given.

\(73 + \ldots = 100\) or \(73 + \square = 100\) is an open number sentence; it is incomplete. It contains an **unknown**. In algebra this is normally called an **equation**.

It is actually a question: \(73 + ? = 100\). (Also see the “Mathematical notes” about symbols for unknowns on the next page of this Teacher Guide.)

A number sentence can also have only a number on one side of the equal sign, for example \(3 \times 12 + 5 \times 12 = 96\) or \(8 \times 12 = 96\). Number sentences like these are used to state **number facts**, for example \(4 + 5 = 9\), and the **answers** for calculations that were done, for example \(256 + 322 = 578\).

**Teaching guidelines**

This section starts by introducing the idea of open number sentences, and completing them by finding the missing number. Learners may engage with questions 1 and 2 straightaway, without any introduction from you.

Question 3 is about the use of number sentences to describe addition facts, and it provides opportunities for practice.

**Answers**

1. 19
2. (a) 20 (b) 19 (c) 18 (d) 15 (e) 30 (f) 40 (g) 20 (h) 20 (i) 60 (j) 50 (k) 70 (l) 80 (m) 75 (n) 25 (o) 35 (p) 12
3. There are numerous possibilities and only a few examples are given below. All learners’ answers should be considered.
   (a) 80 + 20 = 100  
   (b) 75 + 25 = 100  
   (c) 91 + 9 = 100
   (b) 65 + 35 = 100  
   (d) 78 + 22 = 100  
   (e) 40 + 60 = 100
   (c) 56 + 44 = 100  
   (d) 85 + 15 = 100  
   (e) 71 + 29 = 100
   (d) 100 + 200 = 300  
   (e) 150 + 150 = 300  
   (f) 250 + 50 = 300
   (e) 500 + 200 = 700  
   (f) 450 + 250 = 700  
   (g) 145 + 555 = 700
Teaching guidelines
Apart from relating number sentences to the number line, questions 5 to 7 are about using number sentences to articulate the idea of addition and subtraction as inverse operations. It may be necessary to do question 6 as a demonstration on the board.

Questions 4 to 8 are questions for learning and hence critical.

Answers
4. The number behind the blue stickers is 85, because $85 + 3 = 88$.
   So, when adding 5 to the number behind the blue stickers the answer will be 90.
5. (a) Yes  (b) Yes
6. (a) $120 - 62 = 58$  (b) $120 - 58 = 62$
7. (a) 78  (b) 35
8. $35 + 85 = 120$
   $120 - 85 = 35$
   $120 - 35 = 85$

Mathematical notes
In algebra a letter symbol, for example $x$, is normally used to represent an unknown constant, for example $73 + x = 100$.

Symbols used to represent unknown constants (or variables), such as ... or ? or $\square$ or $x$, are called placeholders.

Instead of a symbol, the phrase a number or the number can also be used. The open number sentence $73 + \square = 100$ can thus also be written as $73 + a\text{ number} = 100$. 
Notes on questions

Questions 9 to 12 are intended as practice of addition and subtraction bonds (Mental Mathematics).

Answers

9. There are numerous possibilities, for example:
   \[ 80 + 10 = 90 \quad 90 - 10 = 80 \quad 90 - 80 = 10 \]
   \[ 65 + 25 = 90 \quad 90 - 25 = 65 \quad 90 - 65 = 25 \]
   \[ 81 + 9 = 90 \quad 90 - 9 = 81 \quad 90 - 81 = 9 \]
   \[ 35 + 55 = 90 \quad 90 - 55 = 35 \quad 90 - 35 = 55 \]

10. There are numerous possibilities, for example:
    \[ 580 + 420 = 1000 \quad 1000 - 420 = 580 \quad 1000 - 580 = 420 \]
    \[ 475 + 525 = 1000 \quad 1000 - 525 = 475 \quad 1000 - 475 = 525 \]
    \[ 891 + 19 = 1000 \quad 1000 - 19 = 891 \quad 1000 - 891 = 19 \]
    \[ 450 + 550 = 1000 \quad 1000 - 550 = 450 \quad 1000 - 450 = 550 \]

11. There are numerous possibilities, for example:
   (a) \[ 250 + 150 + 200 = 600 \quad 175 + 125 + 300 = 600 \]
       \[ 450 + 125 + 25 = 600 \quad 130 + 370 + 100 = 600 \]
   (b) \[ 400 + 250 + 150 = 800 \quad 555 + 125 + 120 = 800 \]
       \[ 300 + 450 + 50 = 800 \quad 345 + 105 + 350 = 800 \]
   (c) \[ 750 + 150 + 100 = 1000 \quad 480 + 220 + 300 = 1000 \]
       \[ 505 + 245 + 25 = 1000 \quad 870 + 115 + 15 = 1000 \]

12. There are numerous possibilities, for example:
   (a) \[ 35 + 65 - 50 = 50 \quad 28 + 33 - 11 = 50 \]
       \[ 250 + 45 - 245 = 50 \quad 2 + 53 - 5 = 50 \]
   (b) \[ 400 + 467 - 667 = 200 \quad 55 + 315 - 170 = 200 \]
       \[ 900 + 11 - 711 = 200 \quad 45 + 165 - 10 = 200 \]
   (c) \[ 350 + 300 - 250 = 400 \quad 390 + 230 - 220 = 400 \]
       \[ 457 + 13 - 70 = 400 \quad 985 + 15 - 600 = 400 \]
2.3 Equivalence

Teaching guidelines

The purpose of this section is to develop the use of number sentences to make general statements of equivalence, specifically of the distributive property of multiplication. Note that learners need not know the names of the properties of multiplication (e.g. distributive property) in Grade 5.

The coloured stickers provide a way of making statements equivalent to \( x \times (y + z) = x \times y + x \times z \) without using algebraic letter symbols.

Questions 1 and 2 may form the substance of an interactive whole-class discussion, whereafter learners do questions 3 and 4 individually. Questions 1 to 3 are critical questions for learning.

Answers

1. (a) Learners choose their own numbers, therefore their answers will vary.
   (b) Yes
2. (a) No  (b) Yes
3. (a) Yes  (b) Yes  (c) Yes  (d) No
4. (a) False  (b) True  (c) True  (d) True  (e) True

2.3 Equivalence

Choose a number to hide behind the blue stickers in question 1. It must be the same number for each of the blue stickers. Write your blue number down.

Also choose one number to put behind the yellow stickers. It must be the same number for each of the yellow stickers. Write your yellow number down.

1. (a) How much is your \( \square + \square \)?
   (b) Is it true that \( 10 \times (\square + \square) = 10 \times \square + 10 \times \square \)?

2. (a) Do you think the other learners in the class chose the same numbers as you to hide behind the blue and yellow stickers in question 1?
   (b) Do you think the other learners in the class also found that the number sentence in question 1(b) is true, although they may have chosen different numbers than you did?

3. Choose two other numbers for your blue and yellow stickers.
   (a) Is it again true that \( 10 \times (\square + \square) = 10 \times \square + 10 \times \square \)?
   (b) Is \( 5 \times (\square + \square) = 5 \times \square + 5 \times \square \)?
   (c) Choose a number to hide behind the red stickers below.

\[ \square \times (\square + \square) = \square \times \square + \square \times \square \]

Is this number sentence true?
   (d) Is the number sentence below true?

\[ \square \times (\square + \square) = \square \times \square + \square \times \square \]

4. In each case state whether you think the sentence is true or false.
   (a) \( 5 \times (400 + 30 + 7) = 5 \times 400 + 30 + 7 \)
   (b) \( 5 \times (400 + 30 + 7) = 5 \times 400 + 5 \times 30 + 5 \times 7 \)
   (c) \( 5 \times (400 - 30 - 7) = 5 \times 400 - 5 \times 30 - 5 \times 7 \)
   (d) \( 5 \times (400 + 60 + 8) = 10 \times (200 + 30 + 4) \)
   (e) \( 5 \times (400 + 60 + 8) = 20 \times (100 + 15 + 2) \)
Grade 5 Term 1 Unit 3  
Whole numbers: Addition and subtraction

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**CAPS time allocation**  
5 hours

**CAPS page references**  
13 to 15 and 132 to 135

**Mathematical background**

Calculations with multi-digit numbers are done by breaking the task down into separate smaller tasks. For example, the single task $254 + 538$ can be broken down into smaller tasks, as follows:

- **Single task:** $254 + 538 = (200 + 50 + 4) + (500 + 30 + 8)$
- **Three separate tasks:** $= (200 + 500) + (50 + 30) + (4 + 8)$

(The numbers are broken down into their place value parts.)

(The rearrangement can be done because addition is commutative and associative.)

Learners can only use “break down, rearrange and build up” methods effectively if they know the addition and subtraction bonds for units, and for multiples of 10 and 100 well, or can quickly reconstruct these facts. The core strategy of replacing a given computational task by a combination of separate tasks can only work if the separate tasks are simpler, and in fact easy to do for learners. This can only be the case if learners are not challenged by tasks such as $200 + 500, 50 + 30$ and $4 + 8$: the answers to such calculations should be readily available in learners’ minds, or learners should be able to find the answers quickly and easily. Unfortunately the majority of learners have inadequate knowledge of addition and subtraction bonds, and can only reconstruct addition and subtraction facts by drawing stripes and counting. In fact, it seems that many learners do not even try to remember addition facts like $5 + 7 = 12$, and adopt the habit to simply draw stripes and count. To overcome this habit, learners need to learn basic number facts and acquire skills to reconstruct basic number facts. Sections 3.1 to 3.4 provide for this.

**Resources**

A set of place value cards for each learner and five sets of large place value cards for teaching purposes (see Addendum, pages 394 to 411)
3.1 Addition and subtraction facts

**Teaching guidelines**

Questions 1, 8, 9 and 10 provide learners with opportunities to relate addition and subtraction to real-life situations. If learners find these questions challenging, suggest that they quickly make rough copies of the drawings so that they can fill in distances on the drawing to support their thinking. If learners make drawings, ensure that they do not waste time on trying to make the drawings accurate and realistic – the drawings should be done quickly since they only serve the purpose of supporting learners’ thinking about the situation.

Even learners who know that 70 + 30 = 100 may be challenged by question 1(a) if they fail to visualise the situation clearly in their minds. You may support learners by making a copy of the drawing on the board and stating the given information and questions verbally, and by annotating the drawing.

If learners are challenged by question 1(b), it may help to point out that they need to use the answer to question 1(a).

Questions 2 and 3 provide for practice in Mental Mathematics.

**Answers**

1. (a) 70 m  
   (b) 270 m  
   (c) 300 m

2. (a) 40 + 60 = 100  
   (b) 80 + 20 = 100  
   (c) 50 + 50 = 100  
   (d) 10 + 90 = 100  
   (e) 100 − 50 = 50  
   (f) 100 − 80 = 20  
   (g) 100 − 60 = 40  
   (h) 100 − 70 = 30  
   (i) 100 − 90 = 10  
   (j) 30 + 70 = 100  
   (k) 100 − 30 = 70  
   (l) 100 − 40 = 60  
   (m) 400 − 30 = 370  
   (n) 700 − 40 = 660

3. (a) 60  
   (b) 60  
   (c) 40  
   (d) 60  
   (e) 440  
   (f) 60
**Notes on questions**

The number lines are given as suggestions that learners may think about positions, distances and movements on the number lines when they do calculations. However, learners should not feel compelled to think in terms of number lines: *If learners can do the calculations and solve the number sentences easily without thinking of number lines, they should do so.*

**Answers**

4. (a) 1 000  (b) 1 000  (c) 1 000  (d) 1 000  
5. (a) 700   (b) 700   (c) 300   (d) 300  
   (e) 300   (f) 300   (g) 3 700  (h) 3 700  
6. (a) 300   (b) 300   (c) 5 700  (d) 5 700  
7. (a) 10 000 (b) 2 000  (c) 10 000 (d) 8 000  
   (e) 10 000 (f) 7 000  (g) 10 000 (h) 4 000  
   (i) 10 000 (j) 5 000  (k) 7 000  (l) 3 000  
   (m) 8 000  (n) 3 000  

**Mathematical notes**

To support thinking about the number sentence $300 + □ = 1 000$, one may think of 300 and 1 000 as positions on the number line, and ask oneself how far one has to move from 300 to get to 1 000.
Teaching guidelines
Suggest to learners that if they have any difficulties with question 8, they could quickly make a rough drawing to help themselves to understand the situation. They should show the given distances on their drawings.
Some learners may indicate distances with arrows:

![Drawing](image1)

Other learners may mark the distances at specific points:

![Drawing](image2)

Note that drawings like these provide learners with an introduction to the number line.

Answers
8. (a) Approximately 120 m
   (b) Approximately 180 m
   (c) 300 m
   (d) 200 m
9. (a) 1 800 m
   (b) 2 600 m
   (c) 2 200 m
10. (a) 3 500 units
    (b) 4 600 units
     (c) 8 100 units
3.2 Addition, subtraction and doubling

Teaching guidelines
To help learners to read and make sense of the tinted passage, you may illustrate the ideas of **sum** and **difference** with drawings on the board, for example:

**Sum:**

```
3 200 + 4 600
```

**Difference:**

```
3 200 - 3 200 = 4 600 - 4 600
```

Note that in questions 1(a) and (b) learners have to calculate a sum and a difference respectively. Their responses to these questions can be used to assess the effectiveness of the introductory discussion.

Mathematical notes
Question 1 involves different meanings of subtraction.

In 1(b) subtraction is used to establish the **difference** between two amounts.

```
3 200 - 4 600 = 4 600 - 3 200
```

In 1(c) subtraction is used to establish a **shortfall**.

```
3 400 + 600 = 6 800 - 3 400
```

In 1(d) subtraction is used to establish how much is **left over** after some money was taken away from a given amount.

While learners usually know that they have to subtract in a situation like 1(d), they often do not realise that subtraction can be used in situations like 1(b) and 1(c). It is quite acceptable if learners do 1(c) like this:

```
3 400 + 600 = 4 000 + 2 800 = 6 800, so he needs another R600 + R2 800 = R3 400.
```

Notes on questions
Questions 1 and 2 are intended to make learners aware of how important it is that they have good knowledge of basic addition and subtraction facts for units and multiples of 10, 100 and 1 000. Discuss this in class to motivate learners for the work that follows.

**Answers**

1. (a) R9 100  (b) R2 300  (c) R3 400  (d) R2 300
2. 1 128 chickens
Notes on questions

Learners are generally used to only doing calculations with, or stating facts about, numbers that are given to them. In question 3 they are required to state facts without any numbers given to them. Learners may need some encouragement and prompting to get started on this.

It is critical that learners acquire the habit of trying to be smart and to avoid doing unnecessary work. Question 4 provides an opportunity for this. Some learners may be inclined to answer the three questions by doing the full calculations. For example, they may do the following for question 4(a):

\[
(400 + 30 + 2) + (100 + 60 + 8) = (400 + 100) + (30 + 60) + (2 + 8) \\
= 500 + 90 + 10 \\
= 600
\]

If learners do this, demonstrate on the board that if you know that \(432 + 165 = 597\), the answer for \(432 + 168\) can quickly and easily be found by adding 3 to 597, because 168 is 3 more than 165. Use this as an opportunity to encourage learners to try to be smart when they do calculations, and challenge them to be smart when they do questions 4(b) and (c).

Also impress on learners that they need to be able to do calculations with small numbers quickly in order to make good progress in Mathematics. The questions that follow will give them opportunities to strengthen their knowledge and skills for adding and subtracting multiples of 10, 100 and 1 000.

Answers

3. Learners write down ten different addition facts as well as two subtraction facts together with each addition fact, for example:

\[
\begin{align*}
3 + 5 &= 8 & 8 - 3 &= 5 & 8 - 5 &= 3 \\
40 + 20 &= 60 & 60 - 20 &= 40 & 60 - 40 &= 20
\end{align*}
\]

4. (a) 600 
(b) 566 
(c) 710

5. (a) 50 tins 
(b) 500 sausages
**Teaching guidelines**

Point out to learners that each row of the picture represents several number facts.

The above picture shows that 2 boxes + 2 boxes = 4 boxes, i.e. that $2 + 2 = 4$.

It also shows that 20 tins + 20 tins = 40 tins, i.e. that $20 + 20 = 40$.

If each tin contains 10 sausages, the picture also shows that 200 sausages + 200 sausages = 400 sausages.

**Answers**

6. (a) 20 tins  (b) 40 tins  (c) 60 tins  (d) 80 tins

7. 3 + 3 = 6  30 + 30 = 60  300 + 300 = 600

   4 + 4 = 8  40 + 40 = 80  400 + 400 = 800

   5 + 5 = 10  50 + 50 = 100  500 + 500 = 1000

   6 + 6 = 12  60 + 60 = 120  600 + 600 = 1200

   7 + 7 = 14  70 + 70 = 140  700 + 700 = 1400

   8 + 8 = 16  80 + 80 = 160  800 + 800 = 1600

   9 + 9 = 18  90 + 90 = 180  900 + 900 = 1800

   10 + 10 = 20  100 + 100 = 200  1000 + 1000 = 2000

   11 + 11 = 22  110 + 110 = 220  1100 + 1100 = 2200

8. (a) 350  (b) 400  (c) 500

   (d) 250  (e) 125  (f) 150

9. (a) 200 sausages  (b) 400 sausages  (c) 600 sausages  (d) 800 sausages

6. (a) How many tins are in the yellow boxes shown above?
   (b) How many tins are in the red boxes?
   (c) How many tins are in the blue boxes?
   (d) How many tins are in the brown boxes?

**Doubling** is an easy way to make addition facts.

For example, it is easy to double 30:

\[ 30 + 30 = 60 \]

We can say: **60 is the double of 30.**

7. Write number sentences to state the doubles of the numbers below.

   Example: 3 + 3 = 6; 30 + 30 = 60; 300 + 300 = 600

<table>
<thead>
<tr>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
<td>40</td>
<td>50</td>
<td>60</td>
<td>70</td>
<td>80</td>
<td>90</td>
<td>100</td>
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<td>300</td>
<td>400</td>
<td>500</td>
<td>600</td>
<td>700</td>
<td>800</td>
<td>900</td>
<td>1000</td>
<td>1100</td>
</tr>
</tbody>
</table>

8. 300 is half of 600. How much is half of each number below?

   (a) 700  (b) 800  (c) 1000

   (d) 500  (e) 250  (f) 300

9. (a) How many sausages are in the yellow boxes above?
   (b) How many sausages are in the red boxes?
   (c) How many sausages are in the blue boxes?
   (d) How many sausages are in the brown boxes?
**Answers**

10. (a) 200 tins  
   (b) 2,000 sausages

11. $10 + 12 + 14 + 16 + 20 = 72$ boxes → 720 tins → 7,200 sausages

12. (a) 70  
    (b) 60  
    (c) 80  
    (d) 90  
    (e) 40  
    (f) 50  
    (g) 80  
    (h) 70  
    (i) 60  
    (j) 90

**Possibilities for extension**

Doubles can be used as starting points for making other number facts, as suggested by the pictures below.

4 + 4 = 8 (boxes)  
40 + 40 = 80 (tins)  
400 + 400 = 800 (sausages)

3 + 4 = 7  
30 + 40 = 70  
300 + 400 = 700

3 + 5 = 8  
30 + 50 = 80  
300 + 500 = 800

Suppose each sausage contains 10 g protein.  
How much protein is in a tin of 10 sausages?  
How much protein is in a box of 10 tins?
3.3 Doubling and other ways to make facts

Critical knowledge and skills
It is critical that learners acquire skills to reconstitute basic addition and subtraction facts that they may have forgotten, and not rely on drawing stripes and counting.

Doubling numbers and extending from doubles is a powerful way of forming addition facts. For example, if you know that $60 + 60 = 120$, it is easy to form other facts by performing easy additions or subtractions on both sides of the equal sign:

- $60 + 60 + 10 = 120 + 10$, hence $60 + 70 = 130$
- $60 + 60 - 10 = 120 - 10$, hence $60 + 50 = 110$

Answers
1. (a) 11 (b) 17 (c) 18 (d) 21 (e) 18 (f) 15
2. 600 1200 800
   1000 1600 400
   1400 1800 2000
   50 150 70
3. (Learners may phrase their explanations in different ways.)
   $60 + 60 = 120$, and 90 is 30 more than 60.
   So $60 + 90$ is $120 + 30$, which is 150.
4. (a) $75 + 75 + 4 = 150 + 4 = 154$ (or phrased like above)
   (b) $400 + 400 + 300 = 800 + 300 = 1100$
   (c) $60 + 60 + 30 = 120 + 30 = 150$
   (d) $50 + 50 + 40 = 100 + 40 = 140$

Teaching guidelines
It may be valuable to share the following idea with learners:

What to do when you do not know an addition fact
Suppose you do not know how much $30 + 50$ is.
You can double the smaller number: $30 + 30 = 60$
Can this help you to know how much $30 + 50$ is?
Teaching guidelines
Like all the other work in this section, question 5 is a Mental Mathematics activity. It provides learners with an opportunity to self-assess their knowledge of simple addition and subtraction facts. Learners have to identify the number sentences for which they cannot give the answers quickly and easily, and write them down. Tell learners that the activities that follow may help them to learn how to find the answers quickly and easily. They will then revisit these number sentences when they do question 7 on page 31 of the Learner Book.

Answers
5.

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>9 + 6  = 15</td>
<td>7 + 6  = 13</td>
<td>7 + 8  = 15</td>
<td></td>
</tr>
<tr>
<td>900 + 600 = 1 500</td>
<td>700 + 600 = 1 300</td>
<td>700 + 800 = 1 500</td>
<td></td>
</tr>
<tr>
<td>1 500 – 700 = 800</td>
<td>1 500 – 600 = 900</td>
<td>700 + 700 = 1 400</td>
<td></td>
</tr>
<tr>
<td>60 + 60 = 120</td>
<td>80 + 50 = 130</td>
<td>30 + 100 = 130</td>
<td></td>
</tr>
<tr>
<td>130 – 50 = 80</td>
<td>130 – 40 = 90</td>
<td>1 300 – 300 = 1 000</td>
<td></td>
</tr>
<tr>
<td>13 – 8 = 5</td>
<td>13 – 9 = 4</td>
<td>12 – 3 = 9</td>
<td></td>
</tr>
<tr>
<td>170 – 60 = 110</td>
<td>18 – 6 = 12</td>
<td>13 – 6 = 7</td>
<td></td>
</tr>
<tr>
<td>15 – 8 = 7</td>
<td>150 – 70 = 80</td>
<td>110 – 60 = 50</td>
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<td>16 – 8 = 8</td>
<td>16 – 7 = 9</td>
<td>1 100 – 500 = 600</td>
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<tr>
<td>180 – 90 = 90</td>
<td>18 – 8 = 10</td>
<td>140 – 60 = 80</td>
<td></td>
</tr>
<tr>
<td>17 – 8 = 9</td>
<td>600 + 900 = 1 500</td>
<td>170 – 90 = 80</td>
<td></td>
</tr>
<tr>
<td>9 + 8 = 17</td>
<td>7 + 9 = 16</td>
<td>70 + 40 = 110</td>
<td></td>
</tr>
<tr>
<td>900 + 800 = 1 700</td>
<td>700 + 900 = 1 600</td>
<td>700 + 400 = 1 100</td>
<td></td>
</tr>
<tr>
<td>1 700 – 600 = 1 100</td>
<td>1 600 – 700 = 900</td>
<td>1 100 – 400 = 700</td>
<td></td>
</tr>
</tbody>
</table>

Here is a way to see that 8 + 6 = 14:

6 can be added to 8 in two steps:
8 + 2 = 10 followed by 10 + 4 = 14.
We can write as follows to show this thinking:
8 + 2 + 4 = 14.
You can also think of a number line to know how much 800 + 600 is:

<table>
<thead>
<tr>
<th>0</th>
<th>500</th>
<th>1 000</th>
<th>1 500</th>
<th>2 000</th>
</tr>
</thead>
<tbody>
<tr>
<td>+600</td>
<td>+200</td>
<td>+600</td>
<td>+600</td>
<td>+600</td>
</tr>
</tbody>
</table>

5. Copy the open number sentences for which you cannot give the answers quickly. You will work on them later.

- 9 + 6 = ...
- 900 + 600 = ...
- 1 500 – 600 = ...
- 60 + 60 = ...
- 130 – 50 = ...
- 13 – 8 = ...
- 170 – 60 = ...
- 15 – 8 = ...
- 180 – 90 = ...
- 17 – 8 = ...
- 9 + 8 = ...
- 900 + 800 = ...
- 1 700 – 600 = ...
- 9 + 8 = ...

Here is a way to see that 8 + 6 = 14:

6 can be added to 8 in two steps:
8 + 2 = 10 followed by 10 + 4 = 14.
We can write as follows to show this thinking:
8 + 2 + 4 = 14.
You can also think of a number line to know how much 800 + 600 is:
Mathematical notes

The tinted passage is not just about different ways of representing subtraction on the number line. The passage describes three ways of thinking about subtraction (three “meanings” of subtraction):

- subtraction as finding the difference between two numbers
- subtraction as filling up a gap between two quantities (addressing a shortfall)
- subtraction as taking something away from a given quantity.

When learners have to engage with an “abstract” subtraction question (no context) such as “How much is 1 500 – 700?”, they can interpret the question in any of the three ways – it becomes a choice between three methods of subtraction.

Answers

6. (a) \(50 + 80 = 130\) \(130 – 50 = 80\) \(130 – 80 = 50\)
(b) \(500 + 800 = 1 300\) \(1 300 – 800 = 500\) \(1 300 – 500 = 800\)
(c) \(7 + 7 = 14\) \(14 – 7 = 7\)
(d) \(70 + 70 = 140\) \(140 – 70 = 70\)
Teaching guidelines
Ensure that learners feel free to use any method they prefer when they do question 8. They
should not feel obliged to use the number line. Ideally, they should be able to write most of
the answers straightaway without even thinking about it.

Answers
7. Refer to question 5, two pages back.
8. (a) 150  (b) 1 500  (c) 70    (d) 80
   (e) 800  (f) 700   (g) 90    (h) 900
   (i) 9 000 (j) 9 000 (k) 130   (l) 1 300
   (m) 600 (n) 1 500 (o) 1 400   (p) 600
   (q) 600 (r) 2 200

9. (a) $350 + 80 = 430$  $430 - 80 = 350$  $430 - 350 = 80$
   (b) $550 + 80 = 630$  $630 - 80 = 550$  $630 - 550 = 80$
   (c) $1 350 + 80 = 1 430$  $1 430 - 80 = 1 350$  $1 430 - 1 350 = 80$
   (d) $6 950 + 80 = 7 030$  $7 030 - 80 = 6 950$  $7 030 - 6 950 = 80$
   (e) $6 500 + 800 = 7 300$  $7 300 - 800 = 6 500$  $7 300 - 6 500 = 800$
   (f) $3 930 + 90 = 4 020$  $4 020 - 90 = 3 930$  $4 020 - 3 930 = 90$
Answers

10. and 11.

\[ \begin{array}{cccc}
160 - 100 &=& 60 & 160 - 40 &=& 120 & 160 - 30 &=& 130 \\
100 - 80 &=& 20 & 180 - 50 &=& 130 & 180 - 70 &=& 110 \\
180 - 90 &=& 90 & 180 - 80 &=& 100 & 180 - 60 &=& 120 \\
180 - 100 &=& 80 & 80 - 40 &=& 40 & 80 - 30 &=& 50 \\
100 - 30 &=& 70 & 130 - 80 &=& 50 & 130 - 70 &=& 60 \\
130 - 90 &=& 40 & 130 - 30 &=& 100 & 130 - 60 &=& 70 \\
130 - 100 &=& 30 & 130 - 40 &=& 90 & 130 - 50 &=& 80 \\
100 - 20 &=& 80 & 120 - 80 &=& 40 & 120 - 70 &=& 50 \\
120 - 90 &=& 30 & 120 - 20 &=& 100 & 120 - 60 &=& 60 \\
120 - 100 &=& 20 & 120 - 40 &=& 80 & 120 - 30 &=& 90 \\
100 - 50 &=& 50 & 150 - 80 &=& 70 & 150 - 70 &=& 80 \\
150 - 90 &=& 60 & 150 - 50 &=& 100 & 150 - 60 &=& 90 \\
150 - 100 &=& 50 & 150 - 40 &=& 110 & 50 - 30 &=& 20 \\
100 - 70 &=& 30 & 170 - 80 &=& 90 & 170 - 90 &=& 80 \\
90 - 70 &=& 20 & 170 - 70 &=& 100 & 170 - 60 &=& 110 \\
170 - 100 &=& 70 & 70 - 40 &=& 30 & 70 - 30 &=& 40 \\
100 - 40 &=& 60 & 140 - 80 &=& 60 & 140 - 70 &=& 70 \\
140 - 90 &=& 50 & 140 - 40 &=& 100 & 140 - 60 &=& 80 \\
140 - 100 &=& 40 & 140 - 90 &=& 50 & 140 - 30 &=& 110 \\
100 - 90 &=& 10 & 190 - 80 &=& 110 & 190 - 70 &=& 120 \\
190 - 90 &=& 100 & 190 - 20 &=& 170 & 190 - 60 &=& 130 \\
190 - 100 &=& 90 & 190 - 40 &=& 150 & 190 - 30 &=& 160 \\
100 - 60 &=& 40 & 160 - 80 &=& 80 & 160 - 70 &=& 90 \\
160 - 90 &=& 70 & 160 - 60 &=& 100 & 160 - 50 &=& 110 \\
\end{array} \]

10. Copy the number sentences for which you cannot find the answers quickly.

\[ \begin{array}{cccc}
160 - 100 &=& \ldots & 160 - 40 &=& \ldots & 160 - 30 &=& \ldots \\
100 - 80 &=& \ldots & 180 - 50 &=& \ldots & 180 - 70 &=& \ldots \\
180 - 90 &=& \ldots & 180 - 80 &=& \ldots & 180 - 60 &=& \ldots \\
180 - 100 &=& \ldots & 80 - 40 &=& \ldots & 80 - 30 &=& \ldots \\
100 - 30 &=& \ldots & 130 - 80 &=& \ldots & 130 - 70 &=& \ldots \\
130 - 90 &=& \ldots & 130 - 30 &=& \ldots & 130 - 60 &=& \ldots \\
130 - 100 &=& \ldots & 130 - 40 &=& \ldots & 130 - 50 &=& \ldots \\
100 - 20 &=& \ldots & 120 - 80 &=& \ldots & 120 - 70 &=& \ldots \\
120 - 90 &=& \ldots & 120 - 20 &=& \ldots & 120 - 60 &=& \ldots \\
120 - 100 &=& \ldots & 120 - 40 &=& \ldots & 120 - 30 &=& \ldots \\
100 - 50 &=& \ldots & 150 - 80 &=& \ldots & 150 - 70 &=& \ldots \\
150 - 90 &=& \ldots & 150 - 50 &=& \ldots & 150 - 60 &=& \ldots \\
150 - 100 &=& \ldots & 150 - 40 &=& \ldots & 50 - 30 &=& \ldots \\
100 - 70 &=& \ldots & 170 - 80 &=& \ldots & 170 - 90 &=& \ldots \\
90 - 70 &=& \ldots & 170 - 70 &=& \ldots & 170 - 60 &=& \ldots \\
170 - 100 &=& \ldots & 70 - 40 &=& \ldots & 70 - 30 &=& \ldots \\
100 - 40 &=& \ldots & 140 - 80 &=& \ldots & 140 - 70 &=& \ldots \\
140 - 90 &=& \ldots & 140 - 40 &=& \ldots & 140 - 60 &=& \ldots \\
140 - 100 &=& \ldots & 140 - 90 &=& \ldots & 140 - 30 &=& \ldots \\
100 - 90 &=& \ldots & 190 - 80 &=& \ldots & 190 - 70 &=& \ldots \\
190 - 90 &=& \ldots & 190 - 20 &=& \ldots & 190 - 60 &=& \ldots \\
190 - 100 &=& \ldots & 190 - 40 &=& \ldots & 190 - 30 &=& \ldots \\
100 - 60 &=& \ldots & 160 - 80 &=& \ldots & 160 - 70 &=& \ldots \\
160 - 90 &=& \ldots & 160 - 60 &=& \ldots & 160 - 50 &=& \ldots \\
\end{array} \]

11. Now complete the sentences you have copied in question 10. You may work from the facts that you know or work in any other way you prefer.
3.4 Add and subtract multiples of 100 and 1 000

**Teaching guidelines**
Work through the tinted passage with learners. Make them aware that filling up to the nearest 100 or 1 000 makes the subtraction calculations simpler and easier.

**Answers**

1. (a) 3 600 + 400 → 4 000 + 1 300 = 5 300
   
   \[5 300 - 1 700 = 3 600\] and \[5 300 - 3 600 = 1 700\]

   (b) 3 800 + 200 → 4 000 + 400 = 4 400
   
   \[4 400 - 600 = 3 800\] and \[4 400 - 3 800 = 600\]

   (c) 3 500 + 500 → 4 000 + 400 = 4 400
   
   \[4 400 - 900 = 3 500\] and \[4 400 - 3 500 = 900\]

   (d) 3 700 + 300 → 4 000 + 1 300 = 5 300
   
   \[5 300 - 1 600 = 3 700\] and \[5 300 - 3 700 = 1 600\]

2. 3 700 + 300 → 4 000 + 1 300 = 5 300
   
   \[5 300 - 1 600 = 3 700\] and \[5 300 - 3 700 = 1 600\]

3. 2 700 + 300 → 3 000 + 3 500 = 6 500
   
   So, 6 500 - 2 700 = 3 800 (from 300 + 3 500)
   and 3 800 + 200 → 4 000 + 2 500 = 6 500
   So, 6 500 - 3 800 = 2 700 (from 200 + 2 500)
4. (a) 5 000  
   (b) 5 000  
   (c) 5 000  
5. Learners check and correct their answers.  
6. Learners copy the number sentences for which they cannot find the answers quickly.  
7. Learners complete their copied number sentences in any way they prefer.

\[
\begin{align*}
360 - 80 &= 280 & 360 + 90 &= 450 & 760 - 670 &= 90 \\
560 - 480 &= 80 & 680 + 70 &= 750 & 430 - 270 &= 160 \\
380 - 90 &= 290 & 780 + 80 &= 860 & 780 - 60 &= 720 \\
720 - 50 &= 670 & 770 + 40 &= 810 & 940 - 70 &= 870 \\
810 - 730 &= 80 & 330 + 80 &= 410 & 670 - 90 &= 580 \\
3 200 - 900 &= 2 300 & 2 300 + 900 &= 3 200 \\
6 700 - 500 &= 6 200 & 3 500 + 800 &= 4 300 \\
4 500 - 900 &= 3 600 & 3 600 + 900 &= 4 500 \\
8 400 + 800 &= 9 200 & 9 200 - 800 &= 8 400 \\
9 200 - 8 400 &= 800 & 5 500 + 700 &= 6 200 \\
6 200 - 700 &= 5 500 & 6 200 - 5 500 &= 700 \\
7 200 - 700 &= 6 500 & 7 200 - 800 &= 6 400 \\
7 300 - 800 &= 6 500 & 7 400 - 900 &= 6 500
\end{align*}
\]

4. How much is each of the following? If it will help you, you may think of movements on the number line. 
   (a) 1 700 + 900 + 700 + 800 + 900 
   (b) 800 + 500 + 900 + 400 + 800 + 700 + 900 
   (c) 1 900 + 6 000 + 800 + 500 + 400

5. Your answers for questions 4(a), (b) and (c) should be the same. If they are not, you have made mistakes. Find and correct your mistakes. 
6. Copy the number sentences for which you cannot find the answers quickly.

\[
\begin{align*}
360 - 80 &= \ldots & 360 + 90 &= \ldots & 760 - 670 &= \ldots \\
560 - 480 &= \ldots & 680 + 70 &= \ldots & 430 - 270 &= \ldots \\
380 - 90 &= \ldots & 780 + 80 &= \ldots & 780 - 60 &= \ldots \\
720 - 50 &= \ldots & 770 + 40 &= \ldots & 940 - 70 &= \ldots \\
810 - 730 &= \ldots & 330 + 80 &= \ldots & 670 - 90 &= \ldots \\
3 200 - 900 &= \ldots & 2 300 + 900 &= \ldots \\
6 700 - 500 &= \ldots & 3 500 + 800 &= \ldots \\
4 500 - 900 &= \ldots & 3 600 + 900 &= \ldots \\
8 400 + 800 &= \ldots & 9 200 - 800 &= \ldots \\
9 200 - 8 400 &= \ldots & 5 500 + 700 &= \ldots \\
6 200 - 700 &= \ldots & 6 200 - 5 500 &= \ldots \\
7 200 - 700 &= \ldots & 7 200 - 800 &= \ldots \\
7 300 - 800 &= \ldots & 7 400 - 900 &= \ldots \\
\end{align*}
\]

7. Now complete the number sentences that you have copied in question 6. You may work from the facts that you know or work in any other way you prefer.
3.5 Rounding off and compensating

**Teaching guidelines**

Use the tinted passages to make learners aware of various ways to do subtraction. You can do some more examples with different numbers on the board.

**Answers**

1. Any one of the following:
   - 3 756 + 44 → 4 000 + 1 254 = 5 254
   - So, 5 254 − 3 756 → 44 + 1 254 = 1 498
   - or
   - 3 756 + 4 → 3 760 + 40 → 3 800 + 200 → 4 000 + 1 254 = 5 254
   - So, 5 254 − 3 756 → 4 + 40 + 200 + 1 254 = 1 498

2. (a) 3 643
   (b) 4 628
   (c) 3 694
   (d) 5 326

3. (a) 8 000 − 3 000 = 5 000
   - 800 − 200 = 600
   - 50 − 40 = 10
   - 6 − 3 = 3
   - 5 000 + 600 + 10 + 3 = 5 613
   - So, 8 856 − 3 243 = 5 613
   - (b) 6 000 − 1 000 = 5 000
   - 800 − 500 = 300
   - 70 − 40 = 30
   - 6 − 2 = 4
   - 5 000 + 300 + 30 + 4 = 5 334
   - So, 6 876 − 1 542 = 5 334
Notes on questions
Question 4 is intended to prepare learners for the explanation in the tinted passage.

Teaching guidelines
Two closely related methods of subtraction are described in the two tinted passages – the underlying strategy in both methods is to replace the place value expansion of the bigger number with a different decomposition of the number.
Emphasise replacement as the underlying strategy when you do examples of both methods on the board.

Answers
4. (a) 543
   (b) 544
5. (a) \(6000 - 2000 = 4000\)
   \(900 - 800 = 100\)
   \(90 - 60 = 30\)
   \(9 - 6 = 3\)
   So, \(6999 - 2866 = 4000 + 100 + 30 + 3 = 4133\)
   (b) Add 544; \(7543 - 2866 = 4133 + 544 = 4677\)
   (c) \(4677 + 2866 = 7543\)
6. (a) 3648
   (b) 4486
7. Yes, it is.
8. \(13 - 6 = 7\)
   \(130 - 60 = 70\)
   \(1400 - 800 = 600\)
   \(6000 - 2000 = 4000\)
   So, \(7543 - 2866 = 4000 + 600 + 70 + 7 = 4677\)
Mathematical notes
“Transfer” as mentioned in the tinted passage was traditionally referred to as “borrowing”.

Teaching guidelines
Note that learners are not required to perform any subtractions in question 9. The aim is to focus their attention on the step prior to actually subtracting (as they will do in question 10), namely the replacement.

Answers
9.  
   (a)  $8000 + 400 + 30 + 2$ → $7000 + 1300 + 120 + 12$
   (b)  $9000 + 10 + 4$ → $8000 + 900 + 100 + 14$
   (c)  $7000 + 500 + 60 + 6$ → $6000 + 1400 + 150 + 16$
   (d)  $8000 + 100 + 40 + 1$ → $7000 + 1000 + 130 + 11$

10. (a)  $2534$  (b)  $3116$  (c)  $1668$  (d)  $2243$

3.6 Use brackets to describe your thinking

Teaching guidelines
Learners need to access the information recorded in this step of the calculation in the tinted passage, but may be challenged by what the brackets actually mean here:

$$(7000 + 1000) + (100 + 100) + (20 + 10) + 5$$

$= 7000 + (1000 + 100) + (100 + 20) + (10 + 5)$$

The different placing of the brackets in the two lines is the conventional mathematical way of indicating two different orders in performing additions, which are possible because of the associative property of addition. In words:

“Instead of doing $(7000 + 1000) + (100 + 100) + (20 + 10) + 5$ by doing the calculations inside brackets first, one may do $7000 + (1000 + 100) + (100 + 20) + (10 + 5)$ by doing the calculations inside brackets first.”

Using horizontal curly brackets is a different way to represent the same rearrangement, and may help learners to understand more quickly:

$$= 7000 + 1000 + 100 + 100 + 20 + 10 + 5$$

Use the example in the tinted passage to explain the rearrangement of the order of additions, and how this may be represented in two ways: with ordinary brackets and with horizontal curly brackets.
Mathematical notes

The associative property of addition provides the logical basis for replacing the place value expansion of a number with a different expansion. The associative property means that when you have to add a collection of numbers, you can group (associate) them in any way you like. Using brackets is one of a variety of ways to show a particular choice of what numbers are grouped together for the purposes of addition. Questions 1 and 2 are about subtraction; then the focus shifts to addition.

The replacement of 6 000 + 400 + 20 + 5 with 5 000 + 1 300 + 110 + 15 in question 2 involves the associative property only, but the replacement of (5 000 + 200 + 30 + 5) + (3 000 + 300 + 50 + 2) with (5 000 + 3 000) + (200 + 300) + (30 + 50) + (5 + 2) involves the associative as well as the commutative property of addition.

Answers
1. 9 000 + 200 + 40 + 5
   = (8 000 + 1 000) + (100 + 100) + (30 + 10) + 5
   = 8 000 + (1 000 + 100) + (100 + 30) + (10 + 5)
   = 8 000 + 1 100 + 130 + 15
2. 6 425
   = 6 000 + 400 + 20 + 5
   = 5 000 + 1 000 + 300 + 100 + 10 + 10 + 5
   = 5 000 + 1 300 + 110 + 15

Teaching guidelines

With a view to get yourself informed about the state of your learners’ grasp of addition, you may ask them to calculate 6 364 + 2 435 and 6 364 + 2 877 on a loose sheet of paper and take it in so that you can later analyse their work.

Then demonstrate how 5 235 + 3 352 can be calculated by breaking each number down into place value parts, rearranging the parts, adding the similar parts and building up the answer, as described in the first tinted passage.

When learners have completed question 4, ask them to again calculate 6 364 + 2 435 on a loose sheet of paper and hand it in. This will help you to assess the impact of your presentation and the practice learners experienced by doing questions 3 and 4.

Answers
3. 5 235 + 3 352
   = (5 000 + 200 + 30 + 5) + (3 000 + 300 + 50 + 2)
   = (5 000 + 3 000) + (200 + 300) + (30 + 50) + (5 + 2)
   = 8 000 + 500 + 80 + 7
   = 8 587
4. (a) 9 416
   (b) 8 789
**Mathematical notes**
A different format for addition and subtraction is introduced in Section 3.7 (page 40 of the Learner Book) as a first step towards adding and subtracting in columns (Term 3).

**Answers**
5. (a) 7 000 + 800 + 90 + 6
   (b) 4 000 + 200 + 30 + 1
   (c) 7 000 + 600 + 60 + 3
6. (a) 8 275
   (b) 7 346
   (c) 7 783
   (d) 6 552

**Teaching guidelines**
When learners have completed question 6, let them again calculate 6 364 + 2 877 on a loose sheet of paper and hand it in, to allow you to assess whether the class has improved as a result of what happened in the classroom.

You may utilise the example in the first tinted passage to point out that the method they use for addition is only possible because numbers can be added in any order (the associative property of addition).

**Answers**
7. (a) 420
   (b) 440
   (c) 4 200
   (d) 4 550
8. \[ 6 \text{ 154} - 2 \text{ 769} = (155 + 5 \text{ 999}) - 2 \text{ 769} \]
   \[ = 155 + (5 \text{ 999} - 2 \text{ 769}) \]
   \[ = 155 + 3 \text{ 230} \]
   \[ = 3 \text{ 385} \]
3.7 Add and subtract 4-digit numbers

Teaching guidelines

Place value cards, included in the Addendum on pages 398 to 411 (which you may copy and laminate), can be used to act out the content of the tinted passage in the classroom. This will help learners to experience the breaking down of numbers into their place value parts and the rearrangement of the parts, which will not change the total because of the commutative and associative properties of addition.

Learners can work in pairs to form the numbers with their place value cards, and you can do the same by sticking your large place value cards on the board.

Ask learners to now take the numbers apart. Do the same on the board with another set of large cards so that the above remains on the board.

Ask learners to rearrange the cards so that the thousands cards are together, the hundreds cards are together, the tens cards are together and the units cards are together. Do the same on the board with another set of large cards.

Ask learners to add the numbers in each group and to represent the answer with cards in each case. Also do this on the board.

The cards (parts) can be rearranged again. The answer 5 761 is now clear.

Ask learners to write down what they did with the cards, using the tinted passage as a guideline if they wish.

Answers

1. (a) 8 681 (b) 9 022 (c) 6 771 (d) 9 640 (e) 4 742 (f) 9 421
2. (a) 8 681 – 6 297 = 2 384 8 681 – 2 384 = 6 297
   (b) 9 022 – 7 834 = 1 188 9 022 – 1 188 = 7 834
   (c) 6 771 – 3 902 = 2 869 6 771 – 2 869 = 3 902
   (d) 9 640 – 6 771 = 2 869 9 640 – 2 869 = 6 771
   (e) 4 742 – 1 795 = 2 947 4 742 – 2 947 = 1 795
   (f) 9 421 – 5 432 = 3 989 9 421 – 3 989 = 5 432
Teaching guidelines

Some learners are challenged by subtraction that involves “borrowing”.

In the explanation in the tinted passage, subtraction is not described as a stepwise process working “from right to left” through the different place value columns. Instead, with a view to make the mathematical nature of the process more transparent, subtraction is described as a series of steps enacted on the numbers in expanded notation.

Learners should preferably do a subtraction question that does not require “borrowing”, for example 7 854 – 2 532, before engaging with the tinted passage. Demonstrate a simple case of subtraction on the board, for example 6 768 – 3 254:

6 768 = 6 000 + 700 + 60 + 8
3 254 = 3 000 + 200 + 50 + 4
6 768 – 3 254 = 3 000 + 500 + 10 + 4
= 3 514

To confront learners with the challenge involved in more difficult cases, you may then write the task in the tinted passage on the board, leaving some space below the first line:

7 234 = 7 000 + 200 + 30 + 4
3 876 = 3 000 + 800 + 70 + 6
7 234 – 3 876 = ?

The problem in this case is that 6 cannot be subtracted from 4, the 70 cannot be subtracted from 30 and 800 cannot be subtracted from 200. Learners may be given some time to propose a solution to the problem, either of their own thinking or by consulting the tinted passage in their textbooks.

Answers

3. (a) 3 756 (b) 1 548 (c) 3 583 (d) 3 649
4. (a) 8 436
(b) Learners check and correct their answers to question 3(d).
5. (a) 7 632 – 3 876 = 633 + (6 999 – 3 876) = 633 + 3 123 = 3 756
(b) Learners check their answers to questions 3(b) and (c) in the same way.
6. R4 367
7. R1 339
8. R3 777

Subtraction can be done by taking the following steps:

Step 1: Break down both numbers into their place value parts.

Step 2: Make changes to the place value parts of the first number if necessary.

Step 3: Subtract each kind of place value part separately. This means subtract thousands from thousands, hundreds from hundreds, tens from tens and units from units.

Step 4: Combine the parts to build up the answer.

Example: Calculate 7 234 – 3 876.

Step 1: 7 234 = 7 000 + 200 + 30 + 4
3 876 = 3 000 + 800 + 70 + 6
Step 2: 7 234 – 3 876 = (6 000 – 3 000) + (1 100 – 800) + (120 – 70) + (14 – 6)
= 3 000 + 300 + 50 + 8
Step 3: 7 234 – 3 876 = 6 000 + 200 + 30 + 4
3 876 = 3 000 + 800 + 70 + 6
Step 4: 7 234 – 3 876 = 3 358

3. Calculate each of the following by using the above method.
   (a) 7 632 – 3 876
   (b) 5 114 – 3 566
   (c) 6 457 – 2 874
   (d) 8 436 – 4 787
4. (a) Calculate 4 787 + 3 649.
   (b) Is your answer for question 3(d) correct? If not, do it again.
5. (a) 7 632 – 3 876 can also be calculated by replacing 7 632 by 633 + 6 999. Do this and check whether you get the same answer as when you did question 3(a).
   (b) Check your answers for questions 3(b) and (c) in the same way.
6. Paul earned R8 245 and used R3 878 to buy a bicycle. How much money does he have left?
7. Mustafizur earns R5 225 per week and Cyril earns R3 886. How much more than Cyril does Mustafizur earn?
8. Carla has saved R5 678 to buy a leather couch that costs R9 455. How much more must she save before she can buy the couch?
3.8 Round off, estimate and solve problems

**Teaching guidelines**

Rounding off means that each of a group of different numbers is represented by the same number. For example, when rounding off to the nearest ten, each of the numbers 25, 26, 27, 28, 29, 30, 31, 32, 33 and 34 is represented by 30:

```
25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44
```

Similarly, when rounding off to the nearest hundred, each of the numbers 250, 251, 252, 253, 254, 255, 256, 257, ............... 345, 346, 347, 348 and 349 is represented by 300:

```
240 250 260 270 280 290 300 310 320 330 340 350
```

It is sometimes useful to estimate approximate answers for addition and subtraction. A good way to do this is to round off the numbers, and to calculate using the rounded-off numbers.

For example, 7 258 – 3 574 can be approximated by rounding off to the nearest thousand:

- $7 000 – 4 000 = 3 000$, so $7 258 – 3 574$ is approximately $3 000$.
- $7 258 – 3 574$ can also be approximated by rounding off to the nearest hundred:
- $7 300 – 3 600 = 3 700$, so $7 258 – 3 574$ is approximately $3 700$.

The table below shows how rounding off to the nearest 100 is done. For example, all numbers between 150 and 249, including 150 and 249, are rounded off to 200.

<table>
<thead>
<tr>
<th>Range</th>
<th>Rounded off to nearest 100</th>
<th>Examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 to 49</td>
<td>0</td>
<td>14, 34, 48, 49</td>
</tr>
<tr>
<td>50 to 149</td>
<td>100</td>
<td>50, 73, 101, 149</td>
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<tr>
<td>150 to 249</td>
<td>200</td>
<td>150, 188, 210, 249</td>
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<td>250 to 349</td>
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<td>250, 277, 325, 349</td>
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<td>350 to 449</td>
<td>400</td>
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<td>450 to 549</td>
<td>500</td>
<td>450, 485, 535, 549</td>
</tr>
<tr>
<td>550 to 649</td>
<td>600</td>
<td>550, 586, 623, 649</td>
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<td>700</td>
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<tr>
<td>1350 to 1449</td>
<td>1400</td>
<td>1350, 1386, 1423, 1449</td>
</tr>
</tbody>
</table>

All the numbers between 250 and 349, including 250 and 349, are rounded off to 300.
Answers

1. (a) 249  
   (b) 150

2. (a) 649  
   (b) 550

3. (a) Any five numbers between 350 and 449, including 350 and 449.  
   (b) Any five numbers between 1150 and 1249, including both 1150 and 1249.

4. (a) 1649  
   (b) 1550

5. (a) Any five numbers between 750 and 849, including both 750 and 849.  
   (b) Any five numbers between 2250 and 2349, including both 2250 and 2349.  
   (c) Any five numbers between 3650 and 3749, including both 3650 and 3749.

6. 500 500 600 1100 3200 3300 8700

7. | Range          | Rounded off to nearest 1000 | Examples |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
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<tbody>
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<td>4500 to 5499</td>
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<td>4540, 5340, 4801, 5489</td>
</tr>
<tr>
<td>5500 to 6499</td>
<td>6000</td>
<td>5600, 6309, 6010, 6459</td>
</tr>
<tr>
<td>6500 to 7499</td>
<td>7000</td>
<td>6590, 6880, 7459, 7009</td>
</tr>
</tbody>
</table>

8. 2499 to nearest 1000: 2000  
   2499 to nearest 100: 2500

---

1. (a) What is the biggest number that is rounded off to 200?  
   (b) What is the smallest number that is rounded off to 200?

2. (a) What is the biggest number that is rounded off to 600?  
   (b) What is the smallest number that is rounded off to 600?

3. (a) Write five different numbers that are all rounded off to 400.  
   (b) Write five different numbers that are all rounded off to 1200.

4. (a) What is the biggest number that is rounded off to 1600?  
   (b) What is the smallest number that is rounded off to 1600?

5. (a) Write five different numbers that are all rounded off to 800.  
   (b) Write five different numbers that are all rounded off to 2300.  
   (c) Write five different numbers that are all rounded off to 3700.

6. Round off each of the following numbers to the nearest 100:  
   513 548 550 1111 3249 3250 8749

   Rounding off to the nearest 1000 works in a similar way:  
   3499 rounded off to the nearest 1000 is 3000 but 3500 rounded off to the nearest 1000 is 4000.

<table>
<thead>
<tr>
<th>Range</th>
<th>Rounded off to nearest 1000</th>
<th>Examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 to 499</td>
<td>0</td>
<td>0, 40, 480, 499</td>
</tr>
<tr>
<td>500 to 1499</td>
<td>1000</td>
<td>500, 730, 1000, 1499</td>
</tr>
<tr>
<td>1500 to 2499</td>
<td>2000</td>
<td>1500, 1800, 2499</td>
</tr>
<tr>
<td>2500 to 3499</td>
<td>3000</td>
<td>2500, 2800, 3499</td>
</tr>
<tr>
<td>3500 to 4499</td>
<td>4000</td>
<td>3500, 3800, 4499</td>
</tr>
</tbody>
</table>

7. Continue the above table for numbers from 4500 up to 7499.

8. Round off 2499 to the nearest 1000, and to the nearest 100.
Teaching guidelines
Learners’ efforts should be directed at understanding and solving the stated problem, not at trying to identify the correct operation as quickly as possible and applying a recipe to execute it.

Answers

9. Rounded off to the nearest...

<table>
<thead>
<tr>
<th></th>
<th>10</th>
<th>100</th>
<th>1 000</th>
</tr>
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<tbody>
<tr>
<td>2 317</td>
<td>2 320</td>
<td>2 300</td>
<td>2 000</td>
</tr>
<tr>
<td>2 344</td>
<td>2 340</td>
<td>2 300</td>
<td>2 000</td>
</tr>
<tr>
<td>2 345</td>
<td>2 350</td>
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<tr>
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<td>2 350</td>
<td>2 300</td>
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<tr>
<td>2 499</td>
<td>2 500</td>
<td>2 500</td>
<td>2 000</td>
</tr>
<tr>
<td>8 005</td>
<td>8 010</td>
<td>8 000</td>
<td>8 000</td>
</tr>
</tbody>
</table>

10. (a) $2 000 + 5 000 = 7 000$
    (b) $2 400 + 4 500 = 6 900$
    (c) $2 370 + 4 520 = 6 890$

11. (a) $6 000 + 3 000 = 9 000$
    (b) $9 000 - 4 000 = 5 000$
    (c) $9 000 - 5 000 = 4 000$
    (d) $3 000 + 6 000 = 9 000$

12. (a) $6 500 + 3 200 = 9 700$
    (b) $9 000 - 3 800 = 5 200$
    (c) $9 300 - 4 900 = 4 400$
    (d) $3 500 + 5 600 = 9 100$

13. (a) 9 704
    (b) 5 244
    (c) 4 489
    (d) 9 063

14. (a) 11(a) 704
    11(b) 244
    11(c) 489
    11(d) 63
    (b) 12(a) 4
    12(b) 44
    12(c) 89
    12(d) 37

9. Round off each of the following numbers to the nearest 10, the nearest 100, and the nearest 1 000.

<p>| | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>2 317</td>
<td>2 344</td>
<td>2 345</td>
<td>2 349</td>
</tr>
<tr>
<td>2 499</td>
<td>8 005</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

10. Estimate in three ways how much 2 366 + 4 522 is:
    (a) by first rounding off each number to the nearest 1000
    (b) by first rounding off each number to the nearest 100
    (c) by first rounding off each number to the nearest 10.

11. Estimate the answers to each of the following questions by rounding off the numbers to the nearest 1 000.
    (a) Lennie needs 6 468 bricks to build a small house and 3 236 bricks to build a wall around his plot. How many bricks does Lennie need in total?
    (b) The bricklayer has already used 3 786 bricks of the 9 030 bricks that were delivered at a building site. How many bricks are still left?
    (c) A school ordered 9 348 books from a supplier. When the school started in January, 4 859 books had been received. How many books are still outstanding?
    (d) There are 3 478 learners in School District A and 5 585 learners in School District B. How many learners are there in the two districts together?

12. Make new estimates for questions 11(a) to (d), this time by rounding off the numbers to the nearest 10.

13. Make accurate calculations to find the exact answers for questions 11(a) to (d).

The difference between an estimate and an accurate answer is called the error. For example, you can estimate that 3 747 + 4 874 is 9 000. The accurate answer is 8 621. The error in this case is 379.

14. (a) Calculate the errors for your estimates in question 11.
    (b) Calculate the errors for your estimates in question 12.
Grade 5 Term 1 Unit 4  Numeric patterns

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.1 Patterns in the tables</td>
<td>Introducing numeric patterns</td>
<td>45</td>
</tr>
<tr>
<td>4.2 Equivalent flow diagrams</td>
<td>Consolidating sequences of multiples</td>
<td>46 to 47</td>
</tr>
<tr>
<td>4.3 Sequences of non-multiples</td>
<td>Developing properties of multiplication (order and grouping)</td>
<td>48 to 51</td>
</tr>
<tr>
<td>4.4 Flow diagrams and rules</td>
<td>Finding rules for families of sequences with a constant difference</td>
<td>51 to 53</td>
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<tr>
<td></td>
<td>Consolidating completing flow diagrams</td>
<td>54</td>
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</tbody>
</table>

**CAPS time allocation** 4 hours

**CAPS page references** 18 to 19 and 136 to 139

**Mathematical background**

Numeric patterns, as part of the Content Area “Patterns, Functions and Algebra”, should serve as building blocks to develop the basic concepts of algebra in the Senior and FET phases. The study of numeric patterns should develop the idea of a relationship between two variable quantities, for example:

<table>
<thead>
<tr>
<th>One variable quantity (the “input numbers”)</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
</tr>
</thead>
<tbody>
<tr>
<td>Another variable quantity (the “output numbers”)</td>
<td>4</td>
<td>7</td>
<td>10</td>
<td>13</td>
<td>16</td>
<td>19</td>
<td>22</td>
<td>25</td>
<td>28</td>
<td>31</td>
<td>34</td>
</tr>
</tbody>
</table>

The word “pattern” means that something is repeated. In the above case, the sequence 4, 7, 10, 13, 16, … can be formed by repeatedly adding 3. This pattern in the sequence can be formed by performing the same calculation each time to move from one number to the next. Such a pattern is called a **recursive pattern**. The word “recur” means that something occurs repeatedly or repeats itself.

The above sequence of output numbers can also be formed by multiplying each input number by 3 and adding 1:

<table>
<thead>
<tr>
<th>One variable quantity (the “input numbers”)</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
</tr>
</thead>
<tbody>
<tr>
<td>Another variable quantity (the “output numbers”)</td>
<td>3 × 1 + 1</td>
<td>3 × 2 + 1</td>
<td>3 × 3 + 1</td>
<td>3 × 4 + 1</td>
<td>3 × 5 + 1</td>
<td>3 × 6 + 1</td>
<td>3 × 7 + 1</td>
<td>3 × 8 + 1</td>
<td>3 × 9 + 1</td>
<td>3 × 10 + 1</td>
<td>3 × 11 + 1</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>7</td>
<td>10</td>
<td>13</td>
<td>16</td>
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<td>22</td>
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<td>31</td>
<td>34</td>
</tr>
</tbody>
</table>

A relationship between two variable quantities, in which each value of the second quantity is uniquely determined by the corresponding value of the first quantity, is called a **function** – the middle word in the CAPS title for this Content Area.

In the above case, the link between the input and output numbers (also called the independent and dependent variables) is given by the calculation plan (rule) “multiply the input number by 3 and add 1”, which can also be represented as 3 × □ + 1, or with this flow diagram:

```
input number  × 3 + 1  output number
```
Overview of the approach to Numeric Patterns
The work on numeric patterns was designed along the following principles and guides:

Sequences of multiples
First, sequences of multiples (the “tables”) are thoroughly developed and reinforced with the intention that fluency with multiples will serve as a building block to study other sequences.

It is established that all the sequences of multiples are of the same type:

- The multiples of $k$ have a constant difference of $+k$ between consecutive numbers (the “horizontal” pattern).
- The multiples of $k$ have a rule of the form $\times k$ (the “vertical” pattern).

Families of sequences
Then it is established that sequences that are obviously different, can be the same in some respects. For example, the sequences in the series of sequences below are clearly different, but they are nevertheless the same in that they share the property that they have a constant difference of 4:

- $3, 7, 11, 15, 19, 23, 27, ...$
- $4, 8, 12, 16, 20, 24, 28, ...$
- $5, 9, 13, 17, 21, 25, 29, ...$
- $6, 10, 14, 18, 22, 26, 30, ...$

We call them “a family of sequences”.

By comparing the flow diagrams, tables and rules with a focus on the relationship between these sequences, a relationship between the calculation rules for these families of sequences can be identified, like this:

<table>
<thead>
<tr>
<th>Sequence</th>
<th>Description in words</th>
<th>Flow diagram/Rule</th>
</tr>
</thead>
<tbody>
<tr>
<td>$3, 7, 11, 15, 19, 23, 27, ...$</td>
<td>One less than multiples of 4</td>
<td>$\times 4 - 1$</td>
</tr>
<tr>
<td>$4, 8, 12, 16, 20, 24, 28, ...$</td>
<td>Multiples of 4</td>
<td>Easy! Start here! $\times 4$</td>
</tr>
<tr>
<td>$6, 10, 14, 18, 22, 26, 30, ...$</td>
<td>Two more than multiples of 4</td>
<td>$\times 4 + 2$</td>
</tr>
</tbody>
</table>
4.1 Patterns in the tables

**Teaching guidelines**

In starting our work on **sequences**, we connect it to the familiar work of counting in multiples and counting on in multiples.

You can therefore tell learners that it is not really new work; it is only different in the way it is represented. When counting, we usually do so **verbally**, but in our work with sequences we have to **write** it down.

Of course our focus is also different. Whereas our counting activities are mostly aimed at number concept development and mental fluency, our work with numeric patterns (number patterns) studies the relationships between the numbers in the sequences we produce.

And we ask different questions, for example:

*If Sally would continue counting 5, 10, 15, 20, …*

- what would the 100th number that she counted be?
- would she count 436?

Our work on numeric patterns must develop the knowledge that will enable Sally to **calculate** the 100th number **instead of actually counting** all the way up to the 100th number, and to **reason** whether 436 is in the sequence or not, without actually having to count past 436.

**Answers**

1. | × | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
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<td>12</td>
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<td>7</td>
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<td>14</td>
<td>21</td>
<td>28</td>
<td>35</td>
<td>42</td>
<td>49</td>
<td>56</td>
<td>63</td>
<td>70</td>
</tr>
</tbody>
</table>

2. Learners discuss methods used to complete the table, e.g. counting on in multiples.
3. Learners discuss the patterns that they see in the table.
Teaching guidelines
You should let learners discuss what methods they are using, to help them realise that the different methods (horizontal differences and vertical rule) are useful for different purposes, so that they can make good decisions when deciding which method to use:

- To calculate the next five numbers, counting on in multiples is a good method.
- Counting on is not a good method to determine the 100th number. Rather use the multiplication rule.

Critical knowledge
The work in the next section (sequences of multiples) requires that learners fully understand the rule for sequences of multiples. It is therefore important that you consolidate this knowledge with learners.

Notes on questions
It is important that learners understand that flow diagrams and tables are equivalent representations. You should let learners discuss how the one is transformed into the other, and how they contain the same information.

Answers
4. (a) ... , 18, 20, 22, 24, 26  
   100th number: 200
(b) ... , 24, 27, 30, 33, 36  
   100th number: 300
(c) ... , 40, 45, 50, 55, 60  
   100th number: 500
(d) ... , 56, 63, 70, 77, 84  
   100th number: 700
(e) ... , 72, 81, 90, 99, 108  
   100th number: 900
(f) ... , 80, 90, 100, 110, 120  
   100th number: 1 000

5. 

For every consecutive input number the output number increases by 6.
The output number is always 6 times the input number.
4.2 Equivalent flow diagrams

**Teaching guidelines**

The main teaching and learning idea in this section is twofold:

- Establishing the concept of equivalence of flow diagrams (flow diagrams giving the same output numbers for the same input numbers) with the implication that one can therefore choose to use the one in the place of the other for specific purposes.
- Applying the concept of equivalence to make calculation easier, especially to make mental calculation easier.

You should make sure that learners understand flow diagrams with two operators – see the note on the next page.

**Answers**

1. (a)

   A
   1
   2
   3
   4
   12
   × 2
   2
   4
   6
   8
   12
   × 2
   4
   8
   12
   16
   48

   B
   1
   2
   3
   4
   12
   × 4
   4
   8
   12
   16
   48

(b) The flow diagrams are different in that they have different operators.
   They are the same in that the same input gives the same output.
   They are the same because multiplying by 2 and then by 2 again is the same as multiplying by 4.
Note on order of operations (BODMAS) and flow diagrams

You should make sure that learners understand flow diagrams with two operators.

The flow diagram representation carries an intuitive left-to-right procedure: the first input produces the first output; the second input produces the second output. For example:

```
2  \rightarrow  4  \rightarrow  8
3  \rightarrow  6  \rightarrow  10
4  \rightarrow  8  \rightarrow  12
```

The left-to-right convention means that there is no need to learn rules such as BODMAS for the order of operations (first multiply before you add). BODMAS does not apply in the flow diagrams. For example, the following flow diagram is equivalent to the above.

```
2  \rightarrow  4  \rightarrow  8
3  \rightarrow  5  \rightarrow  10
4  \rightarrow  8  \rightarrow  12
```

The flow diagram's left-to-right procedure plays the same role as brackets in numeric expressions. For example, to calculate the output value for the input 3, the first diagram uses the arithmetic expression \((3 \times 2) + 4\), and the second diagram uses \((3+2) \times 2\), and of course \((3\times2) + 4 = (3+2) \times 2\).

Answers

1. (c) 4 \times 8: double 8 is 16 and double 16 is 32, so 4 \times 8 = 32
   4 \times 9: double 9 is 18 and double 18 is 36, so 4 \times 9 = 36
   4 \times 14: double 14 is 28 and double 28 is 56, so 4 \times 14 = 56
   4 \times 11: double 11 is 22 and double 22 is 44, so 4 \times 11 = 44
   4 \times 23: double 23 is 46 and double 46 is 92, so 4 \times 23 = 92
   8 \times 23 = 2 \times 4 \times 23 = 184 (the previous answer, i.e. 92, doubled again)
   16 \times 14 = 14 \times 2 \times 2 \times 2 \times 2 \rightarrow 14, 28, 56, 112, 224 (double 4 times), so 16 \times 14 = 224
2. (a) For C, D and E: 3 \rightarrow 18, 4 \rightarrow 24, 12 \rightarrow 72
   (b) They have the same output values, so they are equivalent, because 2 \times 3 = 3 \times 2 = 6.
**Teaching guidelines**

In the answer for question 2(c) below, we use brackets to show which operations we are doing first, but you should not insist that learners use brackets.

**Answers**

2. (c) Various possibilities, for example:

- $9 \times 6 = (9 \times 3) \times 2 = 27 \times 2 = 54$
- $9 \times 12 = (9 \times 6) \times 2 = 54 \times 2 = 108$
- $9 \times 24 = (9 \times 12) \times 2 = 108 \times 2 = 216$
- $8 \times 6 = (8 \times 3) \times 2 = 24 \times 2 = 48$
- $11 \times 14 = (11 \times 7) \times 2 = 77 \times 2 = 154$
- $32 \times 12 = (32 \times 3) \times 2 \times 2 = 96 \times 2 \times 2 = 192 \times 2 = 384$
- $14 \times 20 = (14 \times 2) \times 10 = 28 \times 10 = 280$

3. (a) 

<table>
<thead>
<tr>
<th>Flow Diagram</th>
<th>Input</th>
<th>2</th>
<th>4</th>
<th>6</th>
<th>8</th>
<th>10</th>
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<td></td>
<td>12</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>240</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(b) The operators have been swapped in Flow diagrams F and G, but the output values are the same for the same input values, because the order does not matter. The output values of Flow diagram H are the same as for Flow diagrams F and G, but the operator is the product of the two operators, i.e. $\times 10 \times 2$ (or $2 \times 10$).
Answers
3. (c) Various possibilities, for example:
   \[ 9 \times 20 = (9 \times 2) \times 10 = 18 \times 10 = 180 \]
   \[ 20 \times 12 = 10 \times (2 \times 12) = 10 \times 24 = 240 \]
   \[ 20 \times 20 = (2 \times 2) \times (10 \times 10) = 4 \times 100 = 400 \]
   \[ 8 \times 30 = 8 \times 3 \times 10 = 24 \times 10 = 240 \]
   \[ 8 \times 60 = 8 \times 6 \times 10 = 48 \times 10 = 480 \]
   \[ 9 \times 70 = 9 \times 7 \times 10 = 63 \times 10 = 630 \]
   \[ 9 \times 80 = 9 \times 8 \times 10 = 72 \times 10 = 720 \]

4.3 Sequences of non-multiples

Teaching guidelines
We need to thoroughly reinforce sequences of multiples (“the times tables”) so that they will become easy for learners as a building block to study other sequences.

Have some calculators available for question 1.

Critical knowledge
All learners should understand, know and be able to apply the knowledge common to all multiple sequences: the multiples of \( k \) (1) have a constant difference of +\( k \) and (2) have a rule of the form \( \times k \), for example the rule for multiples of 3 is \( \text{Multiple no.} = 3 \times \text{Position no.} \).

Notes on questions
Problem solving is all about asking yourself the right questions, by reformulating a question from new information that you have. For A(c), the original question is: “Is 436 a number in the sequence?” After recognising A as multiples of 3, the question should be reformulated to: “Is 436 a multiple of 3?” followed by “How do I find out if it is a multiple of 3?”

And then you answer your own question: “If 436 divided by 3 has no remainder.” Then you do it (let learners use the calculator): 436 ÷ 3 = 145.333… So 436 is not a multiple of 3. Therefore 436 is not in the sequence 3, 6, 9, 12, …

Answers
1. A (a) …, 21, 24, 27, 30, 33 (b) 300 (c) No
   B (a) …, 28, 32, 36, 40, 44 (b) 400 (c) Yes
   C (a) …, 42, 48, 54, 60, 66 (b) 600 (c) No
Teaching guidelines

Questions 2 to 4 are developmental activities, designed for learners to engage with the problem of finding rules for families of sequences with the same constant difference.

Question 5 is for consolidation. Learners should therefore complete and discuss all these activities.

The activities take learners through the problem (continuing the sequences and finding the 100th number) in different contexts, which all reinforce each other: flow diagrams, tables, rules.

It is important timewise, but especially conceptually, that learners do not have the mindset of answering each question as a stand-alone, isolated question. Rather, the vitally important idea here is that learners will see the relationship between Sequences A, B, C and D and therefore the relationship between the flow diagrams for the different sequences, and the relationships between the rules for the different sequences. For example:

4, 8, 12, 16, 20, ... Multiples of 4 Easy! 100th number = 100 × 4 = 400
5, 9, 14, 17, 21, ... One more than multiples of 4 100th number = 100 × 4 + 1 = 401

If learners can do this, they will have developed a very important and powerful problem-solving tool. It will make the work easy, and they can finish quickly.

Answers

2. (a) Same: the difference between the numbers is 4 in all four sequences.
   Different: each sequence starts with a different number.
   (b) A: ..., 32, 36, 40, 44, 48 100th number: 400
       B: ..., 33, 37, 41, 45, 49 100th number: 401
       C: ..., 34, 38, 42, 46, 50 100th number: 402
       D: ..., 35, 39, 43, 47, 51 100th number: 403
   (c) 436 ÷ 4 = 109, so 436 is a multiple of 4. So, 436 is in Sequence A but not in B, C or D.

3. (a) A: ..., 100 − ×4−0→ ..., 400
       B: ..., 100 − ×4−1→ ..., 401
       C: ..., 100 − ×4−2→ ..., 402
       D: ..., 100 − ×4−3→ ..., 403
   (b) They all have the same multiplication operator −×4 but different addition operators.
Mathematical notes

We emphasise again that for the required learning process and thinking strategy, learners need to concentrate on the relationship between consecutive sequences, flow diagrams and rules. Then, because the multiples are easy, the others follow, for example:

<table>
<thead>
<tr>
<th>Position × 4 + 0</th>
<th>4</th>
<th>8</th>
<th>12</th>
<th>16</th>
<th>20</th>
<th>24</th>
<th>120</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>↓+1</td>
<td>↓+1</td>
<td>↓+1</td>
<td>↓+1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Position × 4 + 1</td>
<td>5</td>
<td>9</td>
<td>13</td>
<td>17</td>
<td>21</td>
<td>25</td>
<td>121</td>
</tr>
<tr>
<td></td>
<td>↓+1</td>
<td>↓+1</td>
<td>↓+1</td>
<td>↓+1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Position × 4 + 2</td>
<td>6</td>
<td>10</td>
<td>14</td>
<td>18</td>
<td>22</td>
<td>26</td>
<td>122</td>
</tr>
<tr>
<td></td>
<td>↓+1</td>
<td>↓+1</td>
<td>↓+1</td>
<td>↓+1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Position × 4 + 3</td>
<td>7</td>
<td>11</td>
<td>15</td>
<td>19</td>
<td>23</td>
<td>27</td>
<td>123</td>
</tr>
</tbody>
</table>

Answers

3. C: ..., 100 \(\times 4\) \(\times 2\) → ..., 402
   D: ..., 100 \(\times 4\) \(\times 3\) → ..., 403

4. (a) Complete this table. Describe and discuss your methods.

<table>
<thead>
<tr>
<th>Position</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>30</th>
</tr>
</thead>
<tbody>
<tr>
<td>Position</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Position</td>
<td>4</td>
<td>8</td>
<td>12</td>
<td>16</td>
<td>20</td>
<td>24</td>
<td>120</td>
</tr>
<tr>
<td>Position</td>
<td>5</td>
<td>9</td>
<td>13</td>
<td>17</td>
<td>21</td>
<td>25</td>
<td>121</td>
</tr>
<tr>
<td>Position</td>
<td>6</td>
<td>10</td>
<td>14</td>
<td>18</td>
<td>22</td>
<td>26</td>
<td>122</td>
</tr>
<tr>
<td>Position</td>
<td>7</td>
<td>11</td>
<td>15</td>
<td>19</td>
<td>23</td>
<td>27</td>
<td>123</td>
</tr>
</tbody>
</table>

(b) All the sequences have a constant difference of 4 and the rules all have \(\times 4\).

5. (a) All the sequences have a constant difference of 5, but different starting numbers.
   (b) A: 500
       B: 501
       C: 502
       D: 503
       E: 504

   (c) No
4.4 Flow diagrams and rules

**Teaching guidelines**
For learners who have grasped the previous work on families of sequences and their flow diagram representations, this is a quick consolidation or reinforcement exercise, maybe leading to new insights. For learners who have not yet grasped the necessary concepts and notation, it offers another opportunity to do so.

**Answers**

1. 
   - 1
   - 2
   - 3
   - 4
   - 100
   - $x \times 4 + 3$
   - 7
   - 11
   - 15
   - 19
   - 403

2. 
   - 3
   - 4
   - 5
   - 20
   - 23
   - $x \times 4 + 3$
   - 15
   - 19
   - 23
   - 83
   - 95

3. 
   - 3
   - 4
   - 5
   - 20
   - 23
   - $x \times 4 + 4$
   - 16
   - 20
   - 24
   - 84
   - 96

4. 
   - 3
   - 4
   - 5
   - 20
   - 23
   - $x \times 5 + 4$
   - 19
   - 24
   - 29
   - 104
   - 119
Grade 5 Term 1 Unit 5  
Whole numbers: Multiplication and division

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<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
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<td>The concept of multiplication</td>
<td>55 to 57</td>
</tr>
<tr>
<td>5.2 Multiplication facts</td>
<td>Mental Mathematics</td>
<td>58 to 59</td>
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<td>5.3 Double, double and double again</td>
<td>Mental Mathematics</td>
<td>59 to 60</td>
</tr>
<tr>
<td>5.4 Multiply by building up from known parts</td>
<td>Breaking down and building up to multiply</td>
<td>61 to 62</td>
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<tr>
<td>5.5 Strengthen your knowledge of multiplication facts</td>
<td>Mental Mathematics</td>
<td>62 to 63</td>
</tr>
<tr>
<td>5.6 Practise multiplication and solve problems</td>
<td>Practice and problem solving</td>
<td>64 to 65</td>
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<tr>
<td>5.7 Multiples, factors and products</td>
<td>Terminology relating to multiplication</td>
<td>65 to 67</td>
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<td>5.8 Division</td>
<td>Using the idea of division as the inverse of multiplication to solve grouping and sharing problems</td>
<td>67 to 68</td>
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**CAPS time allocation**  
6 hours

**CAPS page references**  
13 to 15 and 140 to 143

**Mathematical background**

The break down and build up method of multiplication comprises the following steps:

Step 1: Break down the numbers into place value parts, for example: $36 \times 47 = (30 + 6) \times (40 + 7)$

Step 2: Distribute multiplication over addition: $(30 + 6) \times (40 + 7) = (30 + 6) \times 40 + (30 + 6) \times 7$, and again:

$= 30 \times 40 + 6 \times 40 + 30 \times 7 + 6 \times 7$

Step 3: Calculate the small products by using known facts:

$= 1200 + 240 + 210 + 42$

Step 4: Add up the parts:

$= 1692$

Division is normally performed by adding up multiples of the divisor. For example, the following combination of multiples can be used to calculate $578 \div 7$:

$50 \times 7 = 350$

$20 \times 7 = 140$, hence $70 \times 7 = 350 + 140 = 490$

$10 \times 7 = 70$, hence $80 \times 7 = 490 + 70 = 560$

$2 \times 7 = 14$, hence $82 \times 7 = 560 + 14 = 574$

So $578 \div 7 = 82$ and the remainder is 4.
5.1 What is multiplication?

**Teaching guidelines**

It is important that learners have some awareness of the wide variety of situations to which multiplication is applicable. Understanding multiplication narrowly, namely as repeated addition only, is a serious misconception that may withhold learners from noticing when the solution of problems requires multiplication for which repeated addition is not helpful.

By way of introduction, you may alert learners to some of the wide variety of real situations in which multiplication is applicable, including Situations A, B and C on page 55 of the Learner Book. Explain the difference between Situations A and C.

In Situation A it makes sense to think of a number of cans each costing R8.

In Situation C it makes no sense to think of a number of pictures of houses.

Rather, Situation C is about a comparison between the size of a picture and the size of an actual house:

To interpret Situation C, one may also think of “stretching” the picture in all directions so that it attains the size of the actual house.

Situation A is a rate situation – the cans of juice sell at a fixed rate (price in this case).

Situation C is a ratio or scale factor situation.

5.1 What is multiplication?

We often know certain things about a situation, but then there may also be things that we do not know. Here are some examples.

A. You may know that one can of juice costs R8 and that you need 23 cans. You may not know what the total cost of 23 cans is.

B. You may know that there is 200 g of honey in a jar and that you will get only one eighth of it. You may not know how many grams of honey you will get. \( \frac{1}{8} \) of 200 is \( \frac{1}{8} \) of 100 which is . . .

C. You may know that this house is 50 times bigger than the picture shows, and that the picture of the house is 4 cm high. You may want to know how high the actual house is.

What you do to find the information you need in situations like the above, is called multiplication.

Multiplication can be done in different ways, for example by repeated addition, by repeated doubling and by breaking down numbers into parts of which you already know the answers.
Teaching guidelines (continued)

Situation B (the jar of honey) on the previous page is related to Situation A, but it extends the meaning of multiplication into the domain of fractions.

A sequence of questions like these may help learners to understand that Situation B is similar to Situation A:

1. How many grams of honey are there in 3 jars of 200 g each?
2. How many grams of honey are there in $2\frac{1}{2}$ jars?
3. How many grams of honey are there in 2 jars?
4. How many grams of honey are there in $1\frac{3}{8}$ jars?
5. How many grams of honey are there in $\frac{5}{4}$ jars?
6. How many grams of honey are there in $1\frac{1}{8}$ jars?
7. How many grams of honey are there in $1\frac{3}{8}$ jars?
8. How many grams of honey are there in $\frac{3}{4}$ of a jar?
9. How many grams of honey are there in $\frac{1}{2}$ of a jar?

Apart from enriching the meanings learners assign to multiplication, a sequence of questions like these may strengthen learners’ concept of fractions.

Note that Situation B can also be understood as a situation that requires division: $200 \div 8$.

While it is important that learners know that multiplication can be performed as repeated addition, as shown for $23 \times 8$ in the tinted passage on page 56 of the Learner Book, it is important that they can do it in quicker ways, as shown. Learners should also realise that multiplication by doubling is only easy if you are skilled at doubling, and that multiplication by building up from known parts is only easy if you know basic multiplication facts. Emphasise this and tell learners that over the next two lessons, when they will be doing Sections 5.2 and 5.3, they will strengthen their knowledge of multiplication facts, their skills at forming multiplication facts and their skills at doubling.

Answers

1. $8 \times 23 = 8 \times 20 + 8 \times 3 = 160 + 24 = 184$
2. (a) $6 \times 32 = 6 \times 30 + 6 \times 2 = 180 + 12 = 192$
   (b) Yes. $32 + 32 + 32 + 32 + 32 = 192$
Teaching guidelines

Demonstrate doubling and rounding off and compensating on the board with either the example $23 \times 8$ used in the tinted passages, or with another example (e.g. $42 \times 17$).

Answers

3. Yes. $28 + 28 = 56$, that is $2 \times 28$
   $56 + 56 = 112$, that is $4 \times 28$
   $112 + 112 = 224$, that is $8 \times 28$

4. $30 \times 8 = 240$, so $28 \times 8 = 240 - 2 \times 8 = 240 - 16 = 224$

5. (a) $32 \times 29$ by doubling:
   $32 + 32 = 64$, that is $2 \times 32$
   $64 + 64 = 128$, that is $4 \times 32$
   $128 + 128 = 256$, that is $8 \times 32$
   $256 + 256 = 512$, that is $16 \times 32$
   $29 = 16 + 8 + 4 + 1$
   So, $32 \times 29 = 32 \times 16 + 32 \times 8 + 32 \times 4 + 32 \times 1$
   $= 512 + 256 + 128 + 32$
   $= 928$

(b) $32 \times 29$ by rounding off and compensating:
   Example: Round both numbers off to 30: $30 \times 30 = 900$
   We still need $2 \times 29$ (double 29) = 58, but we took $1 \times 30$ too much.
   $32 \times 29 = 900 + 58 - 30 = 928$
   (There are many other ways with rounding off and compensating. Consider learners’ methods.)

(c) $32 \times 29$ by breaking down into known or easy parts:
   Example: $32 \times 29 = (30 + 2) \times (20 + 9)$
   $= (30 \times 20) + (30 \times 9) + (2 \times 20) + (2 \times 9)$
   $= 600 + 270 + 40 + 18$
   $= 928$
5.2 Multiplication facts

Teaching guidelines
A good way to start this lesson is to put some 1-digit multiplication questions to the whole class, stating the questions verbally and also writing the questions and the answers (when given) on the board, for example:

How much is …?

5 × 6
5 × 10
3 × 7
6 × 7
12 × 7 (Suggest doubling if learners hesitate.)
6 × 14

Draw learners’ attention to the fact that the answers for 6 × 7, 12 × 7 and 6 × 14 can all be obtained from 3 × 7 = 21, by doubling. Emphasise the idea that if you know one fact you can form other facts from it, for example by doubling.

Impress on learners that they need to know basic facts in order to be able to multiply with larger numbers.

Answers

1. (a) 150, 175, 200, 225, 250, 275
   (b) 90, 105, 120, 135, 150, 165
   (c) 48, 56, 64, 72, 80, 88
   (d) 54, 63, 72, 81, 90, 99
   (e) 42, 49, 56, 63, 70, 77

2. (a) 125 (b) 200 (c) 250 (d) 90
   (e) 56 (f) 54 (g) 63 (h) 72

3. (a) 3 × 6 (b) 3 × 10
   (c) 3 × 7 (d) 7 × 6
   (e) 70 × 6 (f) 7 × 4
   (g) 70 × 4 (h) 70 × 4

4. (a) 70 × 4 (b) 70 × 4
   (c) 3 × 15 (d) 5 × 12
   (e) 4 × 8 (f) 80 × 4
5.3 Double, double and double again

**Mathematical notes**

In order to use doubling effectively as a method of multiplication, it is important that learners learn to keep track of which multiples of the starting number are formed when the number is repeatedly doubled. For example, when 5 is repeatedly doubled, the following multiples of 5 are formed:

\[
\begin{align*}
1 \times 5 &= 5 \\
2 \times 5 &= 10 \\
4 \times 5 &= 20 \\
8 \times 5 &= 40 \\
16 \times 5 &= 80 \\
32 \times 5 &= 160 \\
64 \times 5 &= 320
\end{align*}
\]

When 7 is doubled, the following multiples of 7 are formed:

\[
\begin{align*}
1 \times 7 &= 7 \\
2 \times 7 &= 14 \\
4 \times 7 &= 28 \\
8 \times 7 &= 56 \\
16 \times 7 &= 112 \\
32 \times 7 &= 224 \\
64 \times 7 &= 448
\end{align*}
\]

You may do the above examples on the board to empower learners for questions 2 and 3 on the next page.

**Answers**

1. 400

5. (a) 2,920 (b) 3,220 (c) 3,340 (d) 3,340 (e) 3,358 (f) 3,358

6. (a) 2,010 (b) 2,280 (c) 2,490 (d) 2,490 (e) 2,546 (f) 2,546

7. (a) 2,160 (b) 1,920 (c) 2,280 (d) 2,280 (e) 2,304 (f) 2,304

8. (a) 2,240 (b) 2,150 (c) 2,390 (d) 2,390 (e) 2,408 (f) 2,408

5.3 Double, double and double again

You already know that to **double** a number means to add it to itself. For example, when you double 5, you get 10.

When you double 10, you get 20.

When you double 20, you get 40.

When you double 50, you get 100.

When you double 100, you get 200.

1. **What do you get when you double 200?**

When you double 50 you get 100 which is 50 + 50.

We can also say it is "two fifties" or 2 × 50.

When you double again you get 200 which is 50 + 50 and another 50 + 50.

So when you double 50 and double again, you get 200 which is 50 + 50 + 50 + 50.

We can also say this is "four fifties" or 4 × 50.

By doubling, we have found the multiplication fact 4 × 50 = 200.
Teaching guidelines
Suggest to learners that they produce extended answers for questions 2 and 3, as demonstrated in the notes on the previous page for doubling 5 and 7 repeatedly.

Answers
2. (a) 8 fifties
   (b) \(8 \times 50 = 400\)

3. (a) 240
   (b) \(2 \times 30; 4 \times 30; 8 \times 30\)
   (c) 480
   (d) \(2 \times 60; 4 \times 60; 8 \times 60\)

4. (a) By adding 3 repeatedly  21  24  27
   (b) By doubling repeatedly  48  96  192
   (c) By adding 25 repeatedly  175  200  225
   (d) By doubling repeatedly  400  800  1600
   (e) By doubling repeatedly  48  96  192
   (f) By doubling repeatedly  72  144  288
   (g) By adding 7 repeatedly  28  35  42
   (h) By doubling repeatedly  56  112  224
   (i) By doubling repeatedly  168  336  672
   (j) By adding 6 repeatedly  24  30  36

5. (a) By repeated addition of 90
   (b) 270
   (c) 540
   (d) 360

6. (a) By repeated doubling
   (b) 560
   (c) 280
   (d) 1120
5.4 Multiply by building up from known parts

Teaching guidelines
The break down and build up method of multiplication is based on the distributive property of multiplication and addition. You can use the diagram in question 2(b) to discuss the distributive property at the start of this section. Ask learners to think of a quick way to find out how many blue rings there are in the diagram, and how many red rings.

Take feedback and conclude the discussion by stating that since there are 7 groups of 40 red rings each, the number of red rings is $7 \times 40 = 280$, and the number of blue rings is $7 \times 8 = 56$. Write these two results on the board. Then ask learners if it is true that the total number of rings in the picture is $7 \times 48$. When this is agreed upon, ask learners whether the answer can be found by calculating $280 + 56$. Allow learners time to reflect on this, and discuss it in small groups.

Let learners then do questions 1 to 6, which will provide them with many opportunities to use the distributive property. The intimidating term “distributive property” need not and should preferably not be raised in class. Rather use an informal description such as “if you have to multiply two numbers by the same other number and find the total, you can first add the two numbers and then multiply”, with reference to a specific example like in question 2.

When learners have completed question 6, ask them to indicate which facts about smaller numbers they used to produce their answers.

Answers
1. (a) $4 \times 6 + 4 \times 9 = 4 \times (6 + 9)$, so $4 \times 15 = 24 + 36 = 60$
   (b) $4 \times 9 + 4 \times 15 = 4 \times (9 + 15)$, so $4 \times 24 = 36 + 60 = 96$
2. (a) 336
   (b) 336
3. 288
4. (a) $6 \times 79 = 474$
   (b) $87 \times 4 = 348$
   (c) $363 \times 6 = 2 178$
5. (a) $5 \times 30$ and $5 \times 6$
   (b) $30 \times 5$ and $6 \times 5$
6. (a) $34 \times 50 = 1 700$
   (b) $34 \times 8 = 272$
   (c) $34 \times 50 + 34 \times 8 = 1 972$
   (d) $34 \times 58 = 1 972$
Teaching guidelines

Questions 7 and 8 are intended to impress on learners that they need to have good knowledge of basic multiplication facts (“tables”) in order to be able to multiply fluently with larger numbers. Tell them that in Section 5.5 they will strengthen their knowledge of basic multiplication facts.

The second tinted passage is about alternative methods of multiplication. Do the example on the board and let learners then engage with question 9.

Answers

7. 50 \times 40 and 3 \times 40 and 50 \times 7 and 3 \times 7

8. (a) 50 \times 60 and 7 \times 60 and 50 \times 8 and 7 \times 8   \quad 57 \times 68 = 3 876
(b) 90 \times 40 and 4 \times 40 and 90 \times 9 and 4 \times 9   \quad 94 \times 49 = 4 606
(c) 60 \times 60 and 8 \times 60 and 60 \times 8 and 8 \times 8   \quad 68 \times 68 = 4 624
(d) 70 \times 10 and 3 \times 10 and 70 \times 9 and 3 \times 9   \quad 73 \times 19 = 1 387
(e) 80 \times 80 and 7 \times 80 and 80 \times 8 and 7 \times 8   \quad 87 \times 88 = 7 656
(f) 30 \times 90 and 4 \times 90 and 30 \times 8 and 4 \times 8   \quad 34 \times 98 = 3 332
(g) 50 \times 50 and 7 \times 50 and 50 \times 2 and 7 \times 2   \quad 57 \times 52 = 2 964
(h) 60 \times 80 and 3 \times 80 and 60 \times 5 and 3 \times 5   \quad 63 \times 85 = 5 355

9. 73 \times 19 = 73 \times 20 \ (i.e. \ double 73 \ multiplied \ by \ 10) \ - \ 73 \ (i.e. \ one \ 73 \ less) = 1 387
\quad 34 \times 98 = 34 \times 100 - 2 \times 34 \ (two \ 34s \ less) = 3 332
\quad 57 \times 100 = 5 700, \ \ and \ half \ of \ that \ is \ 2 850
\quad \text{so,} \quad 57 \times 52 = 57 \times 50 + 57 \times 2 \ (\text{double} \ 57)
\quad \quad = 2 850 + 114
\quad \quad = 2 964

5.5 Strengthen your knowledge of multiplication facts

Teaching guidelines

This section provides learners with opportunities to strengthen their knowledge of basic multiplication facts. Please see “Notes on questions” on the next page.

Answers

1. (a) 24   (b) 35   (c) 36   (d) 35   (e) 360
(f) 350   (g) 14   (h) 1 400   (i) 21   (j) 42
(k) 18   (l) 36   (m) 72   (n) 3 600   (o) 1 200
(p) 1 800   (q) 2 400   (r) 3 000

7. Which facts do you need to know to find out how much 53 \times 40 + 53 \times 7 and 53 \times 47 are?

To find out how much 46 \times 73 is by using the breaking down and building up method, you need to know how much 46 \times 70 is and how much 46 \times 3 is. To know that, you need to know how much 40 \times 70, 6 \times 70, 40 \times 3 and 6 \times 3 are.

8. In each case state which facts you need to know so that you can easily find the answer by using the breaking down and building up method. If you know the facts that are needed, give the answer too.
(a) 57 \times 68   (b) 94 \times 49   (c) 68 \times 68   (d) 73 \times 19
(e) 87 \times 88   (f) 34 \times 98   (g) 57 \times 52   (h) 63 \times 85

Note that 94 \times 49 can be calculated as follows:
94 \times 100 = 9 400, \ \ and \ \ half \ of \ that \ is \ 4 700,
so 94 \times 50 = 4 700.
94 \times 49 is 94 less than 94 \times 50,
so 94 \times 49 = 4 700 – 94 = 4 606.

9. Show how 73 \times 19, 34 \times 98 and 57 \times 52 can be calculated in similar ways.

62 UNIT 5: WHOLE NUMBERS: MULTIPLICATION AND DIVISION
Notes on questions

Questions 1, 3, 4(b), 5 and 6 provide learners with opportunities to assess their own knowledge of multiplication facts, and specifically to identify products for which they do not know the answers straightaway or cannot find the answers quickly. Questions 2 and 4(c) guide learners towards repeated counting as a way to establish multiplication facts that they do not know as yet.

Answers

2. (a) 30, 36, 42, 48, 54, 60  
   (b) 300, 360, 420, 480, 540, 600  
   (c) 3 000, 3 600, 4 200, 4 800, 5 400, 6 000

3. to 5. These questions can be done in table format under your guidance.

6.  
   $70 \times 90 = 6 300$  $60 \times 90 = 5 400$  $70 \times 80 = 5 600$  $60 \times 70 = 4 200$  
   $80 \times 90 = 7 200$  $40 \times 70 = 2 800$  $80 \times 80 = 6 400$  $90 \times 90 = 8 100$

2. Write the next six numbers in each sequence. While you do this you may find the answers for some parts of question 1. Fill those answers in when you find them.
   (a) 6  12  18  24  ...  
   (b) 60  120  180  240  ...  
   (c) 600  1 200  1 800  2 400  ...

3. Copy and complete this table of multiplication facts. In cases where you do not know the answer, you may look at the sequences that you wrote in question 2, or use any other method.

<table>
<thead>
<tr>
<th>3 × 6</th>
<th>30 × 6</th>
<th>3 × 60</th>
<th>30 × 60</th>
</tr>
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<tbody>
<tr>
<td>6 × 6</td>
<td>7 × 6</td>
<td>70 × 6</td>
<td>70 × 60</td>
</tr>
<tr>
<td>8 × 6</td>
<td>9 × 6</td>
<td>90 × 6</td>
<td>90 × 60</td>
</tr>
<tr>
<td>5 × 6</td>
<td>2 × 6</td>
<td>20 × 6</td>
<td>20 × 60</td>
</tr>
<tr>
<td>9 × 6</td>
<td>8 × 6</td>
<td>80 × 6</td>
<td>80 × 60</td>
</tr>
<tr>
<td>4 × 6</td>
<td>1 × 6</td>
<td>10 × 6</td>
<td>10 × 60</td>
</tr>
</tbody>
</table>

4. (a) Make a similar table for the multiplication facts for 7 and 70, but do not fill in any answers yet.
   (b) Now fill in the answers that you know immediately.
   (c) Try to find more answers. If you need to, you may also write sequences for 7, 70 and 700, like the sequences in question 2.

5. Do what you have done for 7 and 70 in question 4, for each of the following.
   (a) 8 and 80  
   (b) 9 and 90

6. For which of the following can you give the answers straight away?

<table>
<thead>
<tr>
<th>70 × 90</th>
<th>60 × 90</th>
<th>70 × 80</th>
<th>60 × 70</th>
</tr>
</thead>
<tbody>
<tr>
<td>80 × 90</td>
<td>40 × 70</td>
<td>80 × 80</td>
<td>90 × 90</td>
</tr>
</tbody>
</table>
5.6 Practise multiplication and solve problems

Teaching guidelines

You may do some examples on the board at the start, for example:

\[
56 \times 38 = 50 \times 38 + 6 \times 38 = 50 \times 30 + 50 \times 8 + 6 \times 30 + 6 \times 8 = 1500 + 400 + 180 + 48 = 2128
\]

Emphasise the strategy to break the multiplication down into smaller parts for which the answers can be found easily.

Learners who do not read questions thoroughly will easily make mistakes in question 4. For example, some learners may simply add R22 and R34 and produce the false answer R56. Suggest to learners that for questions in which more than two numbers occur, they write a calculation plan before doing any calculations, and then reconsider the calculation critically by checking whether it corresponds to the given situation. A correct calculation plan for question 4 is \(36 \times 22 + 48 \times 34\).

\[
12 \times 36 - 338 \text{ is a correct calculation plan for question 5.}
\]

Both of \(55 \times 43 - 346 - 129\) and \(55 \times 43 - (346 + 129)\) are correct calculation plans for question 7.

Once learners have done question 5, you may use it to explain the concept “capacity”, which is important in the work on volume and capacity that learners will do later in the year. In the situation in question 5, the capacity of the train is \(12 \times 36 = 432\) seated passengers.

Question 6 looks complicated, but there is a short way of doing it. The long route is to calculate the total cost of 43 ℓ in January \((43 \times R59 = R2357)\), use this to calculate the total cost in February \((R2357 + R86 = R2443)\), and use this to calculate the new selling price \((R2443 \div 43 = R61)\). The short route is to argue that R86 more for 43 ℓ is R2 more for 1 ℓ, since \(2 \times 43 = 86\).

Answers

1. (a) 3219 (b) 1073 (c) 2496 (d) 2146 (e) 1248 (f) 2496 (g) 1944 (h) 1944 (i) 1183 (j) 2964 (k) 2964 (l) 3116

2. (a) 2496 trees (b) 1248 trees

3. (a) 1944 apples (b) 1656 apples

4. R2424 5. 94 empty seats

5. R61 per litre 7. R1890
Teaching guidelines
Although learners may not recognise and do it as such, question 9(b) is a grouping situation. It can be calculated as 100 ÷ 26, which has the answer 3 remainder 22. This means that with 3 rows only, 22 learners still need chairs. Hence the answer to the real question is 4 rows of chairs.

Question 10 involves ratio. Learners who quickly recognise the relationship between 18 and 72, i.e. that $72 = 18 \times 4$, may find the answer as follows:

- If she sells 18 pancakes, she sells 42 muffins.
- If she sells another 18 pancakes, she sells another 42 muffins.
- If she sells another 18 pancakes, she sells another 42 muffins.
- If she sells another 18 pancakes, she sells another 42 muffins.
- So if she sells $18 + 18 + 18 + 18 = 72$ pancakes, she sells $42 + 42 + 42 + 42 = 168$ muffins.

If learners do not make progress with question 10, you may ask them how many muffins they think Mrs Baker would sell if she sells 36 pancakes. This may put them on a path towards the solution.

Answers
8. (a) 1 494 cm  (b) 6 cm
9. (a) 1 248 cm  (b) 4 rows
10. 168 muffins

5.7 Multiples, factors and products

Teaching guidelines
Preferably use a different example than the one in the tinted passage to introduce the terms “factor”, “product” and “multiple”, for example $5 \times 9 = 45$.

The term “product” is used in two ways. The calculation plan $5 \times 9$ is called the product of 5 and 9, and the number 45 is also called the product of 5 and 9.

Answers
1. Any three, e.g. $2 \times 18; 3 \times 12; 4 \times 9; 6 \times 6$
2. Example: 18, 30, 36, 54, 66 (and many more; consider all answers)
Answers

3. (a) 1 × 24  2 × 12  3 × 8  4 × 6
   (b) 1 × 36  2 × 18  3 × 6  4 × 9  6 × 6
   (c) 1 × 60  2 × 30  3 × 20  4 × 15  5 × 12  6 × 10
   (d) 1 × 72  2 × 36  3 × 24  4 × 18  6 × 12  8 × 9
   (e) 1 × 100  2 × 50  4 × 25  5 × 20  10 × 10
   (f) 1 × 120  2 × 60  3 × 40  4 × 30  5 × 24
   6 × 20  8 × 15  10 × 12
   (g) 1 × 180  2 × 90  3 × 60  4 × 45  5 × 36
   6 × 30  9 × 20  10 × 18  12 × 15
   (h) 1 × 240  2 × 120  3 × 80  4 × 60  5 × 48
   6 × 40  8 × 30  10 × 24  12 × 20  15 × 16

4. Examples: 80, 120, 160, 200, 240, 280, 320, 360, 400, 800, ...

5. (a) 7  (b) 12

6. (a) 40 × 10  (b) 40 × 11  (c) 40 × 12
   (d) 40 × 13  (e) 40 × 16  (f) 40 × 18

7. (a) 30 × 20  (b) 30 × 23  (c) 30 × 24  (d) 30 × 28

8. (a) 468  (b) 472

Teaching guidelines

There is some danger that the focus on multiples and factors may lead learners to think that numbers can only be expressed as products, for example 472 = 8 × 59. Yet it is important that learners realise that numbers can also be expressed in the form product + remainder, for example 472 = 6 × 78 + 4. This is a formal way to express the answer for 472 ÷ 78.

You may explain the content of the tinted passage without reference to division at this stage.

Answers

9. Learners’ answers will vary. Consider all answers.
   Example: 8 × 109 = 872 and 872 + 1 = 873; so, 873 = 8 × 109 + 1
   7 × 124 = 868 and 868 + 5 = 873; so, 873 = 7 × 124 + 5
5.8 Division

Teaching guidelines

It is important that learners distinguish between grouping and sharing in situations where a quantity is divided into equal parts. Use questions A and B as a vehicle to let learners experience the difference between grouping and sharing, i.e. between finding the number of equal parts and finding the size of the equal parts.

Put questions A and B in the tinted passage to learners, ask them to estimate the answers and to write the estimates down. Let them then check their estimates. You may have to demonstrate how they can check by multiplying in each case. There is no need to mention “division” at this stage: Learners should focus on the real situations A and B to develop an understanding of the difference between sharing and grouping. Talking about division now may turn their minds away from the situations and make them think in terms of the given numbers only.

Let learners work for about 5 minutes, trying to find the accurate answers; then do questions A and B on the board. Use one side of the board for working on question A and the other side of the board for working on question B. In question A you have to find out how many pieces of 4 cm will make up 824 cm. You can build the number up in parts: 100 pieces of 4 cm each gives 400 cm of tape. Another 100 pieces brings you to 800 cm of tape. You can then add pieces one by one. (These actions are very similar to the steps in formal “long division”.) You may set the work out as follows:

**Question A**

100 pieces of 4 cm = 400 cm
100 pieces of 4 cm = 400 cm
5 pieces of 4 cm = 20 cm
1 piece of 4 cm = 4 cm
So, 206 pieces of 4 cm = 824 cm

At this stage there is no need to set the work out more formally. The primary focus should be on learners thinking in terms of the real situations.

**Answers**

1. 42 classrooms

2. R60
Mathematical notes
Remainders have to be dealt with in different ways in different contexts.

In the situation described in question 3, the answer for $925 \div 4$ is 231 remainder 1. Yet the proper answer to the question is 231 pieces; the 1 cm left over (the remainder) is only a quarter of a 4 cm piece.

In the situation described in question 8(a), the answer for $194 \div 8$ is 24 remainder 2. However, this cannot be the answer to the question how many buses are needed. The number of buses needed is 25.

Notes on questions
Questions 3, 8(a) and (b), 9(a), (b) and (c) and 10 are grouping problems.
Questions 4 and 6(a) are sharing problems.
Question 7 is a two-step problem: the cost of one loaf must be calculated first (grouping).

Teaching guidelines
Questions 6 and 7 are similar. Question 7 is more demanding in the sense that learners have to decide by themselves to first calculate the cost of one loaf. Allow them the opportunity to struggle with question 7 and to devise the plan of first calculating the cost of one loaf themselves.

Answers
3. 231 pieces
4. 90 balls
5. (a) 141  (b) 113  (c) 113  (d) 86  (e) 125  (f) 81
6. (a) R9  (b) R342
7. R344
8. (a) 25 minibuses  (b) 59 minibuses
9. (a) 78 boxes (3 muffins left over)  (b) 52 boxes (3 muffins left over)  (c) 63 boxes  (d) R3
10. 14 days

3. How many pieces of 4 cm each can be cut from a roll of wire that is 925 cm long?
4. 720 netball balls are packed in 8 large crates. All the crates have the same number of balls. How many balls are there in each crate?
5. Calculate.
   (a) $846 \div 6$  (b) $904 \div 8$  (c) $452 \div 4$
   (d) $774 \div 9$  (e) $625 \div 5$  (f) $729 \div 9$
6. Fourteen cans of cooldrink costs R126.
   (a) How much does one can cost?
   (b) How much do 38 cans cost altogether?
7. Sixteen loaves of bread cost R128. How much do 43 loaves cost?
8. (a) How many minibuses are needed to transport 194 learners on an outing if each minibus can only seat 8 learners?
   (b) How many minibuses are needed to transport 466 learners if each minibus can only seat 8 learners?
9. (a) Magda packs 315 muffins into boxes of 4 muffins each. How many boxes does she need?
   (b) How many boxes will she need if she packs 6 muffins in each box?
   (c) How many boxes will she need if she packs 5 muffins in each box?
   (d) If Magda sells all 315 muffins for R945 in total, how much does she get for each muffin?
10. The Natural Sciences teacher has to mark 126 projects. If she marks 9 projects per day, how long will it take her to finish marking the projects?
### Learner Book Overview

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### CAPS time allocation
6 hours

### CAPS page references
27 and 144

**Mathematical background**

Learners deal with time and time-related issues every day. Many Grade 5 learners can read clocks and watches, but just as many learners find them difficult to read. There are three issues that make the concept of time difficult:

- **Firstly**, time cannot be seen, touched or physically experienced like length, capacity/volume, area and mass. We measure time by looking at environmental changes or changes in the position of the hands of a clock or the numbers on a clock face.
- **Secondly**, unlike the number system and other forms of measurement, the numbers do not get bigger forever. We measure time in modular units: when we reach certain numbers (e.g. 60 seconds, 60 minutes, 24 hours, 365 days) the numbers wrap around and go back to the beginning. This is different to the way primary school learners work with numbers in other aspects of Mathematics.
- **Thirdly**, in all other topics in primary school Mathematics, numbers are organised in groups and powers of ten, but in the topic of time, numbers are organised in groups of 60, 24, 7, 12 and 365.

The topic of time involves more than just reading clocks. There are in fact three aspects of time that need to be developed:

- the duration of time
- the passing and sequencing of time
- identifying a point in time by, for example, reading a clock.

**Note**: Sections 6.1, 6.2, 6.5 and 6.6 are much shorter than the middle sections (6.3 and 6.4). You may want to consider combining Sections 6.1 and 6.2 into one lesson (i.e. aim to cover both in 1 hour). This will leave you more time for the two middle sections. Sections 6.5 and 6.6 can also be done together.

**Resources**

Analogue and digital clocks for demonstration purposes; stopwatches – see Section 6.4; calendars of the current year
6.1 A little history

**Teaching guidelines**
You can use the information on page 69 of the Learner Book as the basis for a discussion on how people told the time and kept track of time before there were clocks and watches.

You can start by asking learners how they can tell the time of year without a calendar and the time of day without a clock, watch (or cell phone). Learners would have made a water clock in Grade 4.

As suggested on the previous page, you might like to cover both Sections 6.1 and 6.2 in one lesson, i.e. in 1 hour.
6.2 Daytime hours and night-time hours

Mathematical notes
In the Intermediate Phase, learners work with both 12-hour time (using a.m. and p.m.) and 24-hour time. This section focuses on 12-hour time; in the next section learners will work with 24-hour time.

Teaching guidelines
You might like to cover both Sections 6.1 and 6.2 in one lesson (see the note on the first page of this Teacher Guide unit).

Learners could answer questions 1, 3 and 5 in class, and do questions 2 and 4 for additional practice (e.g. as homework).

Possible misconceptions
Learners may not be sure how to write midday and midnight in 12-hour time. You may need to clarify for them that midday is called 12 p.m. and midnight is called 12 a.m. (see the table on page 72 of the Learner Book). This is simply a rule that has been adopted so that everyone uses the same notation (way of writing).

p.m. means after midday (from Latin “post meridiem”; “post” means after and “meridiem” means midday). a.m. means before midday (from Latin “ante meridiem”; “ante” means before).

Answers
1. 12 hours
2. 12 hours
3. 4:30 p.m.
4. 7:30 a.m.
5. 8 hours
6.3 Read, tell and write time

Teaching guidelines
You can check whether learners remember how many minutes there are in an hour, and whether they know how many seconds there are in a minute.

This section is quite long, so you might consider splitting the questions between classwork and homework (or work for additional practice in class whenever there is time). One option is to use

- question 1, the first two rows of question 3, and questions 4, 7, 8 and 9 as classwork, and
- question 2, the last two rows of question 3, and questions 5, 6, 10 and 11 as homework.

Possible misconceptions
Learners may find it difficult to understand why midnight is written as 00:00 in 24-hour time. You can show them what happens on the display of a digital clock, for example between 5 to 12 and 5 past 12. Also refer them to the tinted passage on pages 71 to 72.

Notes on questions
Learners could do question 2 in pairs or in small groups (maximum of three learners). Ask different pairs or groups to explain how they completed the table. Ways include: doubling and halving; addition or repeated addition; multiplication and division; counting in multiples of 15 (1/4 hour = 15 minutes) and 900 (1/4 hour = 900 seconds).

Answers
1. (a) 1 hour = 60 minutes = 3 600 seconds  (b) 1/2 hour = 30 minutes = 1 800 seconds
   (c) 1/4 hour = 15 minutes = 900 seconds  (d) 3/4 hour = 45 minutes = 2 700 seconds

<table>
<thead>
<tr>
<th>Hours</th>
<th>1/2</th>
<th>3/4</th>
<th>1 1/2</th>
<th>2</th>
<th>2 1/4</th>
<th>2 1/2</th>
<th>3</th>
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<td>120</td>
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<td>180</td>
</tr>
<tr>
<td>Seconds</td>
<td>1 800</td>
<td>2 700</td>
<td>5 400</td>
<td>7 200</td>
<td>8 100</td>
<td>9 000</td>
<td>10 800</td>
</tr>
</tbody>
</table>

Here is an example of how learners might explain their calculations:
For the first answer, we said that 1 hour is 60 minutes, so 1/2 hour is 30 minutes. But an hour is also equal to 3 600 seconds, so 1/2 an hour is 3 600 divided by 2, which is 1 800 seconds.

These two clocks show the same time: 30 minutes and 10 seconds past three in the morning.

The analogue clock on the left measures 12-hour time around a circle.
The digital clock on the right measures 24-hour time in numbers.
Which clock do you find easier to read?

People catching aeroplanes may get confused between 8 a.m. and 8 p.m., so flight carriers use the 24-hour time notation. 8 p.m. is 20:00.

The hours from midnight through to the next midnight start at zero. In 24-hour time notation, one minute after midnight is written as 00:01.
Answers

3. | 12-hour time | 24-hour time | 12-hour time | 24-hour time |
   |             |             |             |             |
   | 5 a.m.      | 05:00       | 2:00 p.m.   | 14:00       |
   | 7:30 a.m.   | 07:30       | 3:12 p.m.   | 15:12       |
   | 9:15 a.m.   | 09:15       | 5:32 p.m.   | 17:32       |
   | 11:35 a.m.  | 11:35       | 11:45 p.m.  | 23:45       |

4. (a) D  (b) C  (c) A  (d) B

Teaching guidelines

Do some language work with learners before you begin the next lesson. You can explain to them that the word “night” (which they know already) is used for all the hours between sunset and sunrise. But English also uses the word “evening” for the first part of the night – “evening” means the time between sundown and midnight.

English also uses the word “afternoon” for the last part of the day, between midday (noon) and sunset.

Note about resources and practical work

For Grade 5, the Curriculum and Assessment Policy Statement (CAPS)* states the following: “Learners continue to read, record and calculate time in 12-hour and 24-hour formats and to work with analogue and digital instruments. This is practised regularly. Once learners have been taught to tell the time, it can be practised during the Mental Mathematics section of the lesson, and frequently at other times during the day.”

Notes on questions
To save classroom time, you can photocopy the clock faces provided in the Addendum on pages 417 and 418 for use with questions 6 and 8.

Answers
5. (a) 02:00 (b) 22:15 (c) 11:30 (d) 23:45
   (e) 04:00:30 (f) 21:00:15 (g) 19:39:50
6. (a) (b) (c) (d) (e) (f) (g) (d)
7. (a) 25 seconds past 9 in the morning
   (b) 15 minutes and 30 seconds past 8 in the morning
   (c) 5 seconds past 9 at night/in the evening
   (d) 15 minutes and 25 seconds past 12 in the afternoon
   (e) 50 minutes and 50 seconds past 11 at night or 9 minutes and 10 seconds before midnight
   (f) 12 minutes and 40 seconds past midnight
   (g) 54 minutes and 1 second past 7 in the evening or 5 minutes and 59 seconds before 8 at night/in the evening
   (h) 15 seconds past 3 in the afternoon
8. (a) (b) (c) (d) (e) (f) (g) (h)
9. 2 hours 10 minutes
10. 06:45
11. 16:40
6.4 Intervals of time

Teaching guidelines

Learners can either use stopwatches that occur as single instruments, or stopwatches on cell phones or wrist watches.

Digital stopwatches are usually easier to read than analogue stopwatches. Many cell phones have a stopwatch function, or the possibility of downloading a free stopwatch app. While learners are busy with classwork, you could work with small groups of learners to show them how a stopwatch works, and let them practise using it to measure intervals of time, for example timing the activities in questions 3(a), (b) and (c).

Answers

1. (a) I visited him for a period of 20 minutes.
(b) during some other activity: I shall walk and talk at the same time.
(c) throughout the time that school is taking place
(d) starts = begins; ends = stops or finishes
(e) lasted 4 hours = came to an end after 4 hours
(f) Something happened between 10 o'clock and 11 o'clock: It could have been something quick, e.g. a tree fell down, or it could have been something that went on for an hour, for example a thunderstorm.
(g) I used up an hour.
(h) What is the period of time?

2. Answers will differ. Examples are:
long: How long will you be away?
between: The exam takes place between 09:00 and 12:00.
lasted: The party lasted 5 hours.
while: I ate my apple while I waited for the taxi.
during: We eat our sandwiches during break.

3. Learners’ estimates will differ.

4. (c), (b), (a), (d), (e), (f)

5. 5 days. There are 24 hours in a day. 5 days = 120 hours

6. 87 months. There are 12 months in a year. 7 years = 84 months

7. $2 \frac{1}{2}$ minutes. There are 60 seconds in a minute. $2 \frac{1}{2}$ minutes = 150 seconds
8. (a) Morning. It was before midday. The clock showed 08:35; in the evening it would have shown 20:35.
(b) Twenty-five minutes to nine in the morning; 8:35 a.m.
(c) 205 minutes
(d) 15 minutes
(e) Card 2: 16 minutes Card 3: 18 minutes
   Card 4: 14 minutes Card 5: 17 minutes
(f) It takes her between 14 to 18 minutes to make one card; the time varies by four minutes. Average time per card is about 16 minutes.
(g) 80 minutes or 1 hour and 20 minutes
(h) 125 minutes or 2 hours and 5 minutes
(i) 10:20
(j) Approximately 48 to 50 minutes. Yes, she will finish before her sister returns.
Answers
9.  (a) 5 minutes 22 seconds
    (b) 3 minutes 13 seconds
    (c) 19 seconds
    (d) 12 minutes $1\frac{1}{2}$ seconds
Answers

10. Learners’ answers will vary.

These days we usually use digital stopwatches. Most cell phones have a digital stopwatch. A digital stopwatch is even more accurate than an analogue stopwatch. It accurately counts hundredths of a second, which are also called centiseconds.

10. You need to practise to use a stopwatch accurately.

(a) Measure the lengths of time for activities such as those in question 3 as accurately as possible. (Note: some of the activities in question 3 may take too long to measure with a stopwatch.)

(b) Compare your estimates to the measured time intervals. Work out how far your estimates were out.

11. In 2014, Bongumusa Mthembu from KwaZulu-Natal won the Comrades Marathon (about 90 km) in 5 hours 28 minutes and 34 seconds (05:28:34). Ludwick Mamabolo came second in a time of 5 hours 33 minutes and 14 seconds (05:33:14).

The times of the five fastest runners are recorded in the table below.

<table>
<thead>
<tr>
<th>Runner</th>
<th>Country</th>
<th>Measured time</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Bongumusa Mthembu</td>
<td>KZN, SA</td>
<td>5h 28min 34s</td>
</tr>
<tr>
<td>2. Ludwick Mamabolo</td>
<td>Gauteng, SA</td>
<td>5h 33min 14s</td>
</tr>
<tr>
<td>3. Gift Kelebe</td>
<td>Limpopo, SA</td>
<td>5h 34min 39s</td>
</tr>
<tr>
<td>4. Stephen Msheki</td>
<td>Zimbabwe</td>
<td>5h 35min 18s</td>
</tr>
<tr>
<td>5. Rufus Photo</td>
<td>Limpopo, SA</td>
<td>5h 35min 30s</td>
</tr>
</tbody>
</table>
**Answers**

11. (a) 11:28:34  
(b) 12 seconds  
(c) 1 minute 25 seconds  
(d) 4 minutes 40 seconds

---

**6.5 Calendar time**

**Teaching guidelines**

This section and Section 6.6 are much shorter than the middle sections (6.3 and 6.4). You might like to cover Sections 6.5 and 6.6 in 1 hour.

First assess how much learners know about how a year is put together – how many days there are in a year, in different months, and in a week, as well as how many months there are in a year. You can use the tinted passage on page 78 to fill in any gaps. You might need to check that learners know the difference between leap years and other years.

You could let learners complete question 1 in class and use question 2 for additional practice (e.g. as homework).

**Answers**

1. (a) to (d) Learners’ answers will differ.
   (e) Learners can count on their knuckles, starting with January on a knuckle, February off a knuckle, March on a knuckle, etc. All the months on knuckles have 31 days, as long as you count both July and August on knuckles.
   Learners can also recite rhymes such as:
   *Thirty days has September,*  
   *April, June and November,*  
   *all the rest have thirty-one*  
   *except for February,*  
   *which has twenty-eight*  
   *– rain or shine –*  
   *but in leap years, twenty-nine.*
   Accept any other correct ways that learners may suggest.
   (f) Depends on the year.
   (g) Depends on the year. No.
### Answers

2. (a) 31 days  
(b) 4 full weeks  
(c) Yes. February has 29 days.  
(d) Thursday  
(e) 81 days  
(f) 56 days  
(g) 19 July; Tuesday (Note: 9 August is Women’s Day, hence it is not a school day.)  
(h) Freedom Day; South Africa’s first fully democratic election  
(i) 99 days  
(j) 18 August
6.6 Years and decades

Teaching guidelines
Work through the tinted passage and the “timeline” with the class. You could also draw a timeline on the board, and ask learners to suggest events/information that you can add to it, for example:

![Timeline diagram]

You could then also add the information that the learners bring to class – see question 5.

Answers
1. The answer depends on what today’s date is.
2. Learners’ answers are determined by their current age. They have to add 10 years to it.
3. Learners’ answers will differ, because it depends on how old they are now.
4. Learners’ answers will differ.
5. Learners’ answers will differ.
Grade 5 Term 1 Unit 7  
Data handling

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>7.1 Asking questions about a situation</td>
<td>Asking questions that can be answered by collecting and analysing data</td>
<td>81 to 82</td>
</tr>
<tr>
<td>7.2 Drawing and interpreting graphs</td>
<td>Drawing and interpreting bar graphs, interpreting pie charts, and interpreting and drawing pictographs</td>
<td>83 to 86</td>
</tr>
<tr>
<td>7.3 Summarising and analysing data</td>
<td>Working with a data table, identifying the mode, drawing conclusions and making predictions</td>
<td>86 to 89</td>
</tr>
<tr>
<td>7.4 Project</td>
<td>Gathering data about waste at school</td>
<td>90</td>
</tr>
</tbody>
</table>

**CAPS time allocation**  
10 hours

**CAPS page references**  
30 to 31 and 145 to 146

In this unit we help learners to become familiar with the context of recycling from a data point of view. The unit provides opportunities to work on every step of the data-handling cycle, namely asking questions, gathering data, representing data, analysing and summarising data, and interpreting and reporting data about recycling. The topic lends itself to integration with Natural Sciences. If possible, you could get the latest information about waste recycling in South Africa and adapt the answers. This would enhance the relevance of the topic.

**Mathematical background**

Data are bits of information about a particular context. We ask questions about a situation or context that lead to the collection of information. The way in which the data are organised and represented, and the further questions that we ask, allow us to see trends in the data. In data handling we usually work with large amounts of information related to particular contexts. Instead of focusing on each bit of information separately, the way we organise, represent and analyse the data gives us ways of talking in general about the data. We look at the data in a global way and draw out trends or characteristics that describe the data.

Data handling differs from other parts of Mathematics in three respects:

- **The answer to data questions is in the information from lots of data gathered.**
  Data handling is necessary where measurements and frequencies vary, and therefore one measurement cannot provide accurate information about a situation. Lots of different data can be confusing, so we organise the data that we collect in different ways to get a “picture” of the situation.

- **The numbers we use in data handling always have some description of a category they belong to, or some unit of measurement.**
  In Mathematics, learners work mostly with abstract numbers. In data handling the numbers must be interpreted in a context. The same number 245 can be 245 kg or 245 people, depending on the question.

- **Data questions are always answered with a story about the context.**
  Data handling starts when we need to answer a question about a situation where the property we look at varies. The numerical answers we get by data handling must be interpreted to answer the question about the situation.
7.1 Asking questions about a situation

Teaching guidelines

You may introduce the work in this unit by explaining the meaning of the word “data”: Say we want to answer questions such as “How many learners in our school don’t like to read storybooks?”, “Why don’t they like to read storybooks?”, “If they were told by their teacher to read at least one storybook this term, what type of storybook would they choose?”, etc. The facts, information or opinions that we collect and use as a basis to analyse and discuss a problem or to suggest answers or solutions, are called data.

Discuss the benefits of recycling with learners, especially from an environmental point of view. Also discuss possible recyclable material in the school environment.

Some of the questions in this section are designed to help learners clarify their own thoughts and questions about recycling. Writing down their own questions about recycling can help to stimulate learners’ interest in the topic. Their questions will also help you to better understand learners’ prior knowledge about recycling.

You might like to ask learners to discuss the answers to questions 1 and 2 in pairs but to record their work individually. It is important that you let learners share their answers and have class discussions so that everyone can learn from each other. You might like to let learners share their answers to questions 1 and 2 before working through question 3 on page 82. The ideas generated here will help with the project in the final section.

Answers

1. Here are some possible questions: I wonder how much glass (or paper or plastic) is recycled every month in the town where I live? I wonder how much recyclable waste ends up in our town’s landfill(s)? I wonder how much waste we can recycle at home and what kinds of waste? I wonder how much glass (or paper or plastic) a waste collector collects every day? I wonder how many people sort their waste? I wonder why some people recycle and others don’t? I wonder how much we can earn by recycling glass (or paper or plastic)? I wonder what is the most popular material to collect for recycling?

2. (a) Waste is anything that someone does not need anymore. Things become waste when they are not needed any more, for example when we have used the milk in a container or food in a tin, the container or tin becomes waste.

(b) Learners think about the route to the landfill of waste that is collected. If we run out of landfill space, we will pollute land and rivers with excess waste, affecting our drinking water and the quality of the food we eat. Birds, animals and indigenous plants will be affected.

(c) Learners’ answers will vary. If we know how much and what types of waste we create, then we can plan to create less waste, and to recycle waste more efficiently. Municipalities can use the information to plan how much landfill space they will need. Waste buy-back centres can use the information for planning.

Since 2011, the Department of Environmental Affairs has been gathering information from municipalities about how they manage the waste that people create. All this information becomes data about waste management and recycling.

2. (a) Write down what you think “waste” is. How do things become waste?

(b) Where does the waste end up where you are living? What do you think will happen if South Africa’s towns and cities run out of landfill space?

(c) Do you think data about waste in your town or village can be used to plan better? Explain why you say so.

The table on the next page gives information about the waste that was produced by people living in the different provinces of South Africa in 2011. Municipal waste is the waste of households, restaurants and shops, but not the waste of factories or mines.
Possible misconceptions
The idea of “average waste per person” will be new for most learners. They may think that every person actually wastes the amount given. No one knows exactly how much waste was produced by any individual in different provinces; they only know the total waste produced and the number of people living in the province. The kilogram amounts given in the table are amounts calculated by dividing the total waste in any of the provinces by the total number of people in that specific province. For instance, the 113 kg of the Eastern Cape province indicates that people in the Eastern Cape produce on average 113 kg; some people will produce a lot more waste and others will produce less waste.

Mathematical notes
Part of data handling is using facts such as the numbers generated – for example the answers to questions 3(a) and (b) – as the basis for making an opinion, drawing conclusions or asking further questions. In general, the facts are used for further reasoning, as in question 3(c).

Teaching guidelines
Allow learners to share their answers to question 3(c), so that they can learn from each other.

Answers
3. (a) Western Cape, Northern Cape, Gauteng and Mpumalanga
   (b) North West, Limpopo, Free State, Eastern Cape and KwaZulu-Natal
   (c) Learners’ answers will vary; accept all reasonable answers. Some examples of answers are provided:
   Provinces with many big cities, which have many shops and restaurants, may generate more waste per person than provinces that are more rural. (Northern Cape is an exception to this reason. Ask learners to think of a reason why this province generated such a large amount of waste per person).
   It may also be that the wealthier provinces produce more waste than the poorer provinces.
   Provinces with many tourists and migrant workers may show a large mass of waste per person. However, the tourists are not counted as living in the province.
   Similarly, it may be that not all people, for example migrant workers, who work and stay in a certain province (and therefore also generate waste in that province) are registered as living in the province and so they are not included in the calculation.

The sources of the information in the table are The South African Waste Information Centre and the Department of Environmental Affairs.

<table>
<thead>
<tr>
<th>Province</th>
<th>Average kilograms of waste per person in 2011</th>
</tr>
</thead>
<tbody>
<tr>
<td>Western Cape</td>
<td>675</td>
</tr>
<tr>
<td>Eastern Cape</td>
<td>113</td>
</tr>
<tr>
<td>Northern Cape</td>
<td>547</td>
</tr>
<tr>
<td>Free State</td>
<td>119</td>
</tr>
<tr>
<td>KwaZulu-Natal</td>
<td>158</td>
</tr>
<tr>
<td>North West</td>
<td>68</td>
</tr>
<tr>
<td>Gauteng</td>
<td>761</td>
</tr>
<tr>
<td>Mpumalanga</td>
<td>518</td>
</tr>
<tr>
<td>Limpopo</td>
<td>103</td>
</tr>
</tbody>
</table>

3. Read the information in the table. What does it tell you? Answer the questions:
   (a) Which provinces generate high amounts of waste per person?
   (b) Which provinces generate rather small amounts of waste per person?
   (c) Write down some reasons why you think the waste contribution per person in the different provinces varies so much.

The waste per person is calculated as follows:
The total mass of waste collected by all the municipalities in the province is calculated (added up). Then the total mass is divided by the number of people that live in the province. The kilogram waste per person in 2011 is the waste of the average person in 2011.
7.2 Drawing and interpreting graphs

**Mathematical notes**
Converting the data in the table on page 82 to a bar graph allows learners to see at a glance in which provinces the average waste generated per person is high and in which provinces it is low. Learners are asked to compare the data per province in two ways: firstly by finding the difference (subtracting) and secondly by finding how many times more one is than the other (multiplying or dividing). This lays the basis for working with pie charts. Pie charts also look at proportions of data in relation to each other.

**Teaching guidelines**
Prepare a frame of the bar graph and copies of the pie charts on the board or on posters to use during a class discussion.

**Answers**
1.

2. (a) Western Cape: about 675 kg of waste collected per person; Eastern Cape: about 113 kg of waste collected per person; 675 kg – 113 kg = 562 kg
   The waste per person collected in the Western Cape was 562 kg more than the waste per person collected in the Eastern Cape.

   (b) The bar for the Eastern Cape fits almost seven times into the bar for the Western Cape. Therefore, on average, a person in the Western Cape generates almost seven times the amount of waste that a person in the Eastern Cape does.
Teaching guidelines

Learners will have seen and interpreted fractions as sectors of a circle in the Foundation Phase. However, they may only have worked with examples where all the sectors in any circle are the same size. In question 4, each sector represents a different fraction (fifths, quarters, eighths, etc.). You can first let learners work with cut-out circles, which they fold into quarters. Then ask them to mark half and three eighths. Show learners a circle with a quarter and five eighths marked, and ask them to identify the fraction parts with reason.

In question 4 learners will have to approximate what fraction of the circle each sector is.

In question 4(e), learners may at first say the statement is false. You can then ask the class how they think builders’ rubble could be at least partially recycled.

Answers

3. (a) Learners can compare any two bars, so their answers will vary. One example is provided here:
Northern Cape: about 547 kg per person; Free State: about 119 kg per person. Therefore, a person in the Northern Cape generates about 428 kg more waste than a person in the Free State.
The bar for the Free State fits about four and a half times into the bar for the Northern Cape. Therefore, a person in the Northern Cape generates about four and a half times more waste than a person in the Free State.
(b) Learners check each other’s calculations and estimates.

4. (a) The green sector is about one fifth of the circle, therefore organic waste formed about one fifth of all municipal waste in the Western Cape in 2011.
(b) The waste that could be recycled was between a quarter and a fifth of all municipal waste in the Western Cape in 2011.
(c) The blue sector is about three eighths of the circle, so about three eighths of all waste in Gauteng in 2011 was waste that could not be recycled.
(d) In Gauteng. The red sector represents recyclable waste: it is about one quarter of the circle.
(e) True. Composting will eliminate the organic waste represented by the green sectors; recycling will eliminate the waste represented by the red sectors and some of the builders’ rubble represented by the yellow sectors. Then it is only a little more than the waste represented by the blue sectors that will go to the landfills.
Teaching guidelines

Data handling is about making sense of large sets of data. In data representations the information is rounded to approximate values. Learners are used to working with exact answers in Mathematics and may resist working with approximations. Explain to learners that they have to find a scale where the rounding shows the relative size of the groups as accurately as possible. In question 6, let learners try out a scale of 25 and of 50 and discuss the amount of inaccuracy. Then let them try scales of 30, 20 and 10. Thirty is the most convenient rounding for the data, as it shows the relative proportions of the groups of waste pickers most accurately, and yet the bars are not too long. Learners must remember to always say “almost” when they read the frequencies from pictographs.

Answers

5. (a) Yes, the number of people who earn an income by recycling is slowly increasing. You can see this at a glance by looking at the pictograph. In 2009 there were about 35 000 workers and in 2014 about 50 000 workers.
   (b) 2011: about 40 000 people   (c) 2013: about 45 000 people

6. The pictograph below gives a summary of the number of people who earn their income by recycling plastic. These people are informal workers.

   (a) Look at the pictograph. Do you think the number of people who earn their income by recycling plastic is increasing? Explain why you say so.
   (b) Use the key to work out how many people earned their income by recycling plastic in 2011.
   (c) Use the key to work out how many people earned their income by recycling plastic in 2013.

   Number of street waste pickers in Pretoria

<table>
<thead>
<tr>
<th>Year</th>
<th>2009</th>
<th>2010</th>
<th>2011</th>
<th>2012</th>
<th>2013</th>
<th>2014</th>
</tr>
</thead>
<tbody>
<tr>
<td>Key:</td>
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</tbody>
</table>

   Learners can choose any sensible icon, such as stick figures for example, to represent groups of people. Some learners may use a scale of 1:10 or 1:20 instead of the scale of 1:30 used here.
Possible misconceptions
This may be the first time that learners work with pictographs with many-to-one representations. Some learners may not realise that each icon represents more than one data item. You may need to alert learners to the key. You can ask learners why each person in the information is not represented by one icon, i.e. why do icons represent groups of people.

7.3 Summarising and analysing data

Mathematical background
Graphs provide a visual image of data. Another way of analysing data is to look at the shape of the data, i.e. how spread out or clustered it is. Measures of data allow one to describe the spread and the centre of the data. In this section learners begin to examine the typical value or centre of the data by using the concept of mode. The mode of ungrouped numerical data is the data value that appears most.

In many areas of Mathematics there are one or more definite answers to questions or calculations. Data handling often involves a much higher degree of uncertainty. Reasoning in uncertain situations may make learners feel insecure, because they are not used to doing it. In data handling learners need to use their analysis of the data as evidence to back up an argument. In question 3 you may need to support learners to give reasons for their answers that they find in the data in the table.

How to make a pictograph
Step 1: Draw a horizontal line and mark it off in equal lengths. Write the years in the correct order below the line. This is the category axis.

Step 2: Decide on an icon (symbol) and on the number of people that your icon will represent. To do this, look at the size of your largest data value. You may choose a number such as 10, 20, or 30.

You may also make an icon that represents half the number you chose; for example, if you decided your icon will represent 30, then half your icon will represent 15.

Step 3: Round off the data values by counting in the number you chose. If you chose 30, count in 30s. As you count, write down the number closest to each data value. For example, if you count in 30s, then 150 is closest to 154.

Calculate the number of icons you need to represent the data for each year. For example, if your icon represents 30 people, you will need 5 icons to represent 150 people.

Step 4: Draw the icons neatly above each year. The icons must be arranged evenly so that you can see at a glance what the data tell.
Teaching guidelines

You can begin by clarifying what a recycling buy-back centre is. You can also ask learners what kinds of information will help a recycling buy-back centre to run more efficiently and effectively. You can compare their answers with the information provided on page 86 of the Learner Book.

Completing the table in question 3 requires doing 20 calculations of the same type, i.e. adding four values. To save class time and prevent learners from getting bored, you can let different learners do different calculations. Let at least two learners do each calculation so that they can check each other’s answers. It is more valuable for learners to add one group of numbers and check to find the reason for any mistake they might have made, than to ask all learners to do all 20 sets of addition.

There are some questions in this section that require calculations: these questions will have exact answers. However, most of the questions require learners to reason about the context and the data. In these questions learners’ answers will vary. It is important to accept all reasonable answers, but it is more important that learners share these answers with each other, and that you allow time for learners to discuss these answers and to learn from each other.

<table>
<thead>
<tr>
<th>Day</th>
<th>Time</th>
<th>Mass of unsorted waste</th>
<th>Mass of sorted waste</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Paper</td>
<td>Glass</td>
</tr>
<tr>
<td>Monday</td>
<td>10:00</td>
<td>106 kg</td>
<td>21 kg</td>
</tr>
<tr>
<td></td>
<td>12:00</td>
<td>100 kg</td>
<td>23 kg</td>
</tr>
<tr>
<td></td>
<td>14:00</td>
<td>116 kg</td>
<td>41 kg</td>
</tr>
<tr>
<td></td>
<td>16:00</td>
<td>78 kg</td>
<td>25 kg</td>
</tr>
<tr>
<td>Tuesday</td>
<td>10:00</td>
<td>114 kg</td>
<td>25 kg</td>
</tr>
<tr>
<td></td>
<td>12:00</td>
<td>81 kg</td>
<td>24 kg</td>
</tr>
<tr>
<td></td>
<td>14:00</td>
<td>94 kg</td>
<td>35 kg</td>
</tr>
<tr>
<td></td>
<td>16:00</td>
<td>84 kg</td>
<td>34 kg</td>
</tr>
<tr>
<td>Wednesday</td>
<td>10:00</td>
<td>82 kg</td>
<td>25 kg</td>
</tr>
<tr>
<td></td>
<td>12:00</td>
<td>91 kg</td>
<td>46 kg</td>
</tr>
<tr>
<td></td>
<td>14:00</td>
<td>100 kg</td>
<td>31 kg</td>
</tr>
<tr>
<td></td>
<td>16:00</td>
<td>115 kg</td>
<td>24 kg</td>
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<tr>
<td>Thursday</td>
<td>10:00</td>
<td>113 kg</td>
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<td>12:00</td>
<td>101 kg</td>
<td>50 kg</td>
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<td>14:00</td>
<td>112 kg</td>
<td>30 kg</td>
</tr>
<tr>
<td></td>
<td>16:00</td>
<td>92 kg</td>
<td>47 kg</td>
</tr>
<tr>
<td>Friday</td>
<td>10:00</td>
<td>101 kg</td>
<td>36 kg</td>
</tr>
<tr>
<td></td>
<td>12:00</td>
<td>102 kg</td>
<td>36 kg</td>
</tr>
<tr>
<td></td>
<td>14:00</td>
<td>117 kg</td>
<td>44 kg</td>
</tr>
<tr>
<td></td>
<td>16:00</td>
<td>113 kg</td>
<td>32 kg</td>
</tr>
</tbody>
</table>
**Answers**

1. (a) Learners’ answers will vary, for example: I wonder if she receives more waste on a Monday, i.e. after a weekend, than on other days? I wonder if she receives more glass than paper? I wonder if she receives more waste in the morning or in the afternoon? I wonder how much glass/paper/plastic she typically receives per day?

(b) The sample questions in (a) can all be answered with the data. Three examples are provided:

To answer “I wonder if she receives more waste on a Monday, i.e. after a weekend, than on other days?”: Compare the total amounts of waste that she receives each day. Draw a bar graph.

To answer “I wonder if she receives more glass than paper?”: Compare the amounts of glass per day to the amounts of paper per day. Draw two bar graphs.

To answer “I wonder if she receives more waste in the morning or in the afternoon?”: Compare the total amounts of waste received each morning with the total amounts of waste received each afternoon. Draw two bar graphs.

2. (a) 25 kg

(b) There are four modes: 40 kg, 41 kg, 49 kg and 56 kg

3. | Day     | Total mass of unsorted waste | Total mass of paper | Total mass of glass | Total mass of plastic |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Monday</td>
<td>400 kg</td>
<td>110 kg</td>
<td>203 kg</td>
<td>87 kg</td>
</tr>
<tr>
<td>Tuesday</td>
<td>373 kg</td>
<td>118 kg</td>
<td>171 kg</td>
<td>84 kg</td>
</tr>
<tr>
<td>Wednesday</td>
<td>388 kg</td>
<td>126 kg</td>
<td>179 kg</td>
<td>83 kg</td>
</tr>
<tr>
<td>Thursday</td>
<td>418 kg</td>
<td>150 kg</td>
<td>190 kg</td>
<td>78 kg</td>
</tr>
<tr>
<td>Friday</td>
<td>433 kg</td>
<td>162 kg</td>
<td>171 kg</td>
<td>100 kg</td>
</tr>
</tbody>
</table>

(a) On a Friday. It may be because the buy-back centre is in an area where people put out their bins on a Friday; it may be because the street waste pickers collect during the week and deliver on a Friday; it may be that more waste pickers deliver waste on a Friday than on other days. We need more information to be sure.

(b) They receive more glass on a Monday than on any other day. It may be that people drink more beer and wine over weekends and that there are more bottles to collect on a Monday. We need more information to be sure.
3. (c) Plastic is lighter than glass. If you compare two bottles of the same size, the plastic bottle is lighter than the glass bottle. So, a trolley full of plastic will be lighter than a trolley full of glass.

4. Learners' answers will vary. One example could be:
   On Monday the greatest number of waste pickers delivered waste: 25. On Thursday the smallest number delivered waste: 12. On both Wednesday and Friday 20 waste pickers delivered waste. On Tuesday 15 waste pickers delivered waste.

5. (a)
<table>
<thead>
<tr>
<th>Day</th>
<th>Total mass of unsorted waste</th>
<th>Money paid</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monday</td>
<td>400 kg</td>
<td>R4 000</td>
</tr>
<tr>
<td>Tuesday</td>
<td>373 kg</td>
<td>R3 730</td>
</tr>
<tr>
<td>Wednesday</td>
<td>388 kg</td>
<td>R3 880</td>
</tr>
<tr>
<td>Thursday</td>
<td>418 kg</td>
<td>R4 180</td>
</tr>
<tr>
<td>Friday</td>
<td>433 kg</td>
<td>R4 330</td>
</tr>
</tbody>
</table>

She should plan to have about R4 500 available if this is a typical week. Some weeks may vary, but R4 500 is enough for 17 kg more than the biggest amount of waste this week.

(b) No, it is very unlikely that the data will be exactly the same every week. The amounts of waste collected vary, the number of waste pickers that deliver vary, and the times at which they deliver waste to the buy-back centre vary. But if Mrs Mmako says this week is typical, then she means there is not much variation from week to week.

(c) Amount paid: R4 000
   Total number of waste pickers: 25
   R4 000 ÷ 25 = R160

   On a Monday each person typically received about R160.
7.4 Project

**Teaching guidelines**
This project will take about three weeks to complete. Learners must plan the project in the first week and inform the participants (people from whom the data is going to be collected). During the second week they must gather data by sorting and weighing the waste every day, and record the data. During the third week they must represent, analyse and interpret the data.

**Week 1**
Help learners with the following preparations:
- Make labels for the different containers that will be used to hold the waste.
- Talk to the school during assembly to inform them about the project.
- Find a suitable scale to weigh the waste.
- Prepare a data-collecting sheet (see assessment criteria below) that shows the day, the kind of waste and the mass.
- Form groups and decide who will gather and analyse data of different kinds of waste.

**Week 2**
- Help the groups to collect data about different kinds of waste.
- Help the groups to collect, sort and weigh the waste daily (remember to collect waste paper from the office too).

**Week 3**
- Share your assessment criteria with learners. For example:
  - **Data gathering**: The data must be recorded daily in a table. (5 marks)
  - **Data representation and analysis**: The data must be represented in bar graphs or pictographs. The graphs must have a heading, labels on the axes and/or a key. The scale must be correct. The bars must be drawn accurately. The graphs must be neat and easy to read. (10 marks)
  - **Data interpretation and reporting**: Each group must write a report to say what questions they wanted to answer, how and where they gathered the data, and what they found. (10 marks)
- Provide learners with paper to draw the graphs.
- Arrange for learners to present their findings to each other, or to an audience of schoolmates and teachers.

**Resources**
Containers for waste collection; a scale to weigh waste; data-collecting sheets; paper to draw graphs (see Addendum, pages 413 and 414)
Grade 5 Term 1 Unit 8

Properties of two-dimensional shapes

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<th>Content</th>
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</tr>
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<td>Lines are essential parts of all shapes</td>
<td>91 to 93</td>
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<td>8.2 Figures with different shapes</td>
<td>Identifying and naming polygons by counting the number of sides</td>
<td>94 to 96</td>
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<td>8.3 Angles</td>
<td>Angles are used to compare the orientations of pairs of straight lines</td>
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<td>8.4 Right angles around us</td>
<td>Right angles occur when two lines cross to form four equal angles</td>
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<tr>
<td>8.5 Angles and sides in two-dimensional figures</td>
<td>Comparing shapes by comparing lengths of sides, and angles</td>
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CAPS time allocation 7 hours
CAPS page references 21 to 22 and 147 to 149

Mathematical background

Figures are made up of curved and straight lines. The lines may be connected, or not, to form closed or open figures. The lengths of the lines may vary within a figure and also from figure to figure. The directions that lines face (orientations of lines) vary within a particular figure and also from figure to figure. We use the concept of angle to compare the orientations of pairs of straight lines. Length and angle size are the basic quantities we use in geometry.

Both length and angle are measurable quantities. Learners go through four stages when learning to measure:

1. **Identifying and understanding the property they are measuring**
   Most Grade 5 learners know when they are measuring length, mass or capacity/volume. Angle, however, is a new measure and most learners struggle to understand what they are measuring when they first encounter angles. Spend time developing the concept of angle.

2. **Comparing and ordering examples of a particular measure** (see questions 1 and 2 of Section 8.4)
   Instead of measuring angles, learners are asked to compare different angles between straight lines. This is to allow them the opportunity to develop a feel for the sizes of angles. Learners who can say “This angle is bigger than that angle” with the same confidence as when they say “This line is longer than that line” will be in a very strong position when they eventually begin to measure angles. In this unit learners first compare angles by sight.

3. **Using informal or non-standard units to measure** (see question 6 of Section 8.4 and question 2 of Section 8.5)
   In this unit learners make templates of angles and use them to check whether angles are the same size or not.

4. **Using formal or standard units to measure**
   Measuring with formal or standard units allows many people in many different places to measure, quantify and compare measurements using the same measure. Learners will measure angles with protractors from Grade 7 onwards.

The aim is to develop an understanding of what an angle is, and what does and does not affect the size of an angle, before working with formal instruments to measure angles in later grades. Without this focus on **angle concept**, many learners may never understand what an angle is. In this unit many of the activities must be allowed to be learner driven.
8.1 Curved and straight lines

Mathematical notes
There are two basic kinds of lines: straight lines and curved lines. Curved lines may be parts of circles, or they may not.

This section is an informal look at straight lines and curved lines. When we speak of these types of lines we usually mean smooth lines. There are also “lines” that are not smooth. They may look straight or curved as a whole, but they may be quite crooked close-up. The lines we attempt to draw freehand may not be smooth; they may be rather crooked.

Teaching guidelines
If possible, encourage learners to find interesting examples of shapes made up of curved lines and straight lines.

You can begin by asking learners: “What kinds of lines do we find in the shapes around us?”

For enrichment (you may decide if the time is ripe for your learners to explore a bit further) you may ask your learners a question like: “Is a crooked line crooked everywhere?” or “Can we imagine a crooked line as many tiny straight or curved lines?”

Drawing lines helps to focus learners’ attention on the features of the lines. In this section learners are asked to draw various curved and straight lines freehand. Often our skill at representing our ideas in diagrams does not do those ideas full justice. So, when your learners draw freehand straight lines and freehand circles, encourage them to do so as neatly as they can, but do not allow them to spend too much time on each line or circle. We often draw freehand sketches to explain something to someone else. Everyone agrees that the not-so-smooth straight and curved lines we draw represent perfectly smooth straight and curved lines in our heads.

Rock artists used both curves and straight lines in their art.
Notes on questions

Curved lines may or may not be parts of circles. In question 1 there are two shapes with curved sides and two shapes with four straight sides. Drawing lines helps to focus learners’ attention on the kind of line (in these examples straight or curved). Seeing shapes within shapes is a useful skill: learners will use this skill often when they do FET geometry.

Answers

1. (a) Learners’ own freehand drawings of the two circles of different sizes
   (b) Learners’ own freehand drawings of the two squares of different sizes and with different orientations
Notes on questions

The picture of a curve drawn over rectangles in question 2 is used to focus learners’ attention first on curved lines and then on straight lines.

One kind of spiral is shown on page 93 of the Learner Book. There are other kinds of spirals. An example is shown alongside.

The only requirement for a spiral is that, as it continues to spiral (widen), the line becomes longer and moves further away from the starting point at the centre of the spiral.

Answers

2. (a) Learners’ freehand drawing of a spiral. It does not have to be the same kind of spiral as the one shown on page 93.
   (b) Learners’ freehand drawing of the blue lines that make up the eight rectangles, i.e. they copy the blue diagram but not the red spiral on it.

3. Learners’ freehand drawing of lines

4. Learners’ freehand drawing of circles
8.2 Figures with different shapes

**Mathematical notes**

Two-dimensional figures are characterised by

- the number of sides they have,
- whether the sides are straight lines or curved lines,
- the lengths of the sides, and
- how the sides are oriented towards each other at the places where they join (i.e. the size of the angle between them).

In the Intermediate Phase, learners begin to focus on the properties of shapes. When we group shapes according to their properties, we call it classifying shapes.

**Notes on questions**

Question 1 draws learners’ attention to angles. The concept of angle is introduced informally here. This is further explored in Sections 8.3, 8.4 and 8.5. Question 2 continues the focus on straight and curved lines. Question 3 focuses on open and closed figures. In questions 4 to 8 and Section 8.5 learners work with closed figures and their shapes.

**Teaching guidelines**

Encourage learners to begin thinking about the properties of shapes and how different shapes are related to each other. Drawing figures and talking about their shapes is a way to start.

You may open the section with a few questions that will help learners to compare shapes and, in so doing, to group and classify them. The following two questions may be useful: “What do these figures have in common?” and “In what way do the figures differ?”

It is advisable to view this section as being about more than just its contents. Focus also on the process of organising and classifying.

**Answers**

1. (a) to (c) Learners’ own freehand drawings of the angles
2. (a) to (b) Learners’ own freehand drawings of the shapes
3. Open figures: A and C
   Closed figures: B and D
Teaching guidelines
In question 4 learners will classify the figures by looking only at their number of sides. You may find that some learners lose focus and start looking at other properties of the figures. If so, help them to return their focus to counting the number of sides of each figure.

Learning to focus on specific things when there are many things that may grab our attention is a very important skill in Mathematics and in life. Generally, refocus learners’ attention on the particular characteristic under discussion whenever they blur different characteristics and lose focus (e.g. if they muddle up length and angle size when asked about only one of these).

Possible misconceptions
Sometimes when learners see figures that look like stars, they count the pointers of the stars instead of counting the sides of the figures. If learners incorrectly call Figure G in the Learner Book a pentagon or Figure I a quadrilateral, then they have counted the number of pointers and not the number of sides. You can ask learners that make this mistake to draw larger versions of these figures, and to count the sides as they draw them.

Answers
4. (a) Triangles: H
(b) Quadrilaterals: B, D, M, S, U
(c) Pentagons: A, O, P, Q
(d) Hexagons: C, F, K
(e) Heptagons: E, J, L, N, R, T
Teaching guidelines
In questions 5, 6, 7 and 8 you can start by asking learners to talk about “What is the same in all three figures?” This will consolidate the fact that we name polygons according to their number of sides. However, now they will also need to think about the lengths of the lines and the sizes of the angles. Let learners puzzle this out themselves.

Notes on questions
Questions 5 to 8 anticipate the work that learners will do on angle size and side length in Section 8.5. You might like to read ahead to that section.

Intermediate Phase learners are exposed to both irregular and regular shapes. Learners are expected to recognise two-dimensional shapes, whether they are irregular or regular. Question 4 on page 95 of the Learner Book is a good example of the range of each kind of shape that learners are expected to recognise and name. Irregular shapes are the more general form. Learners are not examined on either the definition of regular shapes or the ability to distinguish regular from irregular shapes. You will notice that they are not expected to do either in this unit.

This section ends with a definition of regular polygons, and the red figures are examples of these. This definition is intentionally left to the end of the section because it is not a focus in the unit.

Possible misconceptions
Learners may have the regular two-dimensional shapes (like those in red) in mind when they are asked to make decisions about the characteristics or names of figures they are shown. For example, they may recognise only the red figure in question 7 as a pentagon. They may say that irregular pentagons are not pentagons (e.g. the black figures in question 7 or pentagons that are shaped like an outline of a house: 🐸). In such cases remind learners that the naming is about the number of sides, not about the orientations or lengths of sides.

For a polygon to be regular, both the following conditions must be met: all the sides must be the same length and all the angles must be the same size. If only one of the conditions is met, a figure will not be regular. A square is regular because all its sides are the same length and all its angles are right angles. A rectangle is not regular because although all its angles are right angles, all its sides are not the same length. A rhombus is not regular because although all its sides are the same length, all its angles are not the same size.

Answers
5. to 8. Different side lengths and different angle sizes
8.3 Angles

**Mathematical notes**

The idea of angle can only be properly understood with reference to the ideas of direction and rotation (turn). Two lines that do not have the same direction are said to be at an angle to each other. The difference between the directions of two lines can be measured in terms of how much you have to turn the one line to make its direction equal to that of the other line.

Only when the concept of angle is grasped does the need to be able to measure angles become important. Resist the temptation to talk about degrees or to focus on using protractors; learners will get to this in Grade 7. Focus on developing the concept of angle.

**Teaching guidelines**

You can let your learners experience angles as changeable things (i.e. variables). The examples of opening a door, lifting an arm and opening a book will help fix this idea in learners' minds. Ask them simple questions such as “Is the angle getting bigger or smaller?” and “Describe how the angle is changing” while a door or book is being opened or closed, or a volunteer lifts or drops a straightened arm.

You can also use two sticks to show the concept of angle described in the first paragraph of the “Mathematical notes” above, or let learners work with two strips of cardboard (see the Grade 6 Learner Book, page 93).

**Possible misconceptions**

The angle concept is one of the most troublesome in school mathematics. Many learners go on to tertiary education without a meaningful grasp of what an angle is. The most common misconception is that an angle is somehow a length measurement.

There are two ways you can try to avoid or change this misconception. One way is to give learners a set of cut-outs of shapes of different sizes, but ensure that they all have the same angle at one corner. First ask learners whether, just by looking carefully, they think the angles are the same or not. Then ask learners to put the shapes on top of each other to confirm they have the same angle. Another way is to have a volunteer stand with his one arm extended and raised away from his side to form an angle between his arm and upper torso. Ask the volunteer to keep his arm in a fixed position. Place a straight stick or ruler in his hand and ask learners if the angle has changed. Place another stick/ruler along his side and ask the same question again. As long as the volunteer keeps very still, the angle between his arm and torso is unchanged.

**Answers**

1. Learners’ descriptions of angles in the classroom will differ from class to class.
Answers

2. (a) to (f) Learners’ own drawings of lines and arcs to show angles. Some examples are shown below.

2. There are angles in the pictures below. Make simple but neat drawings of the lines that cross to form the angles. Draw arcs to show the angles.
8.4 Right angles around us

**Mathematical notes**

Right angles are important references in geometry. If you can recognise a right angle, then you know whether an angle is bigger or smaller than a right angle. So recognising right angles helps learners to distinguish acute angles from obtuse angles from Grade 6 onwards. It also helps learners to know that they have read the correct scale on a protractor when they start using protractors in the Senior Phase.

Right angles also play a very important role in applications of mathematics in the construction industry, in woodwork, and so on.

The right-angle template is a tool. It allows us to decide whether a given angle is a right angle or not. This is the germ of the idea of measuring angles. To measure the size of angles we need some sort of reference instrument. The right-angle template is simply a special reference instrument for right angles. The idea of making templates for other angles arises in the next section.

**Teaching guidelines**

You can use the summary paragraphs and related sketches to show learners that when two lines cross and make four angles of the same size, we call these angles right angles. You can then demonstrate how to fold a right-angle template. Ask learners to walk around the classroom and find three angles: one right angle, one angle smaller than a right angle, and one angle bigger than a right angle.

When learners do question 2, ask them not to copy the sketches on page 99. They should rather draw two lines that form different angles than those in the sketch when they cross.

**Answers**

1. and 2. Learners’ own freehand drawings
**Teaching guidelines**

Make a plumb line in class and demonstrate how it can be used to check whether a cupboard stands upright.

**Answers**

3. Check with a right-angle template whether the angle between the table top and the plumb line is a right angle.

4. Monitor learners' practical activity.

5. Monitor learners' practical activity.

6. (a) to (c)
8.5 Angles and sides in two-dimensional figures

Mathematical notes
This section brings together the ideas of line size (length) and angle size. The idea of an angle template for any angle is also explored.

Teaching guidelines
Learners are asked to make comparisons of angles and lengths in a number of figures, and to draw conclusions about their shapes. To do this meaningfully, they need a way of showing that one angle is smaller than another, or that one line is longer than another. In all cases, the only way to be certain is to have a reference tool. Encourage learners to find ways of checking using tools. Sheets of paper can be used to fold or cut out angle templates. Explain to learners that, unless the angle template they make fits exactly on the angle in the given figure, they are not working accurately.

Be aware that learners are never asked to give the lengths of any of the sides of the figures. It may be best not to use a ruler to measure line lengths at first, but rather to mark off lengths on the edge of a sheet of paper – a length template. This will establish a conceptual link with the idea of individual angle templates, which are either folded or cut out to be exactly the same as a given angle.

For questions 1 and 2, it will help learners if one learner has the Learner Book open on page 101 and the learner next to them has it open on page 102. This will allow learners to read the questions and see the figures at the same time, instead of trying to keep the questions in their heads while they turn the pages to see the diagrams.

Notes on questions
In question 1, ask learners to look at the figures in the Learner Book when they answer the questions about the angles and to only use their own drawings for writing down what they have decided (their own drawings are unlikely to be very accurate).

Answers
1. (a) and (b) All angles are smaller than right angles and should be marked with A.
   (c) and (d) All angles are right angles and should be marked with c.

Possible extension
When learners are asked to draw copies of given figures it is unlikely they will make very accurate copies to begin with. Allow them to work in small groups to compare how well they have copied particular figures. It is very likely that there will be some variation between their individual efforts. This raises the important questions: “How can we decide if my copy is good?” “How can we tell if her copy is better than his?” “How do we make sure that my copy is an exact copy?” etc. The key is to make angle and length templates.
Notes on questions
In question 2 (as in question 1), learners have to base their decisions on the figures in the Learner Book, not their own drawn figures, which are unlikely to be exact copies of the given ones.

Answers
1. (e) No right angles. The angles at the top left and bottom right of the figure are bigger than right angles. The angles at the top right and bottom left are smaller than right angles.
   (f), (g), (h): No right angles. All the angles are bigger than right angles.
2. (a) Figures with equal-length sides: (a), (d), (f), (g)
   (b) Figures with equal-size angles: (a), (c), (d), (f), (g)
3. (a) Learners' own work: the other two angles will be smaller than right angles.
   (b) Learners' own work. It is impossible to draw a triangle with two angles bigger than right angles because the lines/sides will never meet (i.e. a closed figure cannot be formed).

2. Compare the figures in question 1.
   (a) Which of the figures have sides that are all the same length?
   (b) Which of the figures have angles that are all the same size?
       Make angle templates to help you decide.
3. (a) Draw a triangle with an angle that is bigger than a right angle.
       Look at the other two angles of your triangle. Are they smaller or bigger than a right angle?
   (b) Try to draw a triangle with two angles that are bigger than right angles. Explain what happens.
Notes on questions

Note that question 5 refers back to question 1 (page 101 of the Learner Book), not to question 4 (page 103). It may help learners if one learner has the Learner Book open on page 103 and the learner next to them has it open on page 101.

You could also ask learners to identify which figures in question 4 are squares, which are rectangles and which are parallelograms. Here you can check whether learners are able to identify squares when their sides are not parallel to the sides of the page. The letters of the alphabet p, q, d and b all have the same shape, but are considered different because they face different directions. Sometimes learners think that if shapes face a different direction they are different shapes. This misconception often happens with squares. The shapes below are all squares.

It is important that learners see the same shapes in a range of different positions. You can cut a piece of card into the shape of a square. Place it against the board and trace around it. Move it to a different place on the board and turn it so that no side is parallel to the edges of the board. Repeat this several times. Each time ask learners to identify the shape that you have drawn. Ask them whether the properties of the shape have changed.

Question 6(b) anticipates the work that will be done in Term 3. You might like to read the notes for Section 6.2 in Term 3 Unit 6 of this Teacher Guide.

Answers

4. (a) The blue and black quadrilaterals have right angles only; the red quadrilaterals have no right angles.
   (b) The black and blue figures are similar in that all their angles are right angles. They are all quadrilaterals. They all have straight sides.
   (c) The black figures have four sides of equal length. The blue figures have two pairs of opposite sides with different but equal lengths.

5. (a) Squares: Figure (d)
   (b) Rectangles: Figures (c) and (d)

6. (a) No, all rectangles are not squares.
   (b) Yes, all squares are rectangles.
Grade 5 Term 1 Unit 9  
Capacity and volume

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<td>Understanding the difference between capacity and volume</td>
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<td>9.2 Make a measuring jug</td>
<td>Using small units of volume to make a scale on a bottle, to measure any volume that can fit in the bottle</td>
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<td>9.3 Litre and millilitre</td>
<td>Learning about the units for measuring volume and capacity</td>
<td>108 to 110</td>
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<tr>
<td>9.4 Calculations and problem solving</td>
<td>Using the concepts of volume and capacity in different contexts</td>
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</table>

**CAPS time allocation**  
5 hours

**CAPS page references**  
26 and 150 to 153

**Mathematical background**
- The term “volume” is used to indicate how much space is taken up by an amount of liquid or other form of material, or by an object.
- The term “capacity” is used to indicate how much space is available in a container, irrespective of how much of the space is taken up at a given moment.
- The same units of measurement are used for volume and capacity.

Though the capacity of a cup or the volume of a liquid is given in litres and millilitres, these units are based on cubic units. The millilitre is really the cubic centimetre.

Length we measure in straight centimetres. Area we measure in centimetres × centimetres (cm²; draw yourself a square with each side 1 cm long). Volume we measure in centimetres × centimetres × centimetres (cm³; draw yourself a cube, like the one you see on page 105 of the Learner Book; each side is 1 cm long).

A litre is really 1 000 of these little cubes. If you packed 1 000 of the little cubes together you would get a bigger cube, 10 cm × 10 cm × 10 cm in size. (Draw this for yourself.) The volume of that cube is one litre. So, one litre is $10^3$ cubic centimetres or 1 000 cubic centimetres.

If we take the litre as our standard unit of volume, then the small unit is the millilitre. So 1 ℓ has the same volume as 1 000 ml.

**Resources**
A tall, narrow glass and a short, wide glass; eight identical glasses; four glasses with the same height but different diameters; 1 ℓ coloured liquid (e.g. tea or cooldrink or water coloured with food colouring); four or more standard teacups; a 1 ℓ container; water; sand; plastic bottles, identical glasses or jars, etc. – see Section 9.2
9.1 Capacity and volume

Teaching guidelines
This unit deals with liquids and the volumes of liquids, but do not treat it as something strange and different to the mathematics the learners already know. Everything they have learnt, including fractions, division and scales on measuring instruments, is going to be useful.

Possible misconceptions
Many young learners will say that the glasses in question 1 contain the same volume of water, and in question 2 that the glass at the beginning of the row contains more than the glass at the end of the row. They look only at the height of the water and do not think about the diameter of the glasses. Later on, they will begin to realise that the diameter of the glass is also important, and that they must consider both height and diameter. When learners consider both dimensions, by themselves and without you telling them, they have developed a new cognitive ability.

Not all learners, even in high school, have this thinking ability, but you can help them to develop it. Do this practically with a tall, narrow glass and a short, wide glass. Fill a container with coloured water and pour all the water into the tall glass. Then refill the same container and pour all the water into the short, wide glass. How can the learners work out that the two glasses contain equal volumes of water? Well, the same container held both volumes, so they must be equal!

Critical knowledge
It is important that learners understand the difference between capacity and volume. “Capacity” means how much a glass (or other container) can hold – it doesn’t matter whether there is something in the glass or not. “Volume” is about how much water (or other substance) is actually in the glass. The glass might not be full. We can say this in another way. We can say “the glass is not full to capacity”.

Notes on questions
Learners may have heard a sports commentator say: “The stadium is full to capacity.” This means the stadium is holding all the people it can hold.

Do not tell learners to compare the diameters of the glasses in question 2. Rather ask them to tell you all the differences they can see between the four glasses. Then some of the learners will notice that the diameters are different.

Answers
1. (a) The glasses contain different volumes of water.
   (b) The sizes of the glasses differ.
Possible misconceptions

Some learners may believe that there is less water in each glass as one moves from left to right in the picture in question 2. This may result from the misconception that if the height of the water column is less (i.e. lower), the amount (volume) of water is also less, irrespective of the width of the glass. To help such learners overcome this misconception, you may demonstrate that when the water in a narrow glass is poured into a wide glass, the height is lower in the wider glass. Also demonstrate that when the water is poured back into the narrow glass, it reaches the same level as before.

Because the focus is strongly on liquids in developing the important distinction between volume and capacity, there is a danger that learners may develop the idea that volume relates to liquids only. To prevent this misconception, you may fill two similar glasses to the same level with water and sand respectively, and point out to learners that the volume of the sand in one glass is equal to the volume of the water in the other glass.

Answers

2. Yes, it is possible. The water in the tall, narrow glass might have the same volume as the water in the wider glass next to it. That volume of the water might be the same as the volume of water in the wide glass at the end of the row. As the glasses become wider, but their heights remain the same, their capacities increase. So, as the glasses widen, the water levels decrease and it is therefore possible that all glasses contain equal volumes of water. (Do your learners understand the word “might”? We say “might” when something is possible but we have not taken measurements to make sure.)

3. (a) Approximately 250 ml
   (b) Approximately 300 ml
   (c) 170 ml
   (d) Approximately 30 ml to 50 ml
Teaching guidelines
Ideally you should have a 1 ℓ container with coloured liquid in the class, as well as some cups and 8 glasses. Let learners do questions 4 and 5, then act the questions out with the cups and glasses while you take feedback on the answers.

When taking feedback on question 4, you may draw 4 cups on the board and ask learners what fraction of a litre each cup will contain. Then, when you take feedback on question 5(b), you may ask how many of the glasses contain the same amount of liquid as one of the cups in question 4. You may also write the following number sentences on the board as a description of the situation in question 4:

\[ 1 000 \text{ ml} = 250 \text{ ml} + 250 \text{ ml} + 250 \text{ ml} + 250 \text{ ml} \]
\[ 1 \ell = \frac{1}{4} \ell + \frac{1}{4} \ell + \frac{1}{4} \ell + \frac{1}{4} \ell \]

Once learners have completed question 5, you may ask them to write similar number sentences to describe the situations in questions 5(a) and (b).

Notes on questions
Question 6 provides learners with opportunities to engage with fractions. To do question 6(b) they have to divide 1 000 in 5 equal parts. The answer can be used to produce the answers for questions 6(c) and (e).

To do question 6(d), learners will need to recognise that one tenth of 1 000 is 100. You may ask learners to make and complete tables such as these as an extension to question 6:

<table>
<thead>
<tr>
<th>100 ml</th>
<th>200 ml</th>
<th>300 ml</th>
<th>400 ml</th>
<th>500 ml</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \frac{1}{10} \ell )</td>
<td>( \frac{2}{10} \ell = \frac{1}{5} \ell )</td>
<td>( \frac{3}{10} \ell = \frac{3}{5} \ell )</td>
<td>( \frac{4}{10} \ell = \frac{2}{5} \ell )</td>
<td>( \frac{5}{10} \ell = \frac{1}{2} \ell )</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>125 ml</th>
<th>250 ml</th>
<th>375 ml</th>
<th>625 ml</th>
<th>750 ml</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \frac{1}{8} \ell )</td>
<td>( \frac{2}{8} \ell = \frac{1}{4} \ell )</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Answers
4. 4 cups
5. (a) 10 glasses  (b) 125 ml  (c) 125 ml
6. (a) 2 000 ml  (b) 200 ml  (c) 600 ml
   (d) 700 ml  (e) 2 600 ml  (f) 1 750 ml
9.2 Make a measuring jug

Teaching guidelines
You may make one measuring jug in class as a demonstration, and let learners make their own jugs at home as a project.

1. \(1 \text{ℓ} \quad \text{or} \quad 750 \text{ml} \quad \text{or} \quad 500 \text{ml}\)
2. \(200 \text{ml} \quad \text{or} \quad 150 \text{ml} \quad \text{or} \quad 100 \text{ml}\)
3. 
   \[
   \begin{array}{ccc}
   - & 1000 \text{ml} & - \\
   - & 800 \text{ml} & - \\
   - & 600 \text{ml} & - \\
   - & 400 \text{ml} & - \\
   - & 200 \text{ml} & - \\
   - & 1000 \text{ml} & - \\
   - & 900 \text{ml} & - \\
   - & 800 \text{ml} & - \\
   - & 700 \text{ml} & - \\
   - & 600 \text{ml} & - \\
   - & 500 \text{ml} & - \\
   - & 400 \text{ml} & - \\
   - & 300 \text{ml} & - \\
   - & 200 \text{ml} & - \\
   - & 100 \text{ml} & - \\
   \end{array}
   \]
4. and 5.
   
   \[
   \begin{array}{ccc}
   - & 1000 \text{ml} & - \\
   - & 750 \text{ml} & - \\
   - & 500 \text{ml} & - \\
   - & 900 \text{ml} & - \\
   - & 675 \text{ml} & - \\
   - & 450 \text{ml} & - \\
   - & 800 \text{ml} & - \\
   - & 600 \text{ml} & - \\
   - & 525 \text{ml} & - \\
   - & 450 \text{ml} & - \\
   - & 375 \text{ml} & - \\
   - & 300 \text{ml} & - \\
   - & 225 \text{ml} & - \\
   - & 150 \text{ml} & - \\
   - & 100 \text{ml} & - \\
   \end{array}
   \]
9.3 Litre and millilitre

**Mathematical notes**
Measuring cups such as those shown in question 3 can be used to accurately measure volumes up to 2 ℓ. Although such jugs can actually hold a bit more than 2 ℓ of liquid, their capacity is indicated as 2 ℓ.

**Teaching guidelines**
A model for teaching conversion of units is given on page 416 in the Addendum.

**Answers**
1. 25 ml
   Learners can work it out like this: 10 × spoon capacity = 250 ml, so what number will give you 250 if you multiply it by 10? This is really a “divide by” problem; we have to divide 250 ml by 10 to get the spoon capacity.

2. (a) 40 (b) 1 500 ml

3. | Container | Capacity of container | Volume of juice |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>litres</td>
<td>millilitres</td>
</tr>
<tr>
<td>(a)</td>
<td>2</td>
<td>2 000</td>
</tr>
<tr>
<td>(b)</td>
<td>2</td>
<td>2 000</td>
</tr>
<tr>
<td>(c)</td>
<td>2</td>
<td>2 000</td>
</tr>
<tr>
<td>(d)</td>
<td>2</td>
<td>2 000</td>
</tr>
</tbody>
</table>
Answers

4. Different scales are given below. For each scale, write the numbers and units (ml or ℓ) that should appear at the marks that the arrows are pointing at. Do this from top to bottom. Write your answers in millilitres as well as in fractions of a litre, for example: 50 ml; \( \frac{1}{20} \) ℓ.

4.(a) 1000 ml \( \frac{1}{5} \) ℓ
800 ml \( \frac{4}{5} \) ℓ
300 ml \( \frac{3}{10} \) ℓ
(b) 1000 ml \( \frac{3}{4} \) ℓ
750 ml \( \frac{3}{5} \) ℓ
250 ml \( \frac{1}{4} \) ℓ
(c) 1000 ml \( \frac{4}{5} \) ℓ
800 ml \( \frac{2}{5} \) ℓ
400 ml \( \frac{2}{5} \) ℓ
(d) 1000 ml \( \frac{7}{8} \) ℓ
875 ml \( \frac{7}{8} \) ℓ
375 ml \( \frac{3}{8} \) ℓ
(e) 1000 ml \( \frac{3}{4} \) ℓ
1600 ml \( 1 \frac{1}{2} \) ℓ
600 ml \( \frac{3}{5} \) ℓ
(f) 1000 ml \( \frac{1}{4} \) ℓ
1500 ml \( 1 \frac{1}{2} \) ℓ
500 ml \( \frac{1}{2} \) ℓ
(g) 1000 ml \( \frac{4}{5} \) ℓ
1600 ml \( 1 \frac{2}{5} \) ℓ
800 ml \( \frac{4}{5} \) ℓ
(h) 1000 ml \( \frac{7}{2} \) ℓ
7500 ml \( 7 \frac{1}{2} \) ℓ
1250 ml \( 1 \frac{1}{4} \) ℓ

5. (a) 3 500 ml
(b) 1 250 ml
(c) 125 ml
(d) 2 500 ml
(e) 2 750 ml
(f) 1 250 ml
(g) 4 700 ml
(h) 6 000 ml
(i) 600 ml

1 litre is 1 000 ml.

You can write 1 500 ml as 1 ℓ + 500 ml or as \( 1 \frac{1}{2} \) ℓ.

Other ways to write this are 1,500 ℓ and 1,5 ℓ. The 1 tells you that you have 1 full litre and the 0,500 or 0,5 tells you that you have another \( \frac{1}{2} \) ℓ.

5. Express each of the following in millilitres.

<table>
<thead>
<tr>
<th>(a) 3 ℓ + 500 ml</th>
<th>(b) 1 ℓ + 250 ml</th>
<th>(c) ( \frac{1}{8} ) ℓ</th>
</tr>
</thead>
<tbody>
<tr>
<td>(d) 2,5 ℓ</td>
<td>(e) 2 ( \frac{3}{4} ) ℓ</td>
<td>(f) 1 ℓ + ( \frac{1}{4} ) ℓ</td>
</tr>
<tr>
<td>(g) 4 ( \frac{7}{10} ) ℓ</td>
<td>(h) 6 ℓ</td>
<td>(i) ( \frac{3}{2} ) ℓ</td>
</tr>
</tbody>
</table>
Answers

6. (a) 1 ℓ + 50 ml; 1 250 ml; $1 \frac{1}{2}$ ℓ
   (b) 5 ℓ + 75 ml; $5 \frac{1}{2}$ ℓ; 5 750 ml
   (c) 4 ℓ + 34 ml; 4 734 ml; $4 \frac{3}{4}$ ℓ

7. (a) 19 $\frac{1}{2}$ ℓ; 19 ℓ + 250 ml; 9 250 ml
   (b) 6 $\frac{1}{2}$ ℓ; 6 ℓ + 5 ml; 650 ml
   (c) 87 ℓ + 50 ml; 8 750 ml = $8 \frac{3}{4}$ ℓ; 8,5 ℓ

9.4 Calculations and problem solving

Notes on questions
To help learners get started on question 1, ask them to draw a picture of an empty paper cup and mark it “250 ml”. Then ask them to colour in the cooldrink to a height that shows where 235 ml would reach, and write “235 ml” next to that height.

Answers

1. (a) She needs about 11 985 ml = 11 ℓ + 985 ml. So she should buy 12 ℓ of cooldrink.
   (b) 8 bottles

2. (a) 45 litres
   (b) 45 000 millilitres
   (c) 79 crates
   (d) 1 422 bottles
**Answers**

3. (a) R130  
(b) 6 cartons of milk at R26 per carton  
   (6 cartons of milk at R26 per carton = R156; 9 cartons at R21 per carton = R189)

4. (a) $1\frac{1}{4}$ℓ milk  
(b) 21 scoops  
(c) 75 scoops of ice cream and $6\frac{1}{4}$ℓ milk  
(d) 8 milkshakes and 24 scoops of ice cream

5. (a) R741  
(b) R10,50  
(c) 109 litres

(a) Annette pays R105 for the milk that she buys at the supermarket. How much would she have paid for the same number of cartons at the shop at the filling station?  
(b) What costs less: 6 cartons of milk at R26 per carton or 9 cartons of milk at R21 per carton?

4. Each milkshake at The Sweet Tooth is made with 3 scoops of ice cream and $\frac{1}{4}$ℓ milk.  
(a) How much milk is used with 15 scoops of ice cream?  
(b) How much ice cream is added to $1\frac{3}{4}$ℓ milk?  
(c) How much ice cream and how much milk are needed for 25 milkshakes?  
(d) How many milkshakes can be made with 2 ℓ milk, and how much ice cream will be needed?

5. (a) If petrol costs R9,50 per litre, how much does 78 ℓ petrol cost?  
(b) If 9 ℓ of petrol cost R94,50, what is the price of 1 ℓ?  
(c) If petrol costs R8,00 per litre and you paid R872 to fill your tank, how many litres did you buy?
# Term 2

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**CAPS time allocation**
1 hour

**CAPS page references**
13 to 15 and 156

**Mathematical background**
Number concept involves a variety of aspects, including the following:
- Knowing the number names and the ability to read number symbols aloud fluently by saying the number names, for example, to say “three hundred and fifty-two thousand nine hundred and seventy-six” when reading 352 976.
- The ability to count, i.e. to establish the number of objects in a collection. Being able to say the number names in sequence is a prerequisite for being able to count, but does not in itself constitute the ability to count.
- Being able to write the number symbol and expanded notation for numbers.

**Resources**
Place value cards
1.1 Counting and representing bigger numbers

Critical knowledge
Apart from knowing how to represent numbers in different ways, learners need to have a sense of the size (magnitude) of the collections or quantities described by larger numbers.

Teaching guidelines
Learners often do not have personal experience of large quantities, hence the diagram with 10 000 stripes on page 116 of the Learner Book. Learners have engaged with this diagram before, in Term 1 Unit 1. It may, however, be useful to guide them towards analysing it by asking questions such as those given on the next page, at the start of the lesson.

Then put questions such as these to the whole class, to get them to form ideas of collections of large numbers of objects in their minds:

“Think of three pages like the next page.
How many blocks of 100 are there on the three pages together?
How many stripes are there on the three pages together?”

Show on the board how thirty thousand can be written in different ways:

\[
\begin{align*}
\text{thirty thousand} \\
30 \text{ thousand} \\
30 \ 000
\end{align*}
\]

Answers
1. (a) 40 000  (b) 70 000  (c) 120 000
   (d) 200 000  (e) 260 000  (f) 400 000
2. (a) 20 000  30 000  40 000  50 000  60 000
   70 000  80 000  90 000  100 000  110 000
   120 000  130 000  140 000  150 000  160 000
   170 000  180 000
   (b) 200 000  210 000  220 000  230 000  240 000
   250 000  260 000  270 000  280 000  290 000
   300 000  310 000  320 000  330 000  340 000
   350 000  360 000  370 000  380 000  390 000
   400 000
Suggested questions to start the lesson
You could put these questions to the whole class at the start of the lesson, to help learners to familiarise themselves with the diagram.

1. Estimate how many stripes there are in the whole diagram.
2. The diagram has ten rows of blocks of stripes. How many blocks are there in each row?
3. How many stripes are there in each block?
4. How many blocks are there in the whole diagram?
5. How many stripes are there in each row?
6. How many stripes are there in the whole diagram?
7. How many stripes are there in half of the diagram?
8. How many stripes are there in three rows of the diagram?
Teaching guidelines
In addition to the questions in the Learner Book, let learners “build” some larger numbers with place value cards. Monitor how they do it. It is important that they do not try to build numbers with single-digit cards only, but use the place value cards that show the place value parts of the numbers.

Possible misconceptions
Learners sometimes have the very dangerous misconception that a number is a collection of single digits. Although the number symbol is written with digits, the digits correspond to the place value parts. Working with place value cards helps to combat this misconception.

Answers
3. (a) three thousand millimetres 3 000 mm  
(b) thirty thousand millimetres 30 000 mm  
(c) three hundred thousand millimetres 300 000 mm  
(d) two hundred and eighty thousand millimetres 280 000 mm  
(e) seven hundred and twenty thousand millimetres 720 000 mm
Teaching guidelines

It is very important that learners get some experience in saying the names of larger numbers aloud. Apart from questions 4 to 6, which learners do in writing, you may do a class activity like the following:

Write five 6-digit numbers on the board, for example the numbers below.
A. 308 207
B. 380 207
C. 380 270
D. 308 720
E. 300 827

Ask learners to write down the numbers, with the labels A to E.

Let learners now work in pairs. One learner reads one of the numbers, without stating the label, and the other learner has to recognise which number is read. If the learners have a disagreement, they consult you. Learners take turns.

Answers

4. (a) 200 000 + 90 000 + 5 000 + 100 + 80 + 5 295 185
(b) 900 000 + 700 + 5 900 705
(c) 500 000 + 4 000 + 30 + 8 504 038
(d) 400 000 + 20 000 + 4 000 + 100 + 40 + 3 424 143
(e) 200 000 + 10 000 + 5 000 + 600 + 80 + 2 215 682
(f) 900 000 + 80 000 + 9 000 + 800 + 90 + 8 989 898
(g) 200 000 + 30 000 + 1 000 + 700 + 10 + 1 231 711
(h) 800 000 + 50 000 + 7 000 + 200 + 60 + 8 857 268
Answers

5. (a) seven hundred and eighty-nine thousand three hundred and twenty-four
   \[700\,000 + 80\,000 + 9\,000 + 300 + 20 + 4\]
   (b) five hundred and twenty-eight thousand seven hundred and thirty-eight
   \[500\,000 + 20\,000 + 8\,000 + 700 + 30 + 8\]
   (c) five hundred and one thousand one hundred and three
   \[500\,000 + 1\,000 + 100 + 3\]
   (d) four hundred and forty-one thousand one hundred and sixty
   \[400\,000 + 40\,000 + 1\,000 + 100 + 60\]
   (e) two hundred and eighty-seven thousand five hundred and sixty-four
   \[200\,000 + 80\,000 + 7\,000 + 500 + 60 + 4\]
   (f) four hundred and eighty-seven thousand nine hundred and twenty-three
   \[400\,000 + 80\,000 + 7\,000 + 900 + 20 + 3\]

6. (a) ten
   (b) hundred
   (c) thousand

   (a) 789 324
   789 320
   789 300
   789 000
   (b) 528 738
   528 740
   528 700
   529 000
   (c) 501 103
   501 100
   501 100
   501 000
   (d) 441 160
   441 160
   441 200
   441 000
   (e) 287 564
   287 560
   287 600
   288 000
   (f) 487 923
   487 920
   487 900
   488 000

1.2 Order and compare numbers

Teaching guidelines
You may explain “ascending” and “descending” as “upwards” and “downwards”, and draw arrows to demonstrate this.

Answers

1. 40 800 41 200 41 600 42 000 42 400 42 800
   43 200 43 600 44 000 44 400 44 800 45 200

2. 9 000 11 250 13 500 15 750 18 000
   20 250 22 500 24 750 27 000 29 250
   31 500 33 750 36 000 38 250 40 500
   42 750 45 000 47 250 49 500 51 750
   54 000 56 250 58 500 60 750 63 000

3. and 4. See the next page.
**Answers**

3. 21 965 47 677 66 152 95 923 98 899 98 987
4. 65 153 31 999 31 001 27 180 20 122 20 121
5. 10 000 40 000 70 000 100 000 130 000 160 000
   190 000 220 000 250 000 280 000 310 000
6. 800 000 794 000 788 000 782 000 776 000 770 000
   764 000 758 000 752 000 746 000 740 000
7. 637 173 641 245 646 091 656 488
   662 786 673 168 680 901
8. 999 820 996 788 953 156 945 678
   941 783 928 028 927 891
9. (a) 63 372 > 63 002 (b) 86 762 > 68 872
   (c) 27 901 < 28 817 (d) 35 530 < 53 305
   (e) 390 860 = 390860 (f) 701 847 < 710 874

5. Count in thirty thousands from 10 000 up to 310 000. Write down the number symbols as you go along.
6. Start at 800 000 and count backwards in six thousands until you reach 740 000. Write the number symbols as you go along.
7. The seven numbers below are all bigger than 600 000 but smaller than 700 000. Arrange these numbers in ascending order:
   641 245 662 786 680 901 646 091
   656 488 673 168 637 173
8. The seven numbers below are all bigger than 900 000 but smaller than 1 000 000. Arrange these numbers in descending order:
   928 028 953 156 999 820 941 783
   927 891 945 678 996 788
9. In each case, decide whether the first number is bigger than, smaller than or equal to the second number. Then write the two numbers with the < or > or = sign between the numbers.
   Examples: 63 372 < 64 372; 45 871 > 20 200; 17 081 = 17081
   (a) 63 372 and 63 002 (b) 86 762 and 68 872
   (c) 27 901 and 28 817 (d) 35 530 and 53 305
   (e) 390 860 and 390860 (f) 701 847 and 710 874
Grade 5 Term 2 Unit 2 Whole numbers: Addition and subtraction

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**Mathematical background**

The format below, which was introduced in Term 1 for 4-digit numbers, is used for addition and subtraction with 5-digit numbers in this unit. It provides a bridge towards adding and subtracting in columns, which is introduced in Term 3.

\[
\begin{align*}
34\,687 + 23\,365 + 18\,435 & = 30\,000 + 4\,000 + 600 + 80 + 7 \\
34\,687 & = 30\,000 + 4\,000 + 600 + 80 + 7 \\
23\,365 & = 20\,000 + 3\,000 + 300 + 60 + 5 \\
18\,435 & = 10\,000 + 8\,000 + 400 + 30 + 5 \\
\text{Total} & = 60\,000 + 15\,000 + 1\,300 + 170 + 17 \\
& = 70\,000 + 6\,000 + 400 + 80 + 7 \\
& = 76\,487 \\
73\,456 - 26\,879 & = 70\,000 + 3\,000 + 400 + 50 + 6 \\
& = 60\,000 + 12\,000 + 1\,300 + 140 + 16 \\
26\,879 & = 20\,000 + 6\,000 + 800 + 70 + 9 \\
73\,456 - 26\,879 & = 40\,000 + 6\,000 + 500 + 70 + 7 \\
& = 46\,577 \\
\end{align*}
\]

Understanding the replacements, shown in red, in the second last step of addition and the second step of subtraction is critical to understanding the “break down, rearrange and build up” methods of addition and subtraction.
2.1 Facts and skills for addition and subtraction

Teaching guidelines
This whole section (questions 1 to 15) is about Mental Mathematics.

Questions 1 to 10 are intended to develop skill in using number facts for small numbers to form number facts for bigger numbers (multiples of 10, 100 and 1 000).

Question 3(c) forces learners to think of each single bottle as 1 000 ml. Experiences like this may help to protect learners against losing awareness of place value when they start to record calculations in columns later in the year (see “Possible misconceptions” on the next page).

Answers
1. Answers will differ. Possible examples are:
   (a) 25 to 30 ml
   (b) Approximately 20 mouthfuls
   (c) Approximately 15 000 ml
2. (a) 3 000 ml
   (b) 40 000 ml
3. (a) 30 bottles
   (b) 50 bottles
   (c) 80 000 ml
Possible misconceptions
When learners start to record calculations in the vertical column format, they may easily lose sight of the actual meanings (place values) of the digits in the tens, hundreds, thousands and ten thousands columns. When recording their work in columns as shown below, learners may think as described in the bubbles and lose sight of the actual magnitude of the numbers. We may refer to this as **loss of awareness of place value**.

5 + 3 = 8

\[ \begin{array}{c}
5 & 2 & 3 & 6 \\
+ & 3 & 2 & 4 & 3 \\
\hline
8 & 4 & 7 & 9
\end{array} \]

There is nothing wrong about using knowledge of number facts for single-digit numbers to produce facts about multi-digit numbers, for example to utilise the knowledge that 5 + 3 = 8 to claim that 5 000 + 3 000 = 8 000. However, it is bad if learners become completely unaware of the fact that they are actually engaging with 5 000 and 3 000 when they just think of 5 + 3 to produce the “8” in the answer 8 479 for the calculation shown above. They should rather have the actual numbers in mind, as shown below.

\[ \begin{array}{c}
5 & 0 & 0 & 0 \\
+ & 3 & 0 & 0 & 0 \\
\hline
8 & 0 & 0 & 0
\end{array} \]

\[ \begin{array}{c}
5 & 2 & 3 & 6 \\
+ & 3 & 2 & 4 & 3 \\
\hline
8 & 4 & 7 & 9
\end{array} \]

\[ \begin{array}{c}
2 & 0 & 0 \\
+ & 2 & 0 & 0 \\
\hline
4 & 0 & 0
\end{array} \]

\[ \begin{array}{c}
6 & 3 \\
\hline
9
\end{array} \]

\[ \begin{array}{c}
3 & + & 4 = 7
\end{array} \]

\[ \begin{array}{c}
5 000 + 3 000 = 8 000
\end{array} \]

\[ \begin{array}{c}
6 + 3 = 9
\end{array} \]

\[ \begin{array}{c}
3 + 4 = 7
\end{array} \]

\[ \begin{array}{c}
200 + 200 = 400
\end{array} \]

\[ \begin{array}{c}
5 236
\end{array} \]

\[ \begin{array}{c}
3 243
\end{array} \]

\[ \begin{array}{c}
8 479
\end{array} \]

\[ \begin{array}{c}
30 + 40 = 70
\end{array} \]

Answers
4. (a) 70 000 ml (b) 90 000 ml
   (c) 60 000 (d) 40 200
   (e) 42 000 (f) 70 700
5. How much is each of the following?
   (a) 40 000 + 20 000 (b) 40 000 + 200
   (c) 40 000 + 2 000 (d) 20 300 + 50 400
6. This line is 100 mm long.
   (a) How many lines like this do you have to put next to each other to get 1 m?
   (b) How many millimetres are there in 1 m?
   (c) How many millimetres are there in 5 m?
   (d) How many millimetres are there in 10 m?
   (e) How many millimetres are there in 15 m?
   (f) How many millimetres are there in 63 m?
7. How many mm long are all these lines together?
   1 100 mm
8. 34 m = 34 000 mm
   How many millimetres are each of the following?
   (a) 20 m + 30 m (b) 4 m + 5 m
   (c) 24 m + 35 m (d) 25 m + 34 m
   (e) 42 m + 43 m (f) 37 m + 56 m

122 UNIT 2: WHOLE NUMBERS: ADDITION AND SUBTRACTION
Mathematical notes

Filling up to the nearest multiple of ten, hundred, thousand, etc. is an important mental mathematics technique. The tinted passage indicates how thinking of the number line can support the mental application of this technique.

Answers

9. (a) 80 ℓ
   (b) 50 000 ml

10. (a) 20 000
    (b) 35 000

11. (a) 15 000 + ? → 20 000 + ? = ?
    15 000 + 5 000 → 20 000 + 3 000 = 23 000
    (b) 57 000 + ? → 60 000 + ? = ?
        57 000 + 3 000 → 60 000 + 4 000 = 64 000
    (c) 85 000 + ? → 90 000 + ? = ?
        85 000 + 5 000 → 90 000 + 10 000 = 100 000
    (d) 36 000 + ? → 40 000 + ? = ?
        36 000 + 4 000 → 40 000 + 6 000 = 46 000
    (e) 69 500 + ? → 70 000 + ? = ?
        69 500 + 500 → 70 000 + 300 = 70 300

9. There is 80 000 ml of milk in a container.
   (a) How many litres of milk is this?
   (b) How many millilitres of milk are left in the container if 30 000 ml of milk is taken out to fill bottles?

10. Calculate each of the following.
    (a) 3 000 + 5 000 + 8 000 + 4 000
    (b) 13 000 + 5 000 + 4 000 + 6 000 + 7 000

You can have a picture like this in your mind to work out how much 35 000 + 8 000 is:

You do not have to draw a number line when you think about it. You may describe your thinking like this:

35 000 + ? → 40 000 + ? = ?
8 000 in total

11. Use question marks and arrows as it is done in the example above, to describe the thinking shown in each of these number line diagrams. Then solve your number sentences.
**Teaching guidelines**

The tinted passage describes two subtraction facts that can be formed if an addition fact is known. It serves as an example for question 12.

As an introduction to question 12, you may demonstrate that the diagram in question 11(a) on page 123 of the Learner Book represents the addition fact $15 000 + 8 000 = 23 000$, and ask learners whether this helps them to know what the answers for $23 000 - 8 000$ and $23 000 - 15 000$ are.

**Notes on questions**

Question 13 provides learners with an opportunity to test their own knowledge and skill with respect to mental mathematics as regards adding and subtracting multiples of 1 000 in the domain 1 000 to 100 000.

Explain to learners that they should identify the number sentences for which they cannot give the answers quickly, and write them down without taking time to find the answers. Once they have worked through question 13 in this way, they should do question 14.

You may let learners repeat question 13 after they have finished question 14. They may then check whether they are now able to find more of the answers immediately.

Learners should try to do question 15 with as little writing as possible, but they should write down the answers. You may let them do question 15 for a second time once they have finished and check whether they get the same answers as before. In cases where they get different answers, they should do the calculations again until a consistent answer is obtained.

**Answers**

12. (a) $23 000 - 8 000 = 15 000$
   (b) $64 000 - 7 000 = 57 000$
   (c) $100 000 - 15 000 = 85 000$
   (d) $46 000 - 10 000 = 36 000$
   (e) $70 300 - 800 = 69 500$

13. to 15. See the next page.
**Answers (continued)**

<table>
<thead>
<tr>
<th>Question</th>
<th>Calculation</th>
<th>Answer</th>
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<td>13.</td>
<td>10 000 + 5 000 = 15 000</td>
<td>15 000</td>
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<tr>
<td></td>
<td>5 000 + 9 000 = 14 000</td>
<td>14 000</td>
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<td></td>
<td>5 000 + 12 000 = 17 000</td>
<td>17 000</td>
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<tr>
<td></td>
<td>19 000 - 7 000 = 12 000</td>
<td>12 000</td>
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<td></td>
<td>17 000 + 8 000 = 25 000</td>
<td>25 000</td>
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<tr>
<td></td>
<td>57 000 + 8 000 = 65 000</td>
<td>65 000</td>
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<td></td>
<td>21 000 + 4 000 = 25 000</td>
<td>25 000</td>
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<td></td>
<td>4 000 + 39 000 = 43 000</td>
<td>43 000</td>
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<td></td>
<td>34 000 + 10 000 = 44 000</td>
<td>44 000</td>
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<td></td>
<td>31 000 + 9 000 = 40 000</td>
<td>40 000</td>
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<td></td>
<td>29 000 + 8 000 = 37 000</td>
<td>37 000</td>
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<td></td>
<td>27 000 + 18 000 = 45 000</td>
<td>45 000</td>
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<tr>
<td>14.</td>
<td>10 000 + 5 000 = 15 000</td>
<td>15 000</td>
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<td>5 000 + 9 000 = 14 000</td>
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<td>19 000 - 7 000 = 12 000</td>
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<td>17 000 + 8 000 = 25 000</td>
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<td></td>
<td>57 000 + 8 000 = 65 000</td>
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<td>21 000 + 4 000 = 25 000</td>
<td>25 000</td>
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<td></td>
<td>4 000 + 39 000 = 43 000</td>
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<td>34 000 + 10 000 = 44 000</td>
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<td>31 000 + 9 000 = 40 000</td>
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<td>29 000 + 8 000 = 37 000</td>
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<td></td>
<td>27 000 + 18 000 = 45 000</td>
<td>45 000</td>
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<tr>
<td>15.</td>
<td>68 788</td>
<td>(a) 68 788</td>
</tr>
<tr>
<td></td>
<td>45 387</td>
<td>(b) 45 387</td>
</tr>
<tr>
<td></td>
<td>65 774</td>
<td>(c) 65 774</td>
</tr>
<tr>
<td></td>
<td>77 778</td>
<td>(d) 77 778</td>
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<tr>
<td></td>
<td>65 324</td>
<td>(e) 65 324</td>
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<td></td>
<td>87 768</td>
<td>(f) 87 768</td>
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<td>87 768</td>
<td>(g) 87 768</td>
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<td></td>
<td>87 768</td>
<td>(h) 87 768</td>
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</tbody>
</table>

14. Learners do the remaining calculations from question 13.

15. Write each of the following as a single number.

(a) 50 000 + 18 000 + 700 + 60 + 28
(b) 40 000 + 4 000 + 1 300 + 80 + 7
(c) 60 000 + 3 000 + 2 700 + 60 + 14
(d) 4 000 + 300 + 30 000 + 40 + 3 + 40 000 + 3 000 + 5 + 30 + 400
(e) 80 000 - 300 + 7 000 + 50 - 5 + 600 - 30 - 2 000 + 9 - 20 000
(f) 30 000 + 4 000 + 200 + 30 + 2 + 50 000 + 3 000 + 500 + 30 + 6
(g) 50 000 + 30 000 + 4 000 + 3 000 + 500 + 200 + 30 + 30 + 6 + 2
(h) 4 000 + 30 + 500 + 30 000 + 3 000 + 200 + 2 + 50 000 + 6 + 30
2.2 Add and subtract 5-digit numbers

Teaching guidelines
Learners have used the methods described in the tinted passages in Term 1 already (Unit 3 Section 3.7), and extension to 5-digit numbers does not present any new conceptual challenge.

Demonstrate the examples in the tinted passages on the board, or use other examples if you wish, and let learners do questions 1 to 6.

Answers
1. (a) 87 015
   (b) 75 925
2. R74 691
3. (a) 57 592 + 53 922 = 111 514
   (b) 62 412 + 49 102 = 111 514
   (c) 41 038 + 70 476 = 111 514
4. Learners check their answers for question 3 and correct their mistakes.
5. (a) 31 440 + 4 716 = 36 156
   (b) 22 611 + 13 545 = 36 156
   (c) 91 633 − 55 477 = 36 156
6. Learners check their answers for question 5 and correct their mistakes.
Teaching guidelines
Subtraction that requires replacement of the expanded form of the larger number is
difficult work for some learners and it requires thorough teaching.

Demonstrate the examples in the tinted passage on the board. Emphasise the idea of
replacing the expanded notation of the larger number with a breakdown into parts that will
make the subtraction easy.

Answers
7. (a) $31000 + 3284 = 34284$
    (b) $21895 + 12389 = 34284$
    (c) $90917 - 56633 = 34284$

A plan needs to be made when there is not enough to subtract from,
as in the above case.

One plan is to think of 73 456 as 70 000 + 3 456 and to transfer 1 from
the 70 000 to the 3 456.

In this way 73 456 is replaced by 69 999 + 3 457.

You can then subtract 26 879 from 69 999, and add the 3 457 back
afterwards:

$69999 = 60000 + 9000 + 900 + 90 + 9$
$26879 = 20000 + 6000 + 800 + 70 + 9$
$69999 - 26879 = 40000 + 3000 + 100 + 20 + 0$
$= 43120$

So, 73 456 - 26 879 = 43 120 + 3 457 which is 46 577.

In this method you thus first change to an easier number to subtract
from, then you add to the answer to compensate for the change you
made.

A different plan is to replace 70000 + 3000 + 400 + 50 + 6 by
60000 + 12000 + 1300 + 140 + 16:

$73456 = 70000 + 3000 + 400 + 50 + 6$
$= 60000 + 12000 + 1300 + 140 + 16$
$26879 = 20000 + 6000 + 800 + 70 + 9$
$73456 - 26879 = 40000 + 6000 + 500 + 70 + 7$
$= 46577$

This is called the transfer method of subtraction. In the past it was
called the borrowing method.

7. Do the calculations in brackets first, then add the answers.
   (a) $(54764 - 23764) + (36153 - 32869)$
   (b) $(54764 - 32869) + (36153 - 23764)$
   (c) $(54764 + 36153) - (32869 + 23764)$
Notes on questions

Questions 10 and 12 serve a twofold purpose:

- practice in addition and subtraction
- developing awareness of properties of operations.

Once learners have completed question 10, you may tell them that they should have obtained the same answers for (a), (c) and (d). Those who have not should do the calculations again. The answer for (b) is different. The four calculation plans demonstrate that additions can be performed in any order, and that subtraction is not commutative.

In question 12 all three calculation plans have the same answer.

Answers

8. Learners check their answers for question 7 and correct their mistakes.

9. (a) 30 592  (b) 94 146  (c) 71 703  (d) 52 821
   (e) 111 110  (f) 122 211  (g) 106 062  (h) 104 949
   (i) 32 045  (j) 18 072  (k) 25 783  (l) 26 937

10. Learners write down which calculations they expect will have the same answer. (In fact, (a), (c) and (d) have the same answer.)

11. (a) 59 476  (b) 39 880  (c) 59 476  (d) 59 476

12. Learners write down which calculations they expect will have the same answer. (In fact, they all have the same answer.)

13. (a) 28 493  (b) 28 493  (c) 28 493

14. (a) 14 717  (b) 38 891  (c) 121 671
   (d) 50 000  (e) 52 966

8. If your answers for 7(a), (b) and (c) are not the same, you have made a mistake. If that is the case, correct your mistake.

9. Calculate:
   (a) 89 324 – 58 732
e 51 592
   (b) 50 130 + 44 016
   (c) 91 265 – 19 562
   (d) 23 481 + 29 340
   (e) 98 765 + 12 345
   (f) 54 321 + 67 890
   (g) 75 849 + 30 213
   (h) 65 748 + 39 201
   (i) 60 073 – 28 028
   (j) 30 314 – 12 242
   (k) 62 891 – 37 108
   (l) 59 832 – 32 895

10. You will do the following calculations later. You will do the calculations from left to right. Which of these do you expect to have the same answers?
   (a) 49 678 + 33 547 – 23 749
   (b) 49 678 – 33 547 + 23 749
   (c) 49 678 – 23 749 + 33 547
   (d) 33 547 – 23 749 + 49 678

11. Do the calculations in question 10.

12. You will do the following calculations later. You will do the calculations from left to right. Which of these do you expect to have the same answers?
   (a) 69 346 + 23 458 – 45 735 – 18 576
   (b) 69 346 – 45 735 + 23 458 – 18 576
   (c) 69 346 – 18 576 + 23 458 – 45 735

13. Do the calculations in question 12.

14. (a) What is the difference between 37 526 and 22 809?
   (b) Work out the sum of 36 127, 1 786 and 978.
   (c) What number is 43 606 more than 78 065?
   (d) Add 37 349 to 53 782 and subtract 41 131 from the answer.
   (e) What number must be added to 35 409 to make 88 357?
2.3 Apply your knowledge

Teaching guidelines
When engaging with word problems, it is critical that learners read the question carefully and try to imagine the described situation in their minds, before they decide on an operation. A good way to nudge learners towards reading and interpreting the given problem is to encourage them to produce an estimated answer first, before they start doing accurate calculations or even decide on what calculations they will do.

Learners’ efforts should be directed at understanding and solving the stated problem, not at trying to identify the correct operation as quickly as possible and applying a recipe to execute it.

Answers
1. (a) R40 000
   (b) R42 485
2. 7 246 m
3. 61 182 houses
4. R32 877
5. 46 936 voters
6. 10 777 people
7. 1 769 lone bulls
8. R68 184
Grade 5 Term 2 Unit 3
Common fractions

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CAPS time allocation
5 hours

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16 and 160 to 162

Mathematical background
It is widely assumed that fractions were invented to aid accurate measurement in cases where the commonly used standard unit of measurement could not provide an exact description of a quantity. This is reflected in the Latin names of some of our current units of measurement, for example centimetres (hundredths of a metre) and millimetres (thousandths of a metre).

If the brown strip below is measured with the yellow strip as a unit, its length is 3 and 3 fifths of the yellow unit.

This example shows how fractions are used as measures.

Mathematically, the fraction concept is very important to the understanding of decimals, because the place value parts after the decimal comma are fractions. For example, the expanded notation for the number 23,47 is \(20 + \frac{3}{10} + \frac{4}{100} + \frac{7}{1000}\) or tens + 3 units + 4 tenths + 7 hundredths.

Fractions are also used to describe parts of collections and parts of non-physical quantities, for example “3 eighths of the learners in a school” or “63 hundredths of the available marks”. In a case like the latter, the percentage notation (\% for hundredths) is commonly used, namely 63%.

In everyday life and language certain fractions, such as “half” and “quarter”, are sometimes used to indicate approximate parts of whole objects. People may, for example, refer to “a quarter of an apple” or “half a loaf of bread”. Although this everyday use of fraction language differs from the mathematical use in the sense that the fraction words are not used to indicate precise parts, the everyday use provides a starting point for learning about fractions.

A fraction is a number of exactly equal parts of the same object or measurement unit, for example 7 eighths of a cake or 7 hundredths of a metre.
3.1 Dividing into fraction parts

**Critical knowledge**

It is terribly important that learners use appropriate, correct language for fractions. They should say and sometimes also write the names of fractions in words. Describing a fraction as “one number over another number”, for example $\frac{3}{5}$ as “3 over 5”, should be strongly discouraged. Fractions are not about two whole numbers. This language usage undermines understanding of a fraction as a number of parts of a given size. The correct name for $\frac{3}{5}$ is “3 fifths”. You should consistently encourage learners to say the fraction names: “fifths”, “sixths”, “tenths”, etc.

It is for this reason that we have chosen to write the names of fractions and fraction parts without a hyphen between the numerator and the denominator (e.g. “two thirds” instead of “two-thirds”). It is also why we often use number symbols instead of the number names as numerators (e.g. “3 twenty-fifths” or “2 thirds”). You should, however, not penalise learners who choose to spell fraction names with hyphens; that is, if they write “one-third”, “two-fifths”, three-eighths”, etc. It is grammatically correct to do so.

**Teaching guidelines**

Discuss the issue of fraction parts of loaves of bread being only approximate. The artist (and a bread cutting machine) cannot give us perfectly equal parts of a loaf.

**Possible misconceptions**

Fraction language is sometimes used in everyday life to refer to approximate parts. For example, when people refer to a quarter of an apple it is seldom exactly a quarter and, in any case, apples differ in shape and size. While the everyday use of fraction language is useful as a starting point for developing knowledge of fractions, it may weaken the understanding of the mathematical meaning of fractions as exact fractional parts of wholes, collections, quantities and units of measurement.

For example, in the circle alongside, each part is not equal to a third of the circle because the three parts are not the same size.

The above also applies to the context of bread used in the Learner Book; hence the pictures of parts of loaves are accompanied by fraction strips, which show exact partitions of a whole. You can point this out to the class.

**Answers**

1. (a) one tenth; $\frac{1}{10}$  
(b) one quarter / one fourth; $\frac{1}{4}$
**Critical knowledge and skills**

Learners must be able to represent fractions diagrammatically by drawing fraction strips, as shown at the top of page 130 of the Learner Book. Note that these are not drawn with a ruler. Learners should be able to make such drawings quickly, drawing freehand so that it does not take up too much time. This will provide them with a tool to help them think what fractions really mean when working on tasks involving fractions. It is extremely important though, that learners do not spend much time on drawing fraction strips accurately. Such strips are usually not used for measuring. They are only there to support learners’ conceptual thinking about fractions.

When drawing fraction strips, it is best if learners initially draw the whole strip, so that they can physically experience the partitioning of the whole strip into equal parts afterwards. This physical experience of partitioning can support their understanding of fractions as the numbers that describe the size of parts of wholes.

**Drawing a fraction strip:** When drawing a fraction strip for an even number of parts it helps to first draw the line that separates the whole strip into two halves. For quarters, eighths, sixteenths, etc., one can then continue to halve the sections, as shown below on the left. For a number of parts that is an uneven number and multiple of three (e.g. 9, 15, etc.), the first step could be to draw two lines to divide the whole strip approximately into thirds, as shown below in the middle. Drawing a fifths strip is slightly more difficult. It helps to draw a line that divides the whole strip into two parts, with the one part about one-and-a-half times as long as the other, as shown below on the right. You can quickly demonstrate this on the board:

1. **To draw quarters:**
2. **To draw ninths:**
3. **To draw fifths:**

**Answers**

2. (a) one eighth; \(\frac{1}{8}\)
(b) one seventh; \(\frac{1}{7}\)
(c) one ninth; \(\frac{1}{9}\)
(d) one eleventh; \(\frac{1}{11}\)

3. (a) six tenths; \(\frac{6}{10}\)
(b) three tenths; \(\frac{3}{10}\)

Diagrams like these are called **fraction strips**.

The strip on the left shows what we mean by sixths.
The strip on the right shows what we mean by twelfths.

2. In each case below, draw a fraction strip. Write down what we call each part, and also write this in fraction notation.
   (a) A loaf of bread, or some other object, is cut into eight equal pieces.
   (b) An object is cut into seven equal pieces.
   (c) An object is cut into nine equal pieces.
   (d) An object is cut into eleven equal pieces.

This loaf of bread is cut into ten equal slices.
The picture below shows 7 tenths of the loaf.

We can write 7 tenths as \(\frac{7}{10}\).

3. What part of the loaf of bread above is shown in each of the pictures below? Give your answer in words and in fraction notation, and also draw a rough fraction strip in each case.
   (a)
   (b)
Notes on questions
When a whole is divided into equal parts, there are three quantities involved:

- the number of parts
- the size of each part
- the size of the whole.

In questions 4, 5 and 6 the size of the whole and the number of parts are given. Learners have to state the size of each part. These are sharing situations.

Note that question 6(b) is a bit tricky: 3 loaves of bread (not one) are shared between 12 people, so each person gets one quarter of the three loaves. The question is really about what part of one loaf each person gets. It is one quarter.

Question 7 is quite different. In each case the size of the whole and the size of each part are given, and learners have to determine the number of equal parts. These are grouping situations. The number of equal parts is the same as the number of children or people.

Answers
4. (a) 15; one fifteenth
   (b) 18; one eighteenth
   (c) 24; one twenty-fourth
5. (a) one twenty-fifth / \(\frac{1}{25}\)
   (b) one fourteenth / \(\frac{1}{14}\)
   (c) one seventh / \(\frac{1}{7}\)
6. (a) one fifth / \(\frac{1}{5}\)
   (b) one quarter / \(\frac{1}{4}\)
7. (a) 8 children
   (b) 15 people
3.2 Work with fraction parts

**Teaching guidelines**

Questions 5, 6 and 7 on page 134 provide learners with opportunities to refresh and consolidate their understanding of equivalent fractions. At least one full lesson period, and preferably two, is required for questions 5, 6 and 7.

Question 1 is very suitable to practise understanding of fractions. Instruct learners to write their answers in words as well as in fraction notation. Whether this is done at home or in class, it is a good idea to ask learners to do the work on loose sheets of paper and hand them in. Analyse the correctness of learners' responses carefully to obtain an assessment of learners' current state of knowledge of fractions. This is **formative assessment** and will guide your teaching.

Once learners have handed in their answer sheets for question 1, you may divide the class into smaller groups. Ask them to do the questions again and to compare their answers. This will provide learners with opportunities to talk about fractions and to say the names of fractions aloud. Doing this exercise may really strengthen their understanding of fractions.

However, it is important that you encourage them to say the proper fraction names, for example “seven tenths”, and not the meaningless and unsound “seven over ten”. Fractions are not made of whole numbers written one over the other. This can lead to a **misconception** of fractions, and later to mistakes such as adding the numerators and adding the denominators when adding fractions. We are trying to avoid leading learners into this trap.

**Answers**

1. (a) three sevenths / \(\frac{3}{7}\)  
   (b) three tenths / \(\frac{3}{10}\) 
   (c) six tenths / \(\frac{6}{10}\)  
   (d) three fifths / \(\frac{3}{5}\)  
   (e) three quarters / \(\frac{3}{4}\)  
   (f) six eighths / \(\frac{6}{8}\)  
   (g) eight twentieths / \(\frac{8}{20}\)  
   (h) four tenths / \(\frac{4}{10}\)  
   (i) two fifths / \(\frac{2}{5}\)  
   (j) six fifteenths / \(\frac{6}{15}\)
Possible misconceptions
As was pointed out on the previous page, learners sometimes think that fractions consist of whole numbers written one over the other. This is quite wrong. The number below the line tells us how many parts there are in the whole and the number above the line tells us how many of these parts we have. If learners get that right in Grade 5, it will have a positive effect in other parts of the curriculum, and also in later grades.

Notes on questions
The tinted passage and questions 2 and 3 serve as a gentle introduction to adding fractions. You may ask learners to read the tinted passage and share what they understand with classmates in small groups, and then proceed to do questions 2 and 3. Note that learners who give $\frac{5}{2}$ of a loaf as an answer to 3(b) should be made aware that this is also equal to 1 whole loaf of bread.

Question 4 is different to the other questions. It is not difficult, but it may enrich the way learners conceptualise fractions.

Answers
2. (a) $\frac{5}{10} + \frac{3}{10} = \frac{8}{10}$ of a loaf
   (b) $\frac{2}{10} + \frac{4}{10} = \frac{6}{10}$ of a loaf
3. (a) $\frac{3}{5}$ of a loaf + $\frac{2}{5}$ of a loaf = $\frac{5}{5}$ of a loaf
   (b) $\frac{2}{5}$ of a loaf + $\frac{3}{5}$ of a loaf = 1 whole loaf
4. (a) 4 loaves  
   (b) 10 loaves  
   (c) 2 loaves
Notes on questions
Questions 5, 6 and 7 are intended to consolidate learners’ awareness of equivalent fractions.

Question 7 is designed to provide you with an opportunity to bring some closure to the development of the idea of equivalent fractions in learners’ minds. There are clearly three good answers for question 7(a):

- 4 twentieths
- 1 fifth
- 1 fifth, which is the same as 4 twentieths.
(The third answer may be phrased in different ways.)

Ask some learners to state their answers in class. After one answer you may ask whether someone has a different answer. Write the given answers on the board. You may take a “vote” on the three answers and write the results of the vote on the board. Do not make any judgement on the relative merit of the three answers, because that may result in learners terminating their own reflections. Reflections strengthen their understanding of equivalent fractions.

Some learners may change their minds once they have seen all three answers, as a result of reflecting on the situation and the given answers. Allow a second round of voting to provide a vehicle for learners to express their realisation that 1 fifth of a loaf is the same amount of bread as 4 twentieths of a loaf.

Question 7(b) provides for assessment of learners’ concept of equivalent fractions at this stage.

Answers

5. (a) 2 eighths / $\frac{2}{8}$
   (b) 4 eighths / $\frac{4}{8}$
   (c) 6 eighths / $\frac{6}{8}$

6. (a) 1 twentieth / $\frac{1}{20}$
   (b) 5 slices
   (c) 5 twentieths / $\frac{5}{20}$
   (d) 10 twentieths / $\frac{10}{20}$
   (e) 15 twentieths / $\frac{15}{20}$

7. (a) one fifth / $\frac{1}{5}$
   (b) $\frac{1}{5}$ and $\frac{4}{20}$ of the loaf are exactly the same.
3.3 Measure with fractions of a unit

Mathematical notes
Understanding fractions as parts of units of measurement is profoundly important. It provides the conceptual basis for learners' understanding of decimal fractions, which is addressed in Grade 6. The use of fractional units of measurement also provides an empowering context for understanding equivalent fractions, in the sense that the same length (or other quantity) can be expressed in different ways in terms of fractional parts of measurement units. As mentioned before, fractions were probably invented to aid accurate measurement in cases where the commonly used standard unit of measurement could not provide an exact description of a quantity.

Answers
1. (a) one fifth  (b) one sixth

Mathematical notes
Learners easily come to understand fractions as physical objects (or names for physical objects), which is wrong. A fraction is a number that can be used to describe the size of an object in terms of a formal or informal measurement unit, which may be another object.

For example, in the statement “Mary eats three eighths of a loaf of bread”, a whole loaf of bread serves as the unit of measurement. The statement is very similar to “Mary eats three eighths of a kilogram of porridge”, in which an “official” unit of measurement, the kilogram, is used. In the statement “Mary eats three eighths of a cake that Paul baked”, the specific cake that Paul baked serves as the unit of measurement. It is an informal unit.

A fraction can also be used to compare two quantities by expressing the one quantity as a fraction of the other quantity. For example, to compare the numbers 12 and 18 one may describe 12 as two thirds of 18. Clearly this is not a physical object, it is a relationship.

Two quantities can also be compared by stating how many repetitions of the one quantity are equal to a specified number of repetitions of the other quantity. For example, 3 ℓ of oil may have the same mass as 2 ℓ of water. This fact may also be expressed by using a fraction, namely by saying that the density of oil is 2 thirds the density of water. The fraction 2 thirds is here used to express the ratio 2 : 3. Density is an abstract quality.
Mathematical notes
It is useful to distinguish three phases in the development of the concept of equivalent fractions in learners’ minds:

• Awareness that the same part of a whole (collection, quantity, unit of measurement) can be described with different fractions (see Ruler A and Ruler B in question 4).
• The ability to specify equivalent fractions by looking at diagrams such as fraction strips.
• Producing equivalent fractions with a formula – this is not done at all in the Intermediate Phase because premature learning of the formula before the concept is strongly formed may inhibit understanding of what equivalent fractions are. So, no formulas are to be taught. The learners are to form their own concepts.

Notes on questions
Questions 4 and 5 provide a lead into the concept of equivalent fractions.

Teaching guidelines
Discuss the fact in class that the same length can be described in different ways, especially with reference to question 5. They already know what Ruler A and Ruler B are called.

Answers
2. one and six tenths of a Brownstick long; $1\frac{6}{10}$ Brownsticks
3. one and two sixths of a Brownstick long; $1\frac{2}{6}$ Brownsticks
4. Ruler A: one and six tenths of a Brownstick long; $1\frac{6}{10}$ Brownsticks
   Ruler B: one and three fifths of a Brownstick long; $1\frac{3}{5}$ Brownsticks
5. (a) Ruler C is a twentieths-ruler.
   (b) 12 twentieths; $\frac{12}{20}$
   (c) 12 twentieths; $\frac{12}{20}$

Write your answers to questions 2 to 7 in words and in symbols. In some of the questions you may be able to state the length in two different ways.

2. How long is this red strip?

3. How long is this blue strip?

4. How long is this yellow strip?

Ruler A above is called a tenths-ruler because it is marked in tenths of a Brownstick.
Ruler B is called a fifths-ruler because it is marked in fifths of a Brownstick.

5. (a) What can we call Ruler C below?
   (b) How many twentieths of a Brownstick is the same length as 6 tenths of a Brownstick?
   (c) How many twentieths of a Brownstick is the same length as 3 fifths of a Brownstick?
Critical knowledge
It is critical that learners understand that equivalent fractions are different, but they represent the same quantities.

Equivalent fractions are different ways to represent the same quantity, or the same part of a whole or a collection.

Answers
6. Ruler D: one and nine twelfths of a Brownstick long; $1 \frac{9}{12}$ Brownsticks
   Ruler E: one and six eighths of a Brownstick long; $1 \frac{6}{8}$ Brownsticks
7. Ruler F: one and three quarters of a Brownstick long; $1 \frac{3}{4}$ Brownsticks
   Ruler C: one and fifteen twentieths of a Brownstick long; $1 \frac{15}{20}$ Brownsticks

Teaching guidelines
Go through the definition of equivalent fractions, and the meaning of “equi-.” Read the tinted sentence, but do not attempt to explain the mathematics. The class has just experienced the truth of the statement in questions 6 and 7, and that is sufficient (until Grade 7).

8. (a) $\frac{1}{4} \ell$ milk $> \frac{1}{5} \ell$ milk  (b) $\frac{1}{4} \ell$ milk $= \frac{2}{8} \ell$ milk
   (c) $\frac{3}{10} \ell$ milk $< \frac{3}{8} \ell$ milk  (d) $\frac{2}{5} \ell$ milk $= \frac{8}{10} \ell$ milk

9. (a) 250 ml $> 200$ ml  (b) 250 ml $= 250$ ml
   (c) 300 ml $< 375$ ml  (d) 800 ml $= 800$ ml
3.4 Compare and order fractions

Mathematical notes
A “fraction wall” is a collection of fraction strips placed directly one below the other. It is not a mathematical idea, just a teaching/learning aid.

Teaching guidelines
Learners do not need to use the given diagrams; they can also draw their own fraction strips for each question.

Notes on questions
In question 1, the same mass is expressed as different but equivalent fractions.

Question 2 provides a way to focus on the fact that a bigger number as denominator means a smaller fraction. A big number as denominator means that the whole is divided into many and hence very small parts.

The fractions in question 3 are what remains of wholes if the fractions in question 2 are removed.

Questions 2 and 3 relate to the fraction wall.

Questions 4(a) and (b) do not require any calculation. However, it is necessary to compute the answer for (c) because the real values are needed to be able to answer the question. The fractions aren’t easily relatable. The answer is 250 ml for both.

Answers
1. (a) $\frac{6}{8}$ kg copper  (b) $\frac{3}{8}$ kg copper  (c) $\frac{5}{8}$ kg copper
   (d) $\frac{9}{15}$ kg copper = $\frac{3}{5}$ kg copper  (e) $\frac{8}{12}$ kg copper = $\frac{2}{3}$ kg copper
   (f) $\frac{13}{15}$ kg copper  (g) $\frac{8}{10}$ kg copper = $\frac{12}{15}$ kg copper
2. $\frac{1}{12}$; $\frac{7}{11}$; $\frac{1}{10}$; $\frac{1}{8}$; $\frac{1}{7}$; $\frac{1}{6}$; $\frac{1}{5}$; $\frac{1}{4}$; $\frac{1}{3}$; $\frac{1}{2}$
3. $\frac{1}{2}$; $\frac{2}{7}$; $\frac{3}{4}$; $\frac{5}{5}$; $\frac{6}{7}$; $\frac{7}{8}$; $\frac{8}{9}$; $\frac{9}{10}$; $\frac{10}{11}$; $\frac{11}{12}$
4. (a) $\frac{2}{5}$ of 1 ℓ of milk  (b) $\frac{2}{5}$ of 1 ℓ of milk
   (c) $\frac{1}{3}$ of 750 ml of milk = $\frac{1}{2}$ of 500 ml of milk
**Possible misconceptions**

Again note that there is a dangerous misconception that is often accompanied by the misleading habit of referring to a fraction as “one number over another number”, for example reading \( \frac{2}{3} \) as “two over three”. The misconception is that the numerator and denominator are two numbers that have similar meanings. This misconception is probably why learners make the error of adding the numerators and adding the denominators when adding fractions.

**Teaching guidelines**

The tinted passage at the bottom of page 139 is specifically phrased to combat the above misconception. Discuss it thoroughly in class. The denominator is the name of the fraction. (The Latin word *nomen* means name.)

**Answers**

5. There are a number of possibilities, of which the following are the most likely to be suggested:
   - (a) \( \frac{1}{2} = \frac{2}{4} = \frac{3}{6} = \frac{5}{10} = \frac{6}{12} \)
   - (b) \( \frac{1}{3} = \frac{2}{6} = \frac{3}{9} = \frac{4}{12} \)
   - (c) \( \frac{1}{4} = \frac{2}{8} = \frac{3}{12} = \frac{5}{20} \)
   - (d) \( \frac{1}{5} = \frac{2}{10} = \frac{3}{15} = \frac{4}{20} \)

Ask the class whether they see any patterns in their answers.

6. Several possibilities, e.g.
   - (a) \( \frac{4}{5} = \frac{12}{15} = \frac{8}{10} \)
   - (b) \( \frac{2}{3} = \frac{10}{15} = \frac{4}{6} \)
   - (c) \( \frac{8}{10} = \frac{3}{6} = \frac{4}{12} \)
   - (d) \( \frac{8}{20} = \frac{12}{18} = \frac{4}{6} \)

7. Several possibilities, e.g.
   - (a) \( \frac{3}{5} < \frac{7}{10} ; \frac{2}{5} ; \frac{3}{4} \)
   - (b) \( \frac{5}{8} < \frac{7}{12} ; \frac{4}{5} ; \frac{3}{4} \)
   - (c) \( \frac{3}{4} < \frac{9}{16} ; \frac{4}{5} ; \frac{11}{12} \)
   - (d) \( \frac{7}{8} < \frac{9}{10} ; \frac{8}{9} ; \frac{11}{12} \)

8. Several possibilities, e.g.
   - (a) \( \frac{1}{5} > \frac{1}{10} ; \frac{2}{20} ; \frac{3}{15} \)
   - (b) \( \frac{3}{7} > \frac{1}{4} ; \frac{11}{25} ; \frac{1}{3} \)
   - (c) \( \frac{3}{4} > \frac{7}{10} ; \frac{3}{5} ; \frac{1}{2} \)
   - (d) \( \frac{3}{5} > \frac{1}{6} ; \frac{1}{5} ; \frac{3}{10} \)
3.5 Count in fractions on the number line

Possible misconceptions
The major and dangerous misconception that a fraction is not a single number but a combination of two numbers “above and below the line”, or “the numerator and the denominator”, is unfortunately widespread. The misconception is supported by

- premature introduction of the common fraction notation before the fraction concept is properly developed,
- insufficient experience in referring to fractions in terms of the actual fraction names, for example “five eighths”,
- the flawed misnaming of fractions as “a number over another number”, for example of 5/8 as “5 over 8” instead of “5 eighths”, and
- confusion between two uses of a horizontal line between two numbers.

Representing fractions on the number line is one way in which this misconception can be resisted. It supports the understanding of a fraction as a single number that occupies a specific position between other numbers (including whole numbers) on the number line.

Notes on questions
On measuring tapes, parts of the number symbols are often not printed to save space, for example... 80 90 100 10 20 30... instead of ... 80 90 100 110 120 130...

When answering the questions in this section, learners should preferably write the number symbols in full, as indicated in the answers below.

Answers
1. \( \frac{7}{5} \) or \( 1\frac{2}{5} \) Brownsticks long
2. (a) \( \frac{3}{5} \) (b) \( \frac{5}{5} \) or 1 (c) \( \frac{8}{5} \) or \( 1\frac{3}{5} \)
3. \( \frac{6}{5} = 1\frac{1}{5} \quad \frac{7}{5} = 1\frac{2}{5} \quad \frac{8}{5} = \frac{3}{5} \quad \frac{9}{5} = 1\frac{4}{5} \)
4. \( \frac{3}{4} \) or 1 \( \frac{4}{4} \) or 1 \( \frac{5}{4} \) or \( 1\frac{1}{4} \) \( \frac{6}{4} \) or \( 1\frac{2}{4} \) \( \frac{7}{4} \) or \( 1\frac{3}{4} \)
5. \( \frac{3}{6} \) \( \frac{4}{6} \) \( \frac{5}{6} \) \( \frac{6}{6} = 1 \) \( \frac{7}{6} = 1\frac{1}{6} \) \( \frac{8}{6} = \frac{13}{6} \) \( \frac{9}{6} = 1\frac{3}{6} \) \( \frac{10}{6} = \frac{14}{6} \) \( \frac{11}{6} = 1\frac{5}{6} \)
6. \( \frac{1}{10} \) \( \frac{2}{10} \) \( \frac{3}{10} \) \( \frac{4}{10} \) \( \frac{5}{10} \) \( \frac{6}{10} \) \( \frac{7}{10} \) \( \frac{8}{10} \) \( \frac{9}{10} \) \( \frac{10}{10} = 1 \) or 1 \( 1\frac{1}{10} \) \( 1\frac{2}{10} \) \( 1\frac{3}{10} \) \( 1\frac{4}{10} \) \( 1\frac{5}{10} \) \( 1\frac{6}{10} \) \( 1\frac{7}{10} \) \( 1\frac{8}{10} \) \( 1\frac{9}{10} \)
Notes on questions
For the purposes of this section, it makes no difference whether learners write, for example, \( \frac{18}{12} \), \( 1 \frac{6}{12} \) or \( 1 \frac{1}{2} \).

Answers
7. \[
\begin{align*}
\frac{1}{12} & \quad \frac{2}{12} & \quad \frac{3}{12} & \quad \frac{4}{12} & \quad \frac{5}{12} & \quad \frac{6}{12} & \quad \frac{7}{12} & \quad \frac{8}{12} & \quad \frac{9}{12} \\
\frac{10}{12} & \quad \frac{11}{12} & \quad \frac{12}{12} & \quad 1 & \quad \frac{1}{12} & \quad \frac{2}{12} & \quad \frac{3}{12} & \quad \frac{4}{12} & \quad \frac{5}{12} & \quad \frac{6}{12} & \quad \frac{7}{12} & \quad \frac{8}{12} & \quad \frac{9}{12} & \quad \frac{10}{12} & \quad \frac{11}{12} & \quad \frac{12}{12} \\
\frac{10}{12} & \quad \frac{11}{12} & \quad \frac{12}{12} & \quad 1 & \quad \frac{1}{12} & \quad \frac{2}{12} & \quad \frac{3}{12} & \quad \frac{4}{12} & \quad \frac{5}{12} & \quad \frac{6}{12} & \quad \frac{7}{12} & \quad \frac{8}{12} & \quad \frac{9}{12} & \quad \frac{10}{12} & \quad \frac{11}{12} & \quad \frac{12}{12} & \quad 2
\end{align*}
\]
8. \[
\begin{align*}
\frac{1}{8} & \quad \frac{2}{8} & \quad \frac{3}{8} & \quad \frac{4}{8} & \quad \frac{5}{8} & \quad \frac{6}{8} & \quad \frac{7}{8} & \quad \frac{8}{8} & \quad 1 & \quad \frac{1}{8} & \quad \frac{2}{8} & \quad \frac{3}{8} & \quad \frac{4}{8} & \quad \frac{5}{8} & \quad \frac{6}{8} & \quad \frac{7}{8} & \quad \frac{8}{8} & \quad 2 & \quad \frac{1}{8} & \quad \frac{2}{8} & \quad \frac{3}{8} & \quad \frac{4}{8} & \quad \frac{5}{8} & \quad \frac{6}{8} & \quad \frac{7}{8} & \quad \frac{8}{8} & \quad 3
\end{align*}
\]
9. (a) \( \frac{1}{7} \)  (b) \( \frac{6}{7} \)  (c) \( \frac{22}{7} \)
    (d) \( \frac{3}{5} \)  (e) \( \frac{11}{5} \)  (f) \( 2 \)

3.6 Solve problems

Teaching guidelines
Do not require learners to read and interpret question 1 themselves. Rather tell them that Mrs Faku has \textit{a pile of cookies} and that she hands out all the cookies to her two sons, in the way described.

Then ask them what part of the cookies the older son gets, and what part the younger son gets, \textit{but do not allow learners to give public answers in class}. It is critical that each learner has the opportunity to engage individually with this question, which allows the formation of some intuitive understanding of ratio.

Answers
1. (a) Older son: \( \frac{2}{3} \); younger son: \( \frac{1}{3} \)
    (b) 24 and 12 cookies respectively
2. Less, because \( \frac{1}{8} < \frac{1}{4} \) of a milk tart. (If there are 15 people and 5 milk tarts, each person can eat one third of a milk tart.)
Answers
3. one third ($\frac{1}{3}$)
4. one quarter ($\frac{1}{4}$)
5. $1\frac{3}{5}$ blocks of butter (1 block and three fifths of a block)
6. (a) $\frac{5}{6}$ of a Brownstick long
   (b) one Brownstick long
   (c) one and three twelfths ($1\frac{3}{12}$) of a Brownstick long
7. (a) $\frac{3}{8}$ kg
   (b) $\frac{7}{10}$ kg
8. (a) $\frac{3}{12}$ kg
   (b) $\frac{8}{12}$ kg
### Learner Book Overview

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### Mathematical background

Length, mass, capacity/volume and area are different properties of objects. When we measure these properties of objects, we are using a numerical value to describe how much of that property (in this case length) we have. This allows us to compare and order objects in terms of their length, for example: “The board is longer than the teacher’s desk.” It also allows us to do calculations, for example: “If a roll of string is 500 m, is this enough string to give each Intermediate Phase learner a 2 m length if there are 4 classes with 40 learners in each grade?”

Learners go through four stages when learning to measure:

1. **Identifying and understanding the property they are measuring**
   Most Grade 5 learners should know when they are measuring length, mass or capacity/volume.

2. **Comparing and ordering examples of a particular measure**
   Young learners place objects directly against each other when measuring length. This becomes less efficient when many objects have to be measured.

3. **Using informal or non-standard units to measure** (see question 1 of Section 4.1)
   Learners choose one object, such as a hand or a foot, to use as a unit to measure and quantify many objects. This method does not work very well, because people’s hands differ in width, and an adult’s foot is longer than a child’s foot.

4. **Using formal or standard units to measure** (see Sections 4.2, 4.3, 4.4 and 4.5)
   This allows people in different places to measure, quantify and compare objects using the same measure.

By Grade 5 most learners are comfortable using a ruler to measure in centimetres and millimetres, and find it easy to use a metre stick. However, many learners find it difficult to use a builder’s tape measure, and many have little or no experience using a trundle wheel (see Section 4.4, question 10).

### Resources

Rulers (two photocopiable rulers are given in the Addendum on page 417), measuring tapes, metre sticks, builder’s tape measures, trundle wheel (if available), roll of string, scissors, koki-pens, correction fluid.
4.1 Know the measuring units

**Teaching guidelines**

In this section, learners first work with informal units, discuss the potential problems with these and then move on to working with standard metric units.

You can refer to the tinted passage to explain that although we tend to measure in kilometres, metres, centimetres and millimetres, other metric units of measurement do exist. This will be touched on again in Section 4.3.

**Answers**

1. (a) The question is really: “How many pencils is the length of your book?” Learners’ answers will vary. Some learners may say that they get a number of whole pencil lengths and then part of a pencil length. Learners may find it difficult to be specific about the size of the part pencil lengths.

(b) Move around the class and try to hear what the learners are saying to each other.

(c) Learners’ answers will vary. Learners may say that it is difficult to compare lengths of books using pencil lengths, as pencil lengths vary (see the first tinted passage on page 143 of the Learner Book).

(d) Ask one or two learners for their reasons.

2. (a) Learners’ answers will vary, but may include the following:
   - to find out their size
   - to compare sizes
   - to be able to do calculations around size.

(b) If everyone used their own unit, people would get confused when they tried to tell each other how big something is. For example, if you wanted to buy material for a dress and said: “I need material that is 30 pencils in length”, what could happen? The shopkeeper might have a shorter pencil than you do, and so you would get less material than you expected. For this reason we have standard units of length, such as the metre. Both you and the shopkeeper know how long a metre is.

**How to read the table on page 143**

Begin at the left, and let learners read across to the right: 1 kilometre is the same length as 10 hectometres; 10 hectometres is the same length as 100 decametres; 100 decametres is the same length as 1 000 metres; 1 000 metres is the same length as 10 000 decimetres, which is the same as 100 000 centimetres, which is the same as 1 000 000 millimetres. And so, 1 kilometre is the same length as 1 000 000 millimetres!

### Table 4.1

<table>
<thead>
<tr>
<th>Kilometres (km)</th>
<th>Hectometres (hm)</th>
<th>Decametres (dam)</th>
<th>Metres (m)</th>
<th>Decimetres (dm)</th>
<th>Centimetres (cm)</th>
<th>Millimetres (mm)</th>
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<tr>
<td>1</td>
<td>10</td>
<td>100</td>
<td>1000</td>
<td>10 000</td>
<td>100 000</td>
<td>1 000 000</td>
</tr>
</tbody>
</table>

In South Africa, we use the **metric (decimal) system**, which is a standard system of measurement. Each unit is always the same size. This system is easy to use. To change from one unit to another, we divide by 10 (or multiples of 10), or multiply by 10 (or multiples of 10).

Below is a table of standard units. This year, we will use the units km, m, cm and mm only.
Teaching guidelines
Learners have not yet engaged with hundredths and thousandths in the work on fractions. Explain to them that when an object is divided into 100 equal parts, each part is called one hundredth of the whole. Similarly, when an object is divided into 1 000 equal parts, each part is called one thousandth of the whole.

Answers
3. (a) cm; or m and cm
   (b) cm; or cm and mm
   (c) km
   (d) m; or m and cm
   (e) mm

The standard unit of measuring length in the International System of Units (the SI) is the metre (m). All the other units are named according to their relationship with the 1 m unit.

A centimetre (cm) is the length of each of the parts if 1 m is divided into 100 equal parts.
Centi- in centimetre means hundredth.

A millimetre is one of the parts that is formed when 1 m is divided into 1 000 equal parts.
Milli- in millimetre means thousandth.

A kilometre (km) is 1 000 times as long as 1 m.
Kilo- in kilometre means thousand.

The rulers and tape measures that you already know are marked in centimetres and millimetres. Your teacher can show you another commonly used ruler. It is 1 m long and is called a metre stick.

3. Which unit will you use if you have to measure the length of each of the objects below: millimetre, centimetre, metre or kilometre?
   (a) the height of one of your classmates
   (b) the length of your pencil
   (c) the distance between two towns
   (d) the height of a wall of a building
   (e) the width of your fingernail
Answers

4. Answers will vary. Examples are: width of a small eraser; width of a pen; width of a tube of lip-salve; width of the ear of a mug. Learners may also say: width of one of their fingers.

5. Answers will vary. Examples include: length of a cell phone; width of an envelope; width of a sheet of A4 paper folded lengthwise; width of some learners’ palms.

6. Answers will vary. Examples include: length of a ruler; length of an A4 sheet of paper; width of a chopping board.

7. Answers will vary. Examples include: width or length of a desk or table; width of two sheets of newspaper; a long stride of an adult; width of a door; height of some classroom windows.

8. (a) Answers will vary. Approximately 3 to 5 cm.
(b) Answers will vary. Approximately 1 m.
(c) Answers will vary. Approximately $2\frac{1}{2}$ m.

4.2 Estimate and measure

**Mathematical notes**

Estimating before measuring can help learners to check whether they have made a mistake when measuring. This is particularly useful when measuring lengths of more than a few metres. However, before learners can estimate lengths they need to have a feel for those lengths. It is also useful to find referents for commonly measured lengths (see Section 4.1, questions 4, 5, 6 and 7). The aim is to use these to estimate other lengths.

When learners take measurements, especially where measurements will vary quite a lot, let them collate and keep these measurements. Use them for data handling. Learners can sort, organise, represent and analyse the data. Examples include Section 4.2, questions 1(a) on Learner Book page 145 (see alongside), 6(g) on Learner Book page 148, and 9(c) and (d) on Learner Book page 149.

**Answers**

1. (a) Answers will vary.
(b) Learners might say that they did not experience any problems with the task, but there are difficulties: the bottom ends of some pencils are rounded, not flat, and this makes it difficult to align them with zero on the ruler; some learners’ pencils are sharpened at both ends, and this makes it hard to see just where the points are above the scale on the ruler.

2. Pencil above ruler: 8 cm; pencil below ruler: $3\frac{1}{2}$ cm

4. Name three objects that are about the length of a centimetre.
   (Hint: look at your hands or look around in the classroom.)

5. Name three objects that are about 10 cm long or wide.

6. Name three objects that are about 30 cm long or wide.

7. Name three objects that are about 1 m long or wide.

8. Now use some of the objects that you named in questions 4 to 7 to help you estimate the following:
   (a) the length of your eraser
   (b) the length of your teacher’s table
   (c) the height of your classroom wall
Mathematical notes
The more learners first estimate and then measure lengths, the better they will become at both estimating and measuring. You may need to encourage learners to estimate the lengths before measuring because sometimes learners measure first, round off the measurement and then present that as an estimate. This way of doing it does not build the skill of estimation, nor does it help learners to check whether their measurements or their estimates are reasonable.

Teaching guidelines
You can remind learners to use the referents for 1 cm, 10 cm, and 30 cm that they developed in the previous section to estimate the lengths of the bars. Ask them questions such as: “Are the bars longer or shorter than 10 cm, longer or shorter than 20 cm?”, “About how many times longer than 1 cm are they?”

Answers
3.

<table>
<thead>
<tr>
<th>Bar</th>
<th>Estimated length</th>
<th>Measured length</th>
</tr>
</thead>
<tbody>
<tr>
<td>Red</td>
<td>Around 10 to 12 cm</td>
<td>9 cm 7 mm</td>
</tr>
<tr>
<td>Purple</td>
<td>Around 10 cm</td>
<td>7 cm 3 mm</td>
</tr>
<tr>
<td>Yellow</td>
<td>Around 5 to 6 cm</td>
<td>4 cm 5 mm</td>
</tr>
<tr>
<td>Green</td>
<td>Around 11 to 15 cm</td>
<td>12 cm 8 mm</td>
</tr>
<tr>
<td>Grey</td>
<td>Around 10 to 12 cm</td>
<td>11 cm 0 mm</td>
</tr>
</tbody>
</table>
Mathematical notes
Many people find it more difficult to estimate the length of a curved line than a straight line.

Teaching guidelines
Cut a piece of string about 20 cm long for each learner.

Notes on questions
In question 4(b) it is difficult to measure the curved lines exactly. Discuss with learners the difficulties they experience when measuring these lines.

What question 5 really asks, is for learners to draw straight lines with lengths 2 cm, 8 cm, 12 cm and 15 cm without using a ruler. They will learn more going through this process than they will by drawing “better estimated lengths” while looking at the markings on their ruler.

Answers
4. (a) Lay the piece of string along each object. Grip it at the point where the object ends. Measure the piece of string from the end to that point.

(b) Accept answers that are within a few millimetres of those stated below.

<table>
<thead>
<tr>
<th>Object</th>
<th>Estimated length</th>
<th>Measured length</th>
</tr>
</thead>
<tbody>
<tr>
<td>The length of the red wire</td>
<td>Expect estimates of about 10 cm</td>
<td>8 cm 2 mm</td>
</tr>
<tr>
<td>The length of the purple wire</td>
<td>Expect estimates of about 20 cm</td>
<td>17 cm 3 mm</td>
</tr>
<tr>
<td>The distance around the yellow disc</td>
<td>Expect estimates of about 6 to 12 cm</td>
<td>8 cm 7 mm</td>
</tr>
<tr>
<td>The distance around the green object</td>
<td>Expect estimates of about 7 to 10 cm</td>
<td>7 cm 4 mm</td>
</tr>
</tbody>
</table>

5. Ask learners to use their rulers to draw accurate length lines next to the estimated lines. For each length (2 cm, 8 cm, etc.), ask how many of them came close to the length they had to estimate. Celebrate their successes!
Teaching guidelines
If possible, try to get a builder’s tape measure. These tape measures are usually 5 m long, and are made of a metal strip that rolls up into a neat plastic case. You can find them at any hardware shop and they cost about R20 to R30. Ask the principal about the school’s budget for mathematics equipment – the school can use the same tape measure year after year.
(Note: Don’t pull the tape out all the way past 5 m or the spring might come loose.) If you cannot get a builder’s tape measure, ask some learners to help you prepare pieces of measuring string, like this:

Take a ruler and measure and mark, with correction fluid, a length of 1 m on a table. Then lay the string along that “line”. Tie a knot at one end; this is the zero mark. Now place the knot on the beginning of the line and put your finger at the other end, on the 1 m mark. Tie another knot there. Check that the length between the two knots is really 1 m. Now repeat; from the last knot, measure 1 m of string and find the place to tie the next knot. So you have three knots, marking the positions 0 m, 1 m and 2 m. Carry on and tie knots at 3 m, 4 m, 5 m, all the way to 10 m. (You need a long piece of string!)

On the day of the lesson, show the learners the 10 m measuring string. Ask them where you should put a mark to show a length of 0,5 m. Use a koki-pen to put a mark there, in the middle between the 0 m knot and the 1 m knot. They will soon see that you can put koki-pen marks at 1,5 m, 2,5 m, 3,5 m, and so on.

In question 6, ask learners to estimate the width of the classroom and the height of the door. Then use the measuring string to measure these lengths. Get them to measure more lengths or distances longer than 2 m. This will require them to estimate longer distances in metres. It will also encourage them not just to read off the final numbers, for example 66 cm, but to think about how many metres come before the numbered intervals.

For question 9 you really need enough tape measures for the class, but if you have only the string you can still get value from it. Learners will soon see that markings at 1 m and 0,5 m spacings do not give a very precise answer. The answer will be something like: “The classroom is between 7 m and 7,5 m wide”. Ask learners how they could get a more precise measurement. They will soon see that they can make more marks at 0,1 m, 0,2 m, 0,3 m, 0,4 m, and so on.

Answers
6. Learners’ estimates will vary; in question 8 they will check their estimates with a measuring instrument.
7. (a) Builder’s tape measure or measuring tape  
   (b) Builder’s tape measure or trundle wheel  
   (c) Measuring tape  
   (d) Measuring tape  
   (e) Ruler  
   (f) Ruler
8. (a) and (b) Learners’ own practical work
Mathematical notes

Learners can learn these conversion factors off by heart. However, as with everything learnt off by heart, learners will sometimes forget the conversion factors and use an incorrect one. It may be better for learners to understand how the relationship between metric units works in general: see the table on page 143 in the Learner Book.

**Teaching guidelines**

<table>
<thead>
<tr>
<th>kilometre</th>
<th>hectometre</th>
<th>decametre</th>
<th>metre</th>
<th>decimetre</th>
<th>centimetre</th>
<th>millimetre</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>10</td>
<td>1</td>
<td>1,5</td>
<td>150</td>
<td>150</td>
<td>150</td>
</tr>
</tbody>
</table>

Learners can use a table like the one above to do conversions. They simply work as follows:

- They write the number under the correct unit and then mark which unit they are converting to, for example to convert 150 cm to metres, they write 150 in the “centimetre” column and make a mark (e.g. a small dot or cross) in the metre column.

- If converting from a unit of a lower power to a unit of a higher power, they divide by 10 each time they move to a unit of a higher power. So, in this example, they divide 150 by 10 and then by 10 again, to get to metres.

- If converting from a unit of a higher power to a unit of a lower power, they multiply by 10 each time they move to a unit of a lower power. So, in this example, to get from 1,5 m to centimetres, they multiply 1,5 by 10 and then by 10 again.

See page 416 in the Addendum for a model that may be used to teach conversion between units of measurement as well as a mnemonic that learners may use to remember the order of the units of measurement.

**Answers**

1. (a) Divide by 100  (b) Divide by 10  (c) Divide by 1 000  
   (d) 500 cm  (e) 60 mm  (f) 9 000 mm

2. (a) 10 cm = 100 mm  (b) 300 mm = 30 cm  (c) 100 cm = 1 000 mm  
   (d) 20 mm = 2 cm  (e) 180 cm = 1 800 mm  (f) 600 mm = 60 cm
Notes on questions
In this section, learners get plenty of practice converting units. You may want to split the questions between classwork and work for additional practice (e.g. homework), so that you have enough time for Sections 4.4 and 4.5. One possibility is to use questions 1, 2, 5, 6, 9, 10 and 11 for classwork, and the rest for additional practice.

Answers
3. | mm | 20 | 50 | 30 | 180 | 90 | 40 | 100 | 1000 | 130 | 540 | 430 | 4300 |
   | cm | 2   | 5   | 3   | 18  | 9  | 4   | 10   | 100   | 13  | 54  | 43  | 430  |

4. (a) 480 cm = \( \frac{48}{10} \) m  
(b) 560 mm = 56 cm  
(c) 30 m = 3 000 cm  
(d) 20 m = 20 000 mm  
(e) 300 mm = 30 cm  
(f) 750 mm = \( \frac{3}{4} \) m

5. (a) | mm | 4 000 | 8 000 | 6 000 | 2 000 | 9 000 | 1 000 |
    | cm | 400   | 800   | 600   | 200   | 900   | 100   |
    | m  | 4      | 8      | 6      | 2      | 9      | 1      |
(b) | mm | 12 000 | 3 000 | 5 000 | 6 000 | 9 000 | 75 000 |
    | cm | 1 200 | 300   | 500   | 600   | 900   | 7 500  |
    | m  | 12     | 3      | 5      | 6      | 9      | 75     |

6. (a) 1 km = 1 000 m  
(b) 1 000 m = 1 km  
(c) 20 km = 20 000 m  
(d) 3 500 m = \( \frac{3}{2} \) km  
(e) 450 km = 450 000 m  
(f) 300 m = \( \frac{3}{10} \) km

7. | m  | 2 000 | 8 500 | 18 000 | 134 000 | 28 000 | 500 | 176 000 | 4 500 | 5 500 |
   | km | 2     | \( \frac{8}{2} \) or 8,5 | 18 | 134 | 28 | \( \frac{1}{2} \) | 176 | 4,5 | \( \frac{5}{2} \) or 5,5 |
Notes on questions
Question 9 prepares learners for question 10. It is useful for learners to answer questions 9(a), (b) and (c) before answering question 10.

Answers

8. (a) 5 892 m = 5 km and 892 m  
(b) 17 056 m = 17 km and 56 m  
(c) 8 331 m = 8 km and 331 m  
(d) 23 451 m = 23 km and 451 m  
(e) 2 003 m = 2 km and 3 m  
(f) 100 400 cm = 1 km and 4 m

9. (a) \( \frac{1}{2} \) m  
(b) \( \frac{1}{4} \) m  
(c) 25 cm

10. (a) 125 cm  
(b) 250 cm  
(c) 175 cm

11. (a) 7 035 m  
(b) 8 m and 4 mm  
(c) 3 m and 8 cm and 2,5 mm  
(d) 10 m and 40 cm  
(e) 36 m and 71 cm  
(f) 4 250 m

12. Yes, but only by converting the lengths to the same unit.

13. (a) 82 km and 894 m  
(b) 19 km and 55 m  
(c) 679 m and 38 cm  
(d) 3 m and 6 cm and 7 mm  
(e) 788 m and 29 cm  
(f) 80 km and 757 m

14. (a) 52 km and 894 m  
(b) 55 m  
(c) 668 m and 62 cm  
(d) 2m and 47 cm and 3 mm  
(e) 612 m and 21 cm  
(f) 65 km and 757 m

15. Learners’ methods will vary.
   (a) 12\( \frac{1}{2} \) m; \( \frac{3}{4} \) m; 643 cm; 870 mm
   (b) 1,5 km; 1 230 m; 21 877 cm
   (c) 521 027 m; 861 490 cm; 1\( \frac{1}{2} \) km; 0,5 km; 91 499 mm; 556 cm
   (d) 25 km; 20 000 m; 150 000 cm
4.4 Rounding off with units of measurement

Mathematical notes
We can round off to the nearest unit of measurement or we can round off to the nearest multiple of a number, for example 5, 10, 100, 1 000. In this section, learners are asked to round off in both these ways.

Measurement provides a useful context for learners to understand rounding off. In particular, questions that ask “is it closer to . . . . or is it closer to . . . .” help learners to understand rounding off.

Teaching guidelines
You should do an activity with the class to explain the simplest kind of “rounding off”. Use your board ruler to draw a line on the board, a little less than a metre long. The board ruler is marked in centimetres, with long marks at 0 cm, 10 cm, 20 cm, 30 cm, and so on. Measure the length of the line. Let’s say it is about 87 cm long. Hold the board ruler next to the line and say to the class: “Is the end of the line closer to 80 cm or is it closer to 90 cm? This line, to the nearest 10 cm, is 90 cm long.”

Let’s say you drew a different line, 92 cm long. Hold the ruler next to the line and say to the class: “Is the end closer to 90 cm or is it closer to 100 cm? This line, to the nearest 10 cm, is 90 cm long.”

Now what if you drew another line, 95 cm long? 95 is halfway between 90 and 100. Explain that we now use the rule that if the measurement is halfway between two main marks on the scale, we round up to the next highest mark. So, in this example, we round 95 cm up to 100 cm. That is like rounding 95 cm up to one whole metre.

Next you can use the tinted passage to motivate and to explain rounding off. You can also show these numbers on a number line or measuring tape so that learners can actually see which multiple the number is closer to.

Rounding off to the nearest 5 is new in Grade 5. You may need to spend some time explaining this.

Teachers sometimes teach a procedure which involves underlining the power you are rounding off to, and circling the digit that follows. This does not help learners to understand the meaning of rounding off. It also becomes confusing when learners need to start rounding off to the nearest 5. It may make more sense if you encourage learners to think of “the nearest multiple to”. 

When a length is given in a smaller unit, we often round it off to a bigger unit.

- If you round off to the nearest 100 cm, it is the same as rounding off to the nearest metre. Rounding off to the nearest 10 mm is the same as rounding off to the nearest centimetre, rounding off to the nearest 1 000 m is the same as rounding off to the nearest kilometre and so on.
- So, 46 mm rounded off to the nearest centimetre is 5 cm. This is because there are 10 mm in 1 cm, and 46 mm is closer to 50 mm than to 40 mm.
- 2 592 m rounded to the nearest kilometre is 3 km. There are 1 000 m in 1 km, and 2 592 m is closer to 3 000 m than 2 000 m.

We can also round off to other numbers, for example to the number 5. The number 5 and its multiples then become your base:

<table>
<thead>
<tr>
<th>Number</th>
<th>Rounded to the Nearest 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>becomes 10</td>
</tr>
<tr>
<td>84</td>
<td>becomes 85</td>
</tr>
<tr>
<td>6</td>
<td>becomes 5</td>
</tr>
<tr>
<td>999</td>
<td>becomes 1 000</td>
</tr>
<tr>
<td>1 844</td>
<td>becomes 1 845</td>
</tr>
<tr>
<td>2 708</td>
<td>becomes 2 710</td>
</tr>
</tbody>
</table>

152 UNIT 4: LENGTH

MATHEMATICS GRADE 5 TEACHER GUIDE [TERM 2] 165
**Notes on questions**

Some of the sub-questions (b, d, e, f, h, i, j) in question 1 require learners to convert between units, or at least to have a sound understanding of the relationship between metric units of length.

Question 2 focuses on rounding to the nearest 5. This is new in Grade 5.

**Answers**

1. (a) 20 cm  
   (b) 100 cm  
   (c) 7 700 km  
   (d) 25 m  
   (e) 2 km  
   (f) 3 cm  
   (g) 10 km  
   (h) 10 m  
   (i) 56 m  
   (j) 2 m

2. (a) 15 km  
   (b) 45 cm  
   (c) 55 cm  
   (d) 300 km  
   (e) 25 mm  
   (f) 90 cm  
   (g) 600 mm  
   (h) 15 m  
   (i) 510 m  
   (j) 20 km

3. (a) 1 750 km  
   (b) 1 100 km  
   (c) 363 100 km; 405 700 km

1. Round the following lengths up or down as required.
   (a) 16 cm to the nearest 10 cm
   (b) 983 mm to the nearest cm
   (c) 7 665 km to the nearest 100 km
   (d) 2 519 cm to the nearest m
   (e) 1 500 m to the nearest km
   (f) 28 mm to the nearest cm
   (g) 9 km to the nearest 10 km
   (h) 999 cm to the nearest m
   (i) 5 569 cm to the nearest m
   (j) 2 099 mm to the nearest m

2. Round off to the nearest 5 of the given unit.
   (a) 16 km  
   (b) 44 cm  
   (c) 57 cm  
   (d) 302 km  
   (e) 25 mm  
   (f) 89 cm  
   (g) 599 mm  
   (h) 14 m  
   (i) 509 m  
   (j) 19 km

3. (a) The distance between Cape Town and Durban is given as 1 753 km. Round it off to the nearest 10 km.
   (b) The distance between Cape Town and East London is given as 1 079 km. Round it off to the nearest 100 km.
   (c) The distance from the Earth to the moon is not the same everywhere. This is because of the shape of the orbit of the Earth around the Sun. The shortest distance is given as 363 104 km. The longest distance is given as 405 696 km.
   Round off both of these distances to the nearest 100 km.
4.5 Problem solving

**Mathematical notes**

In these problems learners will use converting between units, rounding off, addition, subtraction, multiplication, division, and ratio.

**Answers**

1. (a) 184 km and 3 m  
   (b) 39 km and 501 m  
   (c) Sum of all the rounded distances: 184 km, so the difference is 3 m  
   (d) 66 km and 500 m

2. (a) Snail covers 746 cm = 7 m and 46 cm  
    Sparrow covers 746 cm × 5 = 3 730 cm = 37 m and 30 cm  
    Hen covers 3 730 cm × 2 = 7 460 cm = 74 m and 60 cm  
    Scottish Terrier covers 746 cm × 36 = 26 856 cm = 268 m and 56 cm  
   (b) 7 m and 46 cm; 37 m and 30 cm; 74 m and 60 cm; 268 m and 56 cm  
   (c) 7 460 mm  
   (d) 156 m and 66 cm or 15 666 cm  
   (e) 38 792 cm = 387 m and 92 cm
Answers
2. (f) Snail: 745 cm; Sparrow: 3 730 cm; Hen: 7 460 cm; Scottish Terrier: 26 855 cm
   (g) 1 492 cm = 14 m and 92 cm

Notes on questions
In question 5, it is important that learners do the drawings. This will allow them to see that Nandi can plant at the start of a row and at the end of a row. If she plants tomatoes at the start and end of the row she can plant 7 tomato plants and 11 mealie seeds. If learners translate (b) into a number sentence, they will get 300 cm ÷ 50 cm = 6, i.e. 6 tomatoes, and if they translate (c) into a number sentence, they will get 300 cm ÷ 30 cm = 10, i.e. 10 mealie seeds.

Answers
3. (a) 6 000 m (b) 7,5 km
4. (a) 5 × 100 m = 500 m (b) 100 m too few
5. (a) Learners' drawings might look something like this:
   ![Diagram of Nandi's garden]
   (b) 7 tomato plants. (Learners are not expected to show the measurements.)
   (c) 11 mealie seeds. (Learners are not expected to show the measurements.)
   (d) 4 rows (e) 88 mealie seeds (f) 70 tomato plants

(f) Round off the distance each animal travelled in the one hour to the nearest 5 cm.
(g) How far must Sparrow go if he wants to double Snail's distance?
3. For each 1 500 m that Mrs Cat runs, Mr Dog runs 2 000 m.
   (a) How far does Mr Dog run if Mrs Cat runs 4 500 m?
   (b) How far does Mrs Cat run if Mr Dog runs 10 km?
4. Adam wants to put up an electric fence consisting of five wires around his yard. He needs 5 lengths of 120 m wire. He decides to round off the length of the wire to the nearest 100 to make it easier to work out how much wire he will need.
   (a) How many metres of wire does he need if he works it out like this?
   (b) How many metres too many or too few is this?
5. Nandi plants vegetables in her vegetable patch. Each row is 3 m long. There are several rows.
   (a) Draw two rows each 12 cm long and divide each row into 3 equal parts. Each of the parts represents 1 cm.
   (b) In the first row, Nandi plants her tomatoes 50 cm apart. Make marks on your drawing to show where the tomato plants will go. How many can she plant in this row?
   (c) In the next row, she plants mealies 30 cm apart. Make marks on your drawing to show where the mealie seeds will go. How many mealie seeds will she plant in this row?
   (d) She plants more rows of tomatoes, also 50 cm apart. If she has 28 tomato plants, how many rows of tomatoes can she plant?
   (e) For every 7 tomato plants that she plants, she plants 11 mealie seeds. How many mealie seeds will she plant if she plants 56 tomato plants?
   (f) How many tomato plants does she need if she plants 110 mealie seeds?
5. (g) two thirds  
(h) two thirds

6. (a) $37 \text{ mm} + 33 \text{ mm} = 70 \text{ mm}$  
(b) $87 \text{ cm} + 13 \text{ cm} = 1 \text{ m}$  
(c) $155 \text{ m} - 35 \text{ m} = 120 \text{ m}$  
(d) $880 \text{ mm} + 20 \text{ mm} = 90 \text{ cm}$  
(e) $7500 \text{ m} + 500 \text{ m} = 8 \text{ km}$  
(f) $6402 \text{ m} + 3598 \text{ m} = 10 \text{ km}$  
(g) $11\frac{1}{2} \text{ km} - 2\frac{1}{2} \text{ km} = 9000 \text{ m}$  
(h) $1554 \text{ cm} + 46 \text{ cm} = 16 \text{ m}$
Grade 5 Term 2 Unit 5  Whole numbers: Multiplication

### Learner Book Overview

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<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
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</thead>
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<td>165 to 166</td>
</tr>
</tbody>
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### CAPS time allocation
7 hours

### CAPS page references
13 to 15 and 166

### Mathematical background

Multiplication and division are applicable in the following two kinds of situations:

- **Additive situations**, in which a whole quantity can be considered as being made up of equal parts.
  
  Example: A consignment of sugar is packaged into a number of packets of equal mass.
  
  Situations like this can be described with a number sentence of the form:
  
  number of parts \( \times \) size of each part = total quantity, or
  
  number of parts \( \times \) value of each part = total value.
  
  The “value of each part” is sometimes called the **rate**.
  
  The number of parts can be a whole number or a fraction.

- **Multiplicative situations**, in which one quantity can be considered as an enlargement (“stretching”) or reduction (“shrinking”) of another situation.
  
  Example: A scale drawing of a building.
  
  Situations like this can be described with a number sentence of the form:
  
  size of one object \( \times \) scale factor (ratio) = size of another object

### Possible questions

- 430 packets of sugar each have a mass of 400 g. How much sugar is this in total? (430 \( \times \) 400)
- 1 200 kg sugar is packaged in packets of 400 g each. How many packets is this? (1 200 ÷ 400, grouping)
- 1 200 kg of sugar is packed into 400 equal packets. How much sugar is in each packet? (1 200 ÷ 400, sharing)

- A house is 20 times as high as the drawing of the house on a building plan.
  
  - How high is the house if the drawing is 9 cm high? (20 \( \times \) 9)
  
  - How high is the drawing if the house is 240 cm high? (240 ÷ 20)

- The height of a drawing of a house is 15 cm and the actual house is 240 cm high. How much larger than the drawing is the house? (The house is 240 ÷ 15 = 16 times larger than the drawing.)
5.1 Refresh your multiplication memory

**Teaching guidelines**
Explain to learners that question 1 provides them with an opportunity to assess their knowledge of multiplication facts in the domain:

- 1-digit number \( \times \) multiple of 10.

More specifically, question 1 provides learners with an opportunity to identify which multiplication facts in the above domain they cannot easily produce. They should write these facts down so that they can work on them later.

You can save classroom time by making copies of page 419 of the Addendum, so that learners can fill in the answers they know immediately and simply skip those questions for which they cannot produce the answer quickly.

### Answers

<p>| | | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>30 ( \times ) 8 = 240</td>
<td>30 ( \times ) 10 = 300</td>
<td>30 ( \times ) 2 = 60</td>
<td>30 ( \times ) 5 = 150</td>
<td></td>
</tr>
<tr>
<td>70 ( \times ) 7 = 490</td>
<td>70 ( \times ) 8 = 560</td>
<td>70 ( \times ) 10 = 700</td>
<td>70 ( \times ) 2 = 140</td>
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<tr>
<td>80 ( \times ) 6 = 480</td>
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<td>80 ( \times ) 8 = 640</td>
<td>80 ( \times ) 10 = 800</td>
<td></td>
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<tr>
<td>50 ( \times ) 4 = 200</td>
<td>50 ( \times ) 6 = 300</td>
<td>50 ( \times ) 7 = 350</td>
<td>50 ( \times ) 8 = 400</td>
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<tr>
<td>20 ( \times ) 9 = 180</td>
<td>20 ( \times ) 4 = 80</td>
<td>20 ( \times ) 6 = 120</td>
<td>20 ( \times ) 7 = 140</td>
<td></td>
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<tr>
<td>90 ( \times ) 3 = 270</td>
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<td>90 ( \times ) 4 = 360</td>
<td>90 ( \times ) 6 = 540</td>
<td></td>
</tr>
<tr>
<td>60 ( \times ) 5 = 300</td>
<td>60 ( \times ) 3 = 180</td>
<td>60 ( \times ) 9 = 540</td>
<td>60 ( \times ) 4 = 240</td>
<td></td>
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<td>10 ( \times ) 2 = 20</td>
<td>10 ( \times ) 5 = 50</td>
<td>10 ( \times ) 3 = 30</td>
<td></td>
</tr>
<tr>
<td>30 ( \times ) 3 = 90</td>
<td>30 ( \times ) 9 = 270</td>
<td>30 ( \times ) 4 = 120</td>
<td>30 ( \times ) 6 = 180</td>
<td>30 ( \times ) 7 = 210</td>
</tr>
<tr>
<td>70 ( \times ) 5 = 350</td>
<td>70 ( \times ) 3 = 210</td>
<td>70 ( \times ) 9 = 630</td>
<td>70 ( \times ) 4 = 280</td>
<td>70 ( \times ) 6 = 420</td>
</tr>
<tr>
<td>80 ( \times ) 2 = 160</td>
<td>80 ( \times ) 5 = 400</td>
<td>80 ( \times ) 3 = 240</td>
<td>80 ( \times ) 9 = 720</td>
<td>80 ( \times ) 4 = 320</td>
</tr>
<tr>
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<td>50 ( \times ) 2 = 100</td>
<td>50 ( \times ) 5 = 250</td>
<td>50 ( \times ) 3 = 150</td>
<td>50 ( \times ) 9 = 450</td>
</tr>
<tr>
<td>20 ( \times ) 8 = 160</td>
<td>20 ( \times ) 10 = 200</td>
<td>20 ( \times ) 2 = 40</td>
<td>20 ( \times ) 5 = 100</td>
<td>20 ( \times ) 3 = 60</td>
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<tr>
<td>90 ( \times ) 7 = 630</td>
<td>90 ( \times ) 8 = 720</td>
<td>90 ( \times ) 10 = 900</td>
<td>90 ( \times ) 2 = 180</td>
<td>90 ( \times ) 5 = 450</td>
</tr>
<tr>
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<td>60 ( \times ) 8 = 480</td>
<td>60 ( \times ) 10 = 600</td>
<td>60 ( \times ) 2 = 120</td>
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<tr>
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<td>40 ( \times ) 7 = 280</td>
<td>40 ( \times ) 8 = 320</td>
<td>40 ( \times ) 10 = 400</td>
</tr>
<tr>
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<td>10 ( \times ) 6 = 60</td>
<td>10 ( \times ) 7 = 70</td>
<td>10 ( \times ) 8 = 80</td>
</tr>
</tbody>
</table>
Critical knowledge and skills
Without fluency in the production of multiplication facts for 1-digit numbers and multiples of 10, 100 and 1 000, learners cannot do multiplication with multi-digit whole numbers fast and accurately enough to be of any value.

Teaching guidelines
Fluency in the production of basic number facts depends on memorising at least some facts, and the ability to quickly produce non-remembered facts from known facts. Explain this to learners. To save classroom time, you can photocopy the table provided on page 420 of the Addendum.

Demonstrate how new facts can be formed from known facts. Use the example in the tinted passage and other examples of your own choice.

Answers
2. Learners work out the answers to the questions they listed (or skipped) in question 1.
3. Learners copy only their answers from question 2 into the given table.

<table>
<thead>
<tr>
<th>×</th>
<th>2</th>
<th>4</th>
<th>8</th>
<th>3</th>
<th>6</th>
<th>5</th>
<th>10</th>
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<td>630</td>
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<td>80</td>
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<td>240</td>
<td>480</td>
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<td>720</td>
<td>560</td>
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<tr>
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<td>240</td>
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<td>400</td>
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<tr>
<td>20</td>
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<tr>
<td>70</td>
<td>140</td>
<td>280</td>
<td>560</td>
<td>210</td>
<td>420</td>
<td>350</td>
<td>700</td>
<td>630</td>
<td>490</td>
</tr>
</tbody>
</table>
5.2 Working with hundreds

**Teaching guidelines**

The purpose of this section is to develop fluency in the production of multiplication facts for multiples of 10 and 100. While the trick of counting zeros, for example finding $30 \times 40$ by adding two zeros to the answer 12 for $3 \times 4$ is useful, it is important that learners also understand the multiplication facts for multiples of 10 and 100.

The questions are designed to provide learners with opportunities to develop such understanding.

**Answers**

1. (a) 24    (b) 240
2. Double 600 → 1 200 and double again → 2 400
   Mlungisi is right.
3. 2 400
4. (a) 600    (b) 40
5. Both give the same answer: 2 400.
6. 24 000
**Teaching guidelines**

Questions 7 and 8 are intended to help learners to form a sense of the magnitude of multiples of 10, 100, 1 000, 10 000 and 100 000, and how they relate to each other. To promote quality of engagement with the questions, you could make a drawing for question 7(a) on the board and ask learners to suggest how you should change the drawing so that it represents question 7(b), and question 7(c):

[Diagram of drawing]

If learners are challenged by question 8, you may suggest that they write parts of the statements in symbols, for example question 8(b):

10 10 10 10 10 10 10 10 10 10 . . . . . . . . . . . . . . . . . .

Such a representation may provide support for learners’ thinking about the meaning of the statement, for example:

10 10 10 10 10 10 10 10 10 10 . . . . . . . . . . . . . . . . . .

<table>
<thead>
<tr>
<th>ten tens = one hundred</th>
</tr>
</thead>
<tbody>
<tr>
<td>ten tens = one hundred, etc.</td>
</tr>
</tbody>
</table>

**Answers**

7. (a) 100  
    (b) 1 000  
    (c) 10 000  
    (d) 300  
    (e) 700  
    (f) 7 000

8. (a) True  
    (b) False  
    (c) True  
    (d) True  
    (e) True  
    (f) True

9. 100 \times 583 = 100 \times 500 + 100 \times 80 + 100 \times 3 = 50 000 + 8 000 + 300

10. 100 \times 6 = 600  
    100 \times 60 = 6 000  
    200 \times 60 = 12 000  
    400 \times 60 = 24 000  
    60 \times 300 = 18 000  
    30 \times 600 = 18 000  
    50 \times 700 = 35 000  
    400 \times 80 = 32 000  
    900 \times 4 = 3 600  
    40 \times 900 = 36 000  
    70 \times 900 = 63 000  
    8 \times 700 = 5 600  
    600 \times 70 = 42 000  
    30 \times 900 = 27 000  
    700 \times 40 = 28 000
5.3 Multiply 3-digit numbers by 1-digit numbers

**Teaching guidelines**
Do the example in the tinted passage on the board, and possibly one or two more. Emphasise the strategy of replacing the single “difficult” product \((347 \times 8)\) with the sum of three “easy products” \((300 \times 8, 40 \times 8\) and \(7 \times 8\)).

**Notes on questions**
Learners may find question 5 demanding. The question is deliberately designed to provide learners with the challenge to interpret the different numbers given.

At each feeding session the 8 goats together will get \(8 \times 375\) ml, that is \(3\,000\) ml or \(3\) l. Hence Jane needs \(4 \times 3 = 12\) l every day.

Some learners may argue like this and will have to calculate the product of a 2-digit and a 3-digit number:

*Feeding 8 goats four times a day is \(4 \times 8 = 32\) feeds at \(375\) ml per feed, which is \(32 \times 375\) ml.*

If such learners are challenged by the multiplication, you can suggest to them that they first calculate how much milk is needed for one feeding session for 8 goats.

**Answers**
1. (a) 3 941  (b) 2 268  
   (c) 3 258  (d) 4 984  
   (e) 2 442  (f) 4 710  
   (g) 2 556  (h) 3 451  
   (i) 4 696  (j) 2 792  
   (k) 3 346  (l) 7 264
2. 1 666 rooms
3. 1 248 guests
4. 5 193 water sachets
5. 12 l
6. R1 251
7. 7 kg
5.4 Multiply 3-digit numbers by 2-digit numbers

Teaching guidelines
Learners have already multiplied a 2-digit number by a 3-digit number in Term 1. It should suffice to demonstrate one or two cases, for example $67 \times 547$ and $56 \times 884$, on the board before allowing learners to engage with question 1 and proceed to the other questions.

Notes on questions
To do question 4 quickly, one needs to observe that 177 is half of 354. It is unlikely that all learners in a class will notice this by themselves. After giving learners some time to work on question 4, you may ask them what half of 354 is, and suggest that if they know this the question will become easy.

Answers
1. $300 \times 80 + 40 \times 80 + 7 \times 80 + 300 \times 4 + 40 \times 4 + 7 \times 4$
   $= 24000 + 3200 + 560 + 1200 + 160 + 28$
   $= 29148$
2. $80 \times 300 + 80 \times 40 + 80 \times 7 + 4 \times 300 + 4 \times 40 + 4 \times 7$
   $= 24000 + 3200 + 560 + 1200 + 160 + 28$
   $= 29148$
3. (a) 29184 (b) 20992 (c) 15708 (d) 23464 (e) 32121 (f) 21252 (g) 45402 (h) 18434 (i) 18408 (j) 34146 (k) 16704 (l) 22816
4. 177 is half of 354, therefore the answer must be half of $18408 = 9204$ kg
5. R29 296
6. 6 096 light bulbs
7. (a) 18 564 strawberry plants
   (b) 22 320 jars

5.4 Multiply 3-digit numbers by 2-digit numbers

347 $\times$ 84 can be calculated as follows:

347 = 300 $+$ 40 $+$ 7

So, $347 \times 84 = 300 \times 84 + 40 \times 84 + 7 \times 84$

$= 300 \times 80 + 40 \times 80 + 4 \times 80 + 300 \times 4 + 40 \times 4 + 7 \times 4$

Each of the three parts have to be calculated separately.

1. Calculate each of the parts of $347 \times 84$ shown above, and then find out how much $347 \times 84$ is.
2. Calculate $347 \times 84$ in a different way, by first breaking down 84 into 80 and 4.
3. Calculate each of the following.
   (a) 384 $\times$ 76  (b) 64 $\times$ 328
   (c) 374 $\times$ 42  (d) 419 $\times$ 56
   (e) 83 $\times$ 387  (f) 276 $\times$ 77
   (g) 658 $\times$ 69  (h) 709 $\times$ 26
   (i) 52 $\times$ 354  (j) 542 $\times$ 63
   (k) 288 $\times$ 58  (l) 46 $\times$ 496
4. See if you can use your answer for question 3(i) to calculate the mass of 177 bags of river sand if the mass of one bag is 52 kg.
5. The entrance fee for a concert is R32 for school children and R48 for adults. Tickets are sold at the door. How much money is taken at the door if 215 children and 467 adults attend the concert?
6. Twenty-four schools each receive a large box with 254 light bulbs. How many light bulbs is this in total?
7. (a) On a strawberry farm, there are 546 strawberry plants in each bed. How many plants are there altogether in 34 strawberry beds?
   (b) Strawberry jam is also produced on the farm and packed in boxes of 48 jars each. How many jars are there in 465 boxes?
Answers
8. (a) 576 balls  (b) R7 488

5.5 Rate

Mathematical notes
A rate describes how much of one quantity (e.g. money) corresponds to one unit of another quantity (e.g. volume of petrol): R10,40 may correspond to 1 ℓ of petrol. Other examples of rates are speed (the distance that corresponds to a unit of time), dosages (amount of medicine that corresponds to a unit of body mass), tax (amount of tax that corresponds to R1 000 of income) and sound pitch (number of vibrations that correspond to a unit of time).

Any rate situation can be represented by a number sentence of the form

\[ \text{amount} \times \text{rate} = \text{total} \]

For example, if a recipe requires 5 g of salt for every kg of beans, the number sentence is

\[ \text{mass of beans in kg} \times 5 = \text{mass of salt in g} \]

In the case of cost rates, the number sentence can be stated as

\[ \text{amount} \times \text{unit cost} = \text{total cost} \]

In the case of speed, the number sentence can be stated as

\[ \text{duration of time} \times \text{speed} = \text{distance covered} \]

Possible misconceptions
Learners may easily form the misconception that a rate is always constant. This may inhibit them from engaging successfully with situations that involve variable rates, which becomes important in higher grades. The drum play situation used as an introductory context here, and question 2 on the next page, are specifically designed to alert them to variable rates at an early stage.

Teaching guidelines
Ask learners to comment on the difference between Salmon and Rashid’s drum playing once they have finished completing the table in question 2. You may introduce the term “changing rate” or “variable rate” to distinguish Rashid’s playing from Salmon’s playing.

Answers
1. 18 beats
Notes on questions
The first three parts of question 4 demonstrate three different kinds of questions that can be asked with respect to a situation that involves a constant rate.

In question 4(a) the rate and the duration of time are given, and the total number of beats has to be calculated:  \(5 \times 8 = \text{total number of beats}\)

In question 4(b) the duration of time and the total number of beats are given, and the rate has to be calculated:  \(3 \times \text{rate} = 36 \text{ beats}\)

In question 4(c) the rate and the total number of beats are given, and the duration of time has to be calculated:  \(\text{duration of time} \times 8 = 32 \text{ beats}\)

Teaching guidelines
To help learners who are challenged by questions 4(b) and 4(c), you may suggest that they clarify to themselves what is known and what is unknown in each of questions 4(a), (b) and (c). They may make and complete a table like this before attempting to answer questions (b) and (c):

<table>
<thead>
<tr>
<th></th>
<th>Play time</th>
<th>Rate</th>
<th>Number of beats</th>
</tr>
</thead>
<tbody>
<tr>
<td>Question 4(a)</td>
<td>5 minutes</td>
<td>8 beats per minute</td>
<td>unknown</td>
</tr>
<tr>
<td>Question 4(b)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Question 4(c)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Once learners have completed question 4, you may show them how the different questions can be represented by number sentences as shown above. Resist the temptation to show the number sentences before learners have engaged with the questions intensively. Seeing the number sentences may deny them the opportunity to learn to interpret verbal descriptions of situations.

Answers

2.

<table>
<thead>
<tr>
<th></th>
<th>First minute</th>
<th>Second minute</th>
<th>Third minute</th>
<th>Fourth minute</th>
</tr>
</thead>
<tbody>
<tr>
<td>Salmon</td>
<td>6</td>
<td>6</td>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>Rashid</td>
<td>14</td>
<td>19</td>
<td>26</td>
<td>32</td>
</tr>
</tbody>
</table>

3. No

4. (a) 40 beats  (b) At a rate of 12 beats per minute  (c) 4 minutes  (d) 60 beats

5. (a) 222 tomatoes  (b) 400 tomatoes

2. Copy the table below. Count the dots in each cell of the table on page 163 and enter the numbers in your table.

<table>
<thead>
<tr>
<th></th>
<th>First minute</th>
<th>Second minute</th>
<th>Third minute</th>
<th>Fourth minute</th>
</tr>
</thead>
<tbody>
<tr>
<td>Salmon</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Rashid</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Salmon beat his drum at a rate of 6 beats per minute during the whole item.

We can say Salmon played at a constant rate of 6 beats per minute, for 4 minutes.

3. Did Rashid also play at a constant rate during the 4 minutes?

4. (a) In another item, Rashid plays at a constant rate of 8 beats per minute and he plays for 5 minutes. How many beats does he make in total?

(b) In this item Salmon also plays at a constant rate, but he only plays for 3 minutes. He makes 36 beats in total. At what rate does Salmon play?

(c) There is a third drummer in this item. Maria plays at a constant rate of 8 beats per minute, and she makes 32 beats in total. For how many minutes does she play?

(d) If Salmon continues to play as fast as he does in question (b), how many beats will he make in 5 minutes?

5. Eric, Sally and Katie are working on a tomato farm.

(a) Eric picks tomatoes at an almost constant rate of 74 tomatoes per hour. Approximately how many tomatoes will he pick in .3 hours?

(b) Sally also picks tomatoes at an almost constant rate. She picks 240 tomatoes in 3 hours. How many tomatoes will she pick in 5 hours?
5. (c) 6 hours

5.6 Ratio

Mathematical notes

Quantities can be compared in two ways:

- By stating the difference: how much more the one quantity is than the other, for example “Susan earns R24 000 more than William each month.”
- By stating the ratio: by what the one quantity must be multiplied to get the other quantity, for example “Susan earns 3 times as much as William each month.”

Both difference and ratio are used to compare two quantities of the same kind. Ratios appear in different kinds of situations, several of which are addressed in Term 4 Unit 5.

In this unit, the concept of ratio is introduced to compare two rates.

Teaching guidelines

Questions 1 to 7 provide learners with a variety of opportunities to compare two quantities, namely the different constant rates at which Salmon and Rashid beat their drums.

The term “ratio” is only introduced after learners have done these questions (i.e. on page 166 of the Learner Book).

Answers

3. At a rate of 30 beats per minute
4. (a) 150
   (b) 30
Teaching guidelines
Learners’ comparison of the two drum-beating rates culminates in the completion of the table in question 6.

Once learners have completed question 7, you may put this question to the whole class: “Does Rashid beat his drum five times as often as Salmon?”

Reflection and discussion on this question should help learners to consolidate the idea of a fixed ratio between the two drum-beating rates.

Answers
5. (a) 90 times 
   (b) 24 times

6. | Number of beats on the small drum | 30 | 60 | 90 | 120 | 150 | 180 | 210 | 240 |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of beats on the big drum</td>
<td>6</td>
<td>12</td>
<td>18</td>
<td>24</td>
<td>30</td>
<td>36</td>
<td>42</td>
<td>48</td>
</tr>
</tbody>
</table>

7. (a) 60 (b) 150 (c) 45 (d) 5

8. (a) The ratio of Isaac’s steps to Benjamin’s steps is 12 to 20 or 3 to 5.
   (b) 10 steps
   (c) 18 steps
Grade 5 Term 2 Unit 6       Properties of three-dimensional objects

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.1 Flat and curved surfaces on 3-D objects</td>
<td>An overview of the surfaces of 3-D objects</td>
<td>167 to 168</td>
</tr>
<tr>
<td>6.2 Make cylinders and cones</td>
<td>Make cylinders and cones out of paper and other materials</td>
<td>169 to 171</td>
</tr>
<tr>
<td>6.3 Make prisms and pyramids</td>
<td>Make prisms and pyramids out of paper and other materials</td>
<td>172 to 175</td>
</tr>
</tbody>
</table>

**Mathematical background**
Cylinders and prisms are very similar. Any cylinder and any prism has two identical flat surfaces (faces) at the ends. A cylinder has only one other surface, which is curved, while all the other surfaces of a prism are flat – in fact, rectangles.

Cones and pyramids have a flat surface at one end (the base) and a pointed end (like a sharpened pencil) opposite the base. A cone has one curved surface between the flat (circular) base and the pointed end, while a pyramid has one flat triangular surface for each side of the polygonal base.

**Resources**
Many models and/or real-life examples of prisms, pyramids, cylinders and cones; paper, scissors and sticky tape.
6.1 Flat and curved surfaces on 3-D objects

Teaching guidelines
If possible, provide many more examples of prisms, pyramids, cylinders and cones. The best way for learners to begin to distinguish properly between the four types of objects is to have as many as possible of these objects available, and to ask learners to group the objects into the four categories. Ensure that learners are able to justify their classification by referring to the key characteristics mentioned on the previous page of this Teacher Guide.

Possible misconceptions
Some learners may confuse the four kinds of objects because they are not yet distinct in their minds (this is due to inexperience, or to them not focusing on the important characteristics: pointedness or not, curved surfaces or polygonal faces). Beware that some learners may simply be confusing the names, for example saying pyramid when they mean prism.
**Teaching guidelines**

Once learners have completed the questions individually and have written down their answers, let them compare their answers in small groups.

**Answers**

1. Mountains photo: three cylindrical mountains with cone-shaped tops  
   Windmill photo: triangular pyramid as the standing frame for the windmill,  
   cylindrical dam  
   Antlion trap photo: cone-shaped hole  
   Hut photo: cylindrical building, cone-shaped roof  
   Church photo: squared-based pyramidal tower roof  
   Pipes photo: cylinder

2. Learners' own work

3. Learners' own work

4. Probably yes, but the answer depends on the actual classroom.

**Teaching guidelines**

It is worthwhile to teach learners how to make a sketch of a cylinder as seen from an angle:

**Step 1:** Draw the circular edge of one end of the cylinder, as you would see it from the side.

**Step 2:** Draw two lines to show the “body” of the cylinder.  
**Step 3:** Add what you can see of the edge at the other end of the cylinder.

Alternatively, you can start by drawing two straight lines to show the body and then add curves to show the ends.

First then

Similar steps can be followed to draw a prism with a rectangular base, or even a more complicated base like a hexagon.
6.2 Make cylinders and cones

**Teaching guidelines**

Allow learners as much time as possible to explore the characteristics of cones and cylinders. It is very important that the objects are not simply things-to-be-named, but rather objects with specific characteristics.

Demonstrate the rolling of a tube, then let learners roll their own tubes.

Learners may find it quite challenging to draw a sliced cylinder (question 3). Allow them to struggle on their own for at least 5 minutes; then provide support. Some learners may produce reasonable drawings like the one on the right.

A better drawing of a sliced cylinder can be made by drawing separate short cylinders:

```
  _______  
 /       /  
|       |  
|_______|  
```

then

```
  _______  
 /       /  
|       |  
|_______|  
```

The cylindrical slices can be drawn closer together:

```
  _______  
 /       /  
|       |  
|_______|  
```

then

```
  _______  
 /       /  
|       |  
|_______|  
```

The curved surfaces can be shaded to give a better picture of the sliced cylinder:

```
  _______  
 /       /  
|       |  
|_______|  
```


**Answers**

1. Learners’ own practical work
2. (a) Circular shape
   (b) Yes, the two ends are the same.
3. The slices will also be cylinders. See the drawings above.
**Teaching guidelines**

It will definitely make it easier for learners if you first demonstrate question 4. However, it will be of great value if they can engage with the challenge of making sense of the photographs themselves, and manage to perform the actions demonstrated in the photographs. It is an opportunity to develop their graphical literacy.

**Answers**

4. Learners’ own practical work

5. (a) No

   (b) No

   (c) Here are some things learners may mention:

   - The ends of cylinders are the same while the ends of cones differ.
   - A cylinder has two identical ends while a cone has one flat end and one pointed end.
   - The shape of a cylinder viewed from the side is rectangular while the shape of a cone viewed from the side is triangular.
**Teaching guidelines**
Explain to learners that the pictures in question 6 show a particular way in which cylinders and cones can be cut into smaller pieces. It is similar to the way in which a loaf of bread is normally cut into slices:

**Mathematical notes**
The “slices” of the cylinder (see question 6) are called *circular discs*. For the cone, each slice is called a *truncated cone*.

Question 7 is quite important because it challenges learners to explore the similarities and differences between the four kinds of objects. These similarities and differences arise when one thinks about the surfaces (curved or flat) between the ends, and the ends (one pointed end and one flat end, or two identical flat ends).

**Answers**
6. The slices of the cylinder are again cylinders, of equal width. Only one slice of a cone is a cone again, the other slices are not pointed at one end, and they have different widths.
7. (a) The end surfaces of prisms and cylinders are the same, but this is not true for the ends of cones and pyramids.
   (b) Prisms and pyramids have square, rectangular or triangular bases; cylinders and cones have circular bases.

**Enrichment activity**
Ask learners to make a truncated pyramid from paper.
6.3 Make prisms and pyramids

Teaching guidelines
Again, allow learners as much time as possible to explore the characteristics of pyramids and prisms. Simply naming the different objects is not enough. Learners should be able to identify their specific characteristics.

The links between cylinders and prisms, and between cones and pyramids, should become apparent from the way learners are asked to fold cylinders into prisms, and cones into pyramids. The folding process changes the curved edges of the flat (open) ends of cones and cylinders into the polygonal ends of pyramids and prisms. Likewise, the curved surface of a cone or cylinder is folded into flat surfaces. These are triangles in the case of pyramids and rectangles in the case of prisms. Be sure to explore these links with your learners.

Picture 6 shows a square prism. It is open at the two ends.
Picture 7 shows a hexagonal prism and Picture 8 shows a rectangular prism.
Teaching guidelines
Questions 1 to 4 are designed to develop and refine the concept of the “face” of a 3-D object. It is important that you participate in the learners’ activities. When they have finished with question 1, explain to them that in the next activity (i.e. question 2) they will cut pieces of paper that can be used to close the open ends.

Answers
1. (a) to (c) Learners’ own practical work
2. Learners’ own work
3. 4 rectangular pieces and 2 square pieces of paper
4. (a) 5 faces
   (b) 3 rectangular faces and 2 triangular faces
Teaching guidelines
Learners can do question 7 at home as a project.

Answers
5. (a) 7 faces
   (b) 5 rectangular faces and 2 pentagonal faces
6. 6 rectangular faces and 2 hexagonal faces
7. Learners’ own practical work

5. (a) How many faces does a pentagonal prism have?
   (b) What are the shapes of the faces, and how many faces of each kind of shape does a pentagonal prism have?

A prism with ends like this is called a **hexagonal prism**.

6. What are the shapes of the faces, and how many faces of each kind of shape does a hexagonal prism have?

7. Make a square-based pyramid by working as shown in the pictures.
**Answers**

8. Learners' own drawings: 1 square and 4 triangles

9. (a) Pentagonal prism  
   (b) Pentagonal pyramid  
   (c) Triangular pyramid  
   (d) Rectangular prism  
   (e) Square prism or cube

---

8. Make rough drawings of the shapes of all the faces of your square-based pyramid.

These are pictures of the frames of a square-based pyramid and a hexagonal pyramid.

9. In each row below the shapes of all the faces of a 3-D object are shown. In each case name the object that has such faces.

(a)  
(b)  
(c)  
(d)  
(e)  

---
Grade 5 Term 2 Unit 7  Geometric patterns

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<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
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<td>Generating, organising and generalising data</td>
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**CAPS time allocation** 4 hours

**CAPS page references** 19 and 169 to 171

While providing opportunities to develop understanding of patterns, continuing sequences or completing tables according to a pattern also contributes to the development of the **Mental Mathematics** section of the CAPS.

**Mathematical background**

The approach in this unit is not to reduce the work on geometric patterns to numeric patterns in tables – that too – but to capitalise on the visual aspects of geometric representations as a method to find **rules** based on the **structure** of the geometric figures.

This implies that you should help learners not to determine the number of dots in a figure by counting them one by one, but to use “clever counting” by identifying appropriate larger, repeating units. Then, learners shouldn’t just count the larger units, but rather write down a **numerical expression** (calculation plan or rule) describing the number of dots. It is very important that learners should learn to withhold immediate calculation of a numerical expression – what is needed is to analyse the structure of the expression as an object, and to **generalise the structure**, not to generalise numbers.

To find a general rule for the pattern requires a second level of pattern recognition, namely recognising the structure in a series of numerical expressions: what remains unchanged (is **constant**) and what changes (is **variable**). This process is illustrated below:

Square 1 $S_1 = 4 \times 1$

Square 2 $S_2 = 4 \times 2$

Square 3 $S_3 = 4 \times 3$

Square 4 $S_4 = 4 \times 4$

$S_{100} = 4 \times 100$
7.1 Making patterns

**Teaching guidelines**
We suggest that you present this first geometric pattern activity to the class, and solve the questions interactively with input and discussion from learners.

Remind them, and illustrate, that the big idea is not to count one by one, but to use “clever counting”, i.e. to identify larger repeating units – and then also not to count the units, but to write down a **calculation plan**. We illustrate this for question 1:

It is important for learners to “see” in the given drawing of the 9 by 7 border pattern that
- in the height there are 9 blue and 8 black triangles, and
- in the width there are 7 blue and 6 black triangles.

We can now write down our calculation plan:
- Calculation plan for the no. of blue triangles: $2 \times 9 + 2 \times 7$ or $2 \times (9+7)$
- Calculation plan for the no. of black triangles: $2 \times 8 + 2 \times 6$ or $2 \times (8+6)$
- Calculation plan for total: $2 \times 6 + 2 \times 7 + 2 \times 8 + 2 \times 9$ or $2 \times (6+7+8+9)$.

Note that for all the different sizes of this border pattern there is always one less black triangle than blue triangles in the height, and one less black triangle than blue triangles in the width.

**Answers**
1. Blue: 32  Black: 28  Total: 60
2. (a) Blue: $2 \times (12+10) = 44$  Black: $2 \times (11+9) = 40$  Total: $2 \times (9+10+11+12) = 84$
   (b) Blue: $2 \times (15+10) = 50$  Black: $2 \times (14+9) = 46$  Total: $2 \times (9+10+14+15) = 96$
   (c) Blue: $2 \times (20+15) = 70$  Black: $2 \times (19+14) = 66$  Total: $2 \times (14+15+19+20) = 136$
7.2 From pictures to tables

**Teaching guidelines**

From their experience with the way of thinking used in the previous section, you should now encourage learners to continue with “clever counting” and to *use structure* and not counting.

Give learners the opportunity to explain their methods and to learn from each other. Most learners should be able to use an approach as set out below, or to follow other learners explaining what they “see” and how they describe what they are seeing by means of calculation plans. Note that question 4 asks for a calculation plan for the total number of triangles in the pattern.

**Answers**

1. (a) Length 5: 5 black triangles at the bottom and 5 at the top, and 6 + 6 blue triangles.
   
   (b) 22

2. (a) Length 50: 50 black triangles at the bottom, 50 black triangles at the top and 2 × 51 blue triangles.

   (b) No. of triangles in Length 50 = 2 × 50 + 2 × 51 = 202 or 2 × (50 + 51) = 202

3. | Length | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 60  |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of black triangles</td>
<td>2</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>10</td>
<td>12</td>
<td>14</td>
<td>120</td>
</tr>
<tr>
<td>No. of blue triangles</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>10</td>
<td>12</td>
<td>14</td>
<td>16</td>
<td>122</td>
</tr>
<tr>
<td>Total no. of triangles</td>
<td>6</td>
<td>10</td>
<td>14</td>
<td>18</td>
<td>22</td>
<td>26</td>
<td>30</td>
<td>242</td>
</tr>
</tbody>
</table>

4. 1, 2, 3, 4, 20 → 4 × 2 + 6, 10, 14, 18, 82
7.3 Extending patterns

Teaching guidelines
This section is quite challenging. We suggest that all learners should do question 1, but it is not necessary that all learners finish all the questions. It is more important to have a thorough discussion of the solution of question 1.

Answers

1. (a) 

<table>
<thead>
<tr>
<th>Size</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>30</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of purple tiles</td>
<td>2</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>10</td>
<td>12</td>
<td>60</td>
</tr>
<tr>
<td>No. of white tiles</td>
<td>10</td>
<td>14</td>
<td>18</td>
<td>22</td>
<td>26</td>
<td>30</td>
<td>126</td>
</tr>
<tr>
<td>Total no. of tiles</td>
<td>12</td>
<td>18</td>
<td>24</td>
<td>30</td>
<td>36</td>
<td>42</td>
<td>186</td>
</tr>
</tbody>
</table>

(b) Horizontal pattern: No. of purple tiles: 2 tiles are added to the previous size 
No. of white tiles: 4 tiles are added to the previous size 
Total no. of tiles: 6 tiles are added to the previous size 

Vertical pattern: No. of purple tiles: \(\text{Size number} \times 2\) 
No. of white tiles: \(\text{Size number} \times 4 + 6\) 
Total no. of tiles: \(\text{Size number} \times 6 + 6\)

2. (a) 

<table>
<thead>
<tr>
<th>Size</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>30</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of purple tiles</td>
<td>2</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>10</td>
<td>12</td>
<td>60</td>
</tr>
<tr>
<td>No. of white tiles</td>
<td>10</td>
<td>17</td>
<td>24</td>
<td>31</td>
<td>38</td>
<td>45</td>
<td>213</td>
</tr>
<tr>
<td>Total no. of tiles</td>
<td>12</td>
<td>21</td>
<td>30</td>
<td>39</td>
<td>48</td>
<td>57</td>
<td>273</td>
</tr>
</tbody>
</table>

(b) Horizontal pattern: Purple: + 2 tiles White: + 7 tiles Total: + 9 tiles 

Vertical pattern: Purple: \(\text{Size number} \times 2\) 
White: \(\text{Size number} \times 7 + 3\) 
Total: \(\text{Size number} \times 9 + 3\)

3. (a) 

<table>
<thead>
<tr>
<th>Size</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>30</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of purple tiles</td>
<td>4</td>
<td>8</td>
<td>12</td>
<td>16</td>
<td>20</td>
<td>24</td>
<td>120</td>
</tr>
<tr>
<td>No. of white tiles</td>
<td>12</td>
<td>20</td>
<td>28</td>
<td>36</td>
<td>44</td>
<td>52</td>
<td>244</td>
</tr>
<tr>
<td>Total no. of tiles</td>
<td>16</td>
<td>28</td>
<td>40</td>
<td>52</td>
<td>64</td>
<td>76</td>
<td>364</td>
</tr>
</tbody>
</table>

(b) Horizontal pattern: Purple: + 4 tiles White: + 8 tiles Total: + 12 tiles 

Vertical pattern: Purple: \(\text{Size number} \times 4\) 
White: \(\text{Size number} \times 8 + 4\) 
Total: \(\text{Size number} \times 12 + 4\)
7.4 Using patterns to solve problems

Teaching guidelines
This is an interesting real-life problem. It may be somewhat time-consuming, but once
learners get the hang of it, it should not be difficult. However, in order to solve the
problem and to develop an understanding of structure, it is important that all learners do
all the plans.

Mathematical notes
To calculate the number of people for a large number of tables, it is useful to find a
calculation plan for each of Plans 1 to 4.
Again, it is not really difficult, and it certainly is not more challenging than finding the
perimeter of the figures (with the people as “sides” or side lengths)!
The way to “see” structure is to understand that in Figure 4 we try to see a unit of 4, in
Figure 3 we try to see a unit of 3 in the same way, in Figure 2 a unit of 2 and so on, as
illustrated here for Plan 1:

\[
\begin{align*}
1 \text{ table} & \quad 2 \text{ tables} & \quad 3 \text{ tables} & \quad 4 \text{ tables} \\
2 \times 1 + 2 & \quad 2 \times 2 + 2 & \quad 2 \times 3 + 2 & \quad 4 \text{ at top, } 4 \text{ at bottom, plus } 2
\end{align*}
\]

The challenge is then to generalise the structure so that we can, for example, easily
calculate how many people will sit at 15 small tables:

\[
\begin{align*}
T_1 &= 2 \times 1 + 2 \\
T_2 &= 2 \times 2 + 2 \\
T_3 &= 2 \times 3 + 2 \\
T_4 &= 2 \times 4 + 2 \\
\vdots \\
T_{15} &= 2 \times 15 + 2
\end{align*}
\]

So, \( T_{15} = 2 \times 15 + 2 \)
The calculation plan as a flow diagram also helps us to find unknown input values by using
inverse operations in reverse order, for example:

\[
\begin{align*}
? - 2 \times \frac{2}{2} - 2 & \rightarrow 46 \\
22 & \leftarrow \frac{2}{2} + 2 \rightarrow 46
\end{align*}
\]
We briefly outline the thinking to find the rule for Plan 3 using visual structure:

<table>
<thead>
<tr>
<th>Table 1</th>
<th>Table 2</th>
<th>Table 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 x 1 + 4</td>
<td>2 x 2 + 4</td>
<td>2 x 3 + 4</td>
</tr>
</tbody>
</table>

So T15 = 2 x 15 + 4

**Answers**

1. (a) Each square table can seat two people opposite each other, plus one person at each end of the combined row of tables (the “long table”).
   
   (b) 1, 2, 3, 4, 5, 15, 22
   
   (c) 4, 6, 8, 10, 12, 32

2. (a) Each table can seat two people at the short ends. And 6 people can sit at the other two sides of the combined row of tables.
   
   (b) 1, 2, 3, 4, 5, 15, 20
   
   (c) 8, 10, 12, 14, 16, 36, 46

3. (a) Each table can seat two people at the short ends. And 4 people can sit at the other two sides of the combined row of tables.
   
   (b) 1, 2, 3, 4, 5, 15, 21
   
   (c) 6, 10, 12, 14, 16, 34, 46

4. (a) Each table can seat four people opposite each other, plus one person at each end of the combined row of tables.
   
   (b) 1, 2, 3, 4, 5, 11
   
   (c) 6, 10, 14, 18, 22, 62, 46

5. Plan 4
Grade 5 Term 2 Unit 8  

Symmetry

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</tr>
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<td>8.2 Finding lines of symmetry</td>
<td>Identifying lines of symmetry; identifying symmetrically located points</td>
<td>183 to 184</td>
</tr>
<tr>
<td>8.3 Moving figures to make symmetries</td>
<td>Identifying symmetries resulting from moving a shape in various ways, and identifying absence of symmetry</td>
<td>185 to 186</td>
</tr>
</tbody>
</table>

**Mathematical background**

Symmetry occurs when a shape or design can be seen as consisting of two “mirror images”. This means that a straight line, called the line of symmetry, can be drawn through the shape or design in such a way that if we fold along the line, every single line and point on one side of the line lies on top of its twin on the other side of the line – without exceptions. Some shapes have two or more lines of symmetry.

Symmetry is an intuitive concept that plays an important role in art and design – this forms the beginning of the unit. It is followed by a more formal look into symmetry – the symmetry of points. This develops the spatial skill of “seeing” symmetry. In the last section, learners have to identify symmetries and absence of symmetry in a variety of compound shapes.

This quadrilateral possesses no symmetry at all.  
This quadrilateral has only one line of symmetry.  
This quadrilateral has two lines of symmetry.  
This quadrilateral has four lines of symmetry.  
All the lines that pass through the centre of a circle are lines of symmetry.
8.1 Drawing symmetrical figures

Teaching guidelines
The purpose of question 1 is to let learners physically experience symmetry by making symmetrical sets of movements with their two hands, or two successive sets of movements with the same hand. Learners may have to try repeatedly before they get it right. Allow them to share their experiences.

You can draw a simple symmetrical figure on the board to demonstrate what learners are required to do in question 1.

Another way to let learners experience symmetry is to give each learner a piece of cardboard or thick paper that can serve as a template for tracing a figure.

Let learners trace the outline of the template, then pick it up, flip it over and put it down again. They must try to put it down in a position that will produce symmetry when the outline is traced again, as shown below. Let learners then draw the approximate line of symmetry, without a ruler. (It is not accuracy that is important now, it is the ability to visualise where the line of symmetry is.) Note that the broken line figure below does not form a symmetrical design with the tracing on the left – it was shifted down.

Answers
1. Practical activity
2. Pictures with a fold line that is a line of symmetry: (a), (c)
Teaching guidelines
You can do A and C on the board as examples – plot only the necessary dots beforehand.

We have provided dotted paper in the Addendum on page 415. However, it is not critical to have dotted paper. Working on lined paper is almost as good and will still allow the idea of symmetry to develop.

Answers
3. (a) Learners' own work
(b)

3. The figures show what one hand drew.
(a) Redraw the figures on dotted paper.
(b) Complete the figures to show what the other hand must draw to make a symmetrical figure.
8.2 Finding lines of symmetry

**Mathematical notes**
Learners’ individual spatial sense is challenged here, building on the challenges mentioned in the previous section.

**Answers**

1. (a) 
   ![Diagram](image1)
   (b) 
   ![Diagram](image2)
   (c) 
   ![Diagram](image3)
   (d) 
   ![Diagram](image4)

2. (a) 
   ![Diagram](image5)
   (b) 
   ![Diagram](image6)

1. Where must you fold the square to make the dots fall onto each other? Trace each figure onto a clean page and draw a line of symmetry. Try to be accurate.

   ![Diagram](image7)

2. Where must you fold the triangle to make the dots fall onto each other? Trace each figure onto a clean page and draw a line of symmetry. Try to be accurate.

   ![Diagram](image8)
3.  (a)  

(b)  

(c)  

(d)  

(e)  

(f)  

3. Lines of symmetry have been drawn in red on the figures. Trace each figure onto a clean page and draw the missing dots. Try to be accurate.
8.3 Moving figures to make symmetries

Teaching guidelines
The questions in this section require learners to identify symmetries and lines of symmetry (e.g. questions 1 and 2) as well as the absence of symmetry (question 3). The section hence provides for consolidation and refinement of the knowledge learners acquired in Sections 8.1 and 8.2.

The section also provides learners with experiences of the transformations they will learn about in Term 3 Unit 7: translations (questions 1 to 3), reflections (questions 4, 5 and 6(b)) and rotations (questions 4, 5 and 6(c)). However, there is no need for learners to name and engage formally with these transformations now: they only have to provide descriptions in their own language of how the hexagon was moved to form the repetitive designs (patterns) in the various questions.

The explicit references to transformations in the mathematical notes below and on the next page are provided as background orientation for teachers, not with the intention that this should be discussed with learners at this stage.

Mathematical notes
When a symmetrical shape is shifted along the line of symmetry without turning it, the symmetry is repeated and a compound symmetrical design is formed, as demonstrated in the designs in questions 1 and 2.

Shifting a symmetrical shape along a line other than the line of symmetry does not create more symmetries, as shown in question 3.

Answers
1. (a) The hexagon was moved 5 squares to the right.
   (b) The red line
2. (a) The hexagon was moved 4, then 5, then 6 squares to the right.
   (b) The red line
   (c) Many learners may say “yes”, which is wrong. Allow learners to do question 3 to realise that shifting a symmetrical figure along a straight line does not necessarily produce more symmetries.
3. (a) The hexagon was moved 6 squares to the right and 1 square down.
   (b) None
Mathematical notes
A symmetrical design is created when a shape is flipped over. The design in question 4(a) can be produced by flipping the hexagon over the black vertical broken line, then over the green broken line, then over the blue broken line.

The symmetrical design in question 4(a) can also be produced by turning (rotating) the symmetrical hexagon through \(180^\circ\), around the intersection of the extended axis of symmetry (the red broken line) and the vertical broken lines.

Answers
4. (a) The hexagon can be “flipped over” to the right, and again and again. Learners may use different language.
   The pattern can also be produced by turning the hexagon halfway around, around the points where the horizontal and vertical broken lines cross.
   (b) The red, black, green and blue lines
   (c) The black and blue lines

5. (a) The hexagon can be shifted to the right and down and flipped over to the right. Alternatively, it can be turned halfway around the points where the horizontal and vertical broken lines cross.
   (b) None

6. (a) No symmetries
   (b) The group of four hexagons is symmetrical around the green broken line.
      The two hexagons on the left are symmetrical around the black broken line, and the two hexagons on the right are symmetrical around the blue broken line.
   (c) No symmetries
Grade 5 Term 2 Unit 9  Whole numbers: Division

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**CAPS time allocation**  
8 hours

**CAPS page references**  
13 to 15 and 172 to 173

**Mathematical background**

Division is applicable to three different kinds of situations:

- Situations in which a quantity is shared (divided) into a **given number of parts** of unknown equal size – thus, a situation in which the number of equal parts is known but the size of each part is unknown.
- Situations in which a quantity is shared (divided) into an unknown number of **parts of given equal size** – thus, a situation in which the number of equal parts is unknown but the size of each part is known.
- Scaling situations where two quantities of the same kind are compared in terms of their **ratio**, not the difference between the two quantities.

The first step in division is to **estimate** what to multiply the divisor by to reach an answer smaller than the dividend.

For example, when calculating $6247 \div 87$ one may estimate that $50 \times 87$ will be smaller than 6247. Since $50 \times 87 = 4350$ (half of $100 \times 87$, which is 8700), in this case it proves to be a good estimate.

The next step could now be $20 \times 87 = 1740$, leading to $70 \times 87 = 4350 + 1740 = 6090$, which is already close to 6247. One may add 87 to get closer: $71 \times 87 = 6090 + 87 = 6177$.

Since $6247 - 6177 = 70$, the answer is $6247 \div 87 = 71$ remainder 70. This may also be expressed by writing $6247 = 71 \times 87 + 70$. 

9.1 Build multiplication knowledge for division

**Teaching guidelines**

The first step in dividing with multi-digit numbers is to make an estimate that can serve as a starting point (see “Mathematical background” on the previous page). Hence, questions 1 and 2 provide learners with opportunities to strengthen their estimation skills.

You may start the lesson by asking learners to study questions 1(a)–(h) and 2(a)–(j) and to then write down estimated answers. Having to estimate answers will help learners to apply their minds to understand given situations, which is an essential element of problem solving. Then ask them to check their answers by using multiplication.

Once learners have started working on questions 1 and 2, you may suggest that they revise their estimates as they progress.

**Answers**

In questions 1 and 2 there is sometimes more than one solution. Consider learners’ answers.

1. (a) 475; 476; 477; 478; 479  
   (b) 317; 318; 319  
   (c) 238; 239  
   (d) 190; 191  
   (e) 159  
   (f) 136; 137  
   (g) 119  
   (h) 106

2. (a) 95; 96  
   (b) 87; 88  
   (c) 80  
   (d) 74  
   (e) 68; 69  
   (f) 64  
   (g) 60  
   (h) 56; 57  
   (i) 53  
   (j) 50; 51

3. (a) 460  
   (b) 860  
   (c) 680  
   (d) 1 110

**UNIT 9
WHOLE NUMBERS:
DIVISION**

9.1 Build multiplication knowledge for division

1. Find the missing number in each case. You may estimate, check and correct.
   (a) \( 2 \times \ldots \) is at least 950, but less than 960.
   (b) \( 3 \times \ldots \) is at least 950, but less than 960.
   (c) \( 4 \times \ldots \) is at least 950, but less than 960.
   (d) \( 5 \times \ldots \) is at least 950, but less than 960.
   (e) \( 6 \times \ldots \) is at least 950, but less than 960.
   (f) \( 7 \times \ldots \) is at least 950, but less than 960.
   (g) \( 8 \times \ldots \) is at least 950, but less than 960.
   (h) \( 9 \times \ldots \) is at least 950, but less than 960.

2. Find the missing number in each case.
   (a) \( 10 \times \ldots \) is at least 950, but less than 970.
   (b) \( 11 \times \ldots \) is at least 950, but less than 970.
   (c) \( 12 \times \ldots \) is at least 950, but less than 970.
   (d) \( 13 \times \ldots \) is at least 950, but less than 970.
   (e) \( 14 \times \ldots \) is at least 950, but less than 970.
   (f) \( 15 \times \ldots \) is at least 950, but less than 970.
   (g) \( 16 \times \ldots \) is at least 950, but less than 970.
   (h) \( 17 \times \ldots \) is at least 950, but less than 970.
   (i) \( 18 \times \ldots \) is at least 950, but less than 970.
   (j) \( 19 \times \ldots \) is at least 950, but less than 970.

3. How much is each of the following?
   (a) \( 23 \times 20 \)  
   (b) \( 43 \times 20 \)  
   (c) \( 17 \times 40 \)  
   (d) \( 37 \times 30 \)
Teaching guidelines
When learners start with question 4, suggest that they make estimates as in questions 1 and 2, and then check their answers by doing multiplication. They may observe that the answers for question 3 can help them to quickly produce the answers for question 4. This is fine.

Answers
4. (a) 23  (b) 20  (c) 20  (d) 43

5. (a) \(460 + 115 = 575\)  (b) 575  (c) \(690 + 92 = 782\)  (d) 782

Notes on questions
Like questions 3 and 4, but in a different way, question 6 demonstrates the relationship between multiplication and division.

Thus, in question 6(a) learners may say \(18 \times 24 = 432\) or \(24 \times 18 = 432\).

In question 6(b) learners know that the number of rings is neither increased nor decreased, therefore: \(432 \div 12 = 36\). This means that \(12 \times 36 = 432\). This implies that Nathi will rearrange the rings into 36 rows of 12 rings in each.

Answers
6. (a) 432  (b) 36  (c) 54  (d) 48

7. 30

8. 20
9.2 Use multiplication facts to do division

Teaching guidelines
The contexts described in Situations A and B may be utilised as a platform for learners to strengthen their knowledge of how to do division with multi-digit numbers. For this to happen, it is critical that learners engage with the context in their minds. To help them do that, you may bring a box to class. Say to learners that you want to put 24 apples in the box. Ask them to estimate how many such boxes with 24 apples each can be made up from a total of 774 apples. Let them write their estimates down.

To help learners to engage in their minds with Situation B, you may say that you would like 24 of them to each take some apples home. State that you have 774 apples available, and ask them to estimate how many apples each of the 24 lucky learners will get to take home, if they share the apples equally among them. Let them write their estimates down.

Now ask learners how much \(24 \times 2\) is, then how much \(24 \times 10\) is, as well as \(24 \times 20\) and \(24 \times 30\). Confirm the correct answers and let learners write all the answers down, in the form \(24 \times 2 = 48,\ 24 \times 10 = 240,\ etc.\) (This is what is sometimes called a “clue board”.)

Remind learners of Situations A and B again and of the estimates they wrote down. Suggest that they use the multiplication facts for 24 that they have just written down to check and revise their estimates for Situations A and B. Only then let them do question 1.

Answers

1. Situation A:
   \[24 \times 30 = 720\] and \(24 \times 2 = 48\), hence \(24 \times 32 = 720 + 48 = 768\)
   \[774 - 768 = 6\]
   Therefore 32 boxes are needed (and there will be 6 loose apples left over).

   Situation B:
   Each household can get 32 apples (and there will be 6 apples left over).

Teaching guidelines
Let learners engage with Situations C and D by themselves. They do not have to read the tinted passage at the top of page 190 of the Learner Book.
Teaching guidelines

If learners do not seem to make progress with Situations C and D, you may ask them to write down some multiplication facts for 27, like they did for 24. Then they should check whether these facts could help them to make good estimates with respect to Situations C and D.

The word “remainder” is not a new term but some learners may not know it or its implications. Therefore it is important to explain it and demonstrate what it means with a simple example such as the following:

\[ 25 ÷ 4 = 6 \text{ remainder } 1. \] The understanding here is \( 4 \times 6 + 1 = 25. \)

The amount left over after performing division is called a remainder.

Answers

2. \[ 10 \times 33 = 330 \text{ and double } 330 \text{ is } 660 (\text{so } 20 \times 33 = 660) \]
   Half of 330 is \( 5 \times 33 = 165 \)
   \[ 660 + 165 = 825 \] (That is \( 25 \times 33 \))
   \[ 825 + 33 = 858 \] (That is \( 26 \times 33 \))
   \[ 870 - 858 = 12 \]
   Answer: \( 870 + 33 = 26 \text{ remainder } 12 \)

3. (a) 22 rem 9  (b) 8 rem 1  (c) 32 rem 12  (d) 7 rem 2
9.3 Find answers for practical questions

Notes on questions

Question 1 is designed to support learners who have not yet developed a strong sense of division.

(Learners who do already have a strong understanding of division may quickly calculate $24 \times 16 = 384$ and proceed to add another 16 boxes to bring the total to $384 + 384 = 768$ and then add a smaller number of boxes. Alternatively, such learners may add 20 boxes (480 cans) to the first 384 cans to reach 864 cans, then add 5 boxes (half of 10) to reach $864 + 120 = 984$. This would reveal that to reach 1000 cans, a total of 26 boxes must be added and there will then be a surplus of 8 cans. Learners who figure this out by themselves may continue on their own with question 2 and the subsequent questions.)

Question 1 is deliberately designed to be understood as: “How many groups of 24 cans must be added to $16 \times 24$ to make up 1000 cans?” If learners do not make quick progress, you may ask them how many boxes are already there, and to calculate how many cans there are in these boxes. If learners do this but do not proceed further on their own, you may ask them how many cans they will have in total if they add another 20 boxes.

Once all learners have produced the answer for question 1 (26 boxes plus a box of 16 cans), you may point out that they have actually calculated $616 \div 24$ and obtained the answer 25 remainder 16. Highlight to them that they have multiplied (and added) in order to find the answer to a division problem, and suggest that they do this again when they do questions 2, 3 and 4.

Answers

1. $1000 - 384 = 616$ more cans
   $616 = 25 \times 24 + 16$, so 25 boxes with 24 cans and 1 box with 16 cans are needed.
   Alternatively: $1000 \div 24 = 41$ boxes and remainder 16 “loose cans”
   $41$ boxes $- 16$ boxes $= 25$ full boxes, so 25 boxes + 16 loose cans are needed.

2. (a) $1000 = 23 \times 43 + 11$, which means 23 truckloads of 43 bags and 1 truckload of 11 bags in total.
   (b) $500 = 11 \times 43 + 27$, which means 11 truckloads of 43 bags and 1 truckload of 27 bags in total.

3. (a) 17 chickens  (b) 8 chickens  (c) 10 chickens  (d) 18 chickens

4. $851 = 23 \times 37$, which means 37 trees in each row.
**Notes on questions**
The solutions to question 6 provide learners with an opportunity to learn that quantities may not always be shared into equal parts (like in question 5).

**Answers**

5. Total number of learners is $76 + (68 + 68) + 59 + 74 = 345$.  
   $345 ÷ 5 = 69$  
   There will be 69 learners on each bus.

6. Learners’ answers will differ.
   (a) Three examples:
   - $634 = 8 \times 75 + 34$, which means 8 buses with 75 learners and 1 bus with 34 learners.
   - $634 = 4 \times 80 + 3 \times 85 + 1 \times 59$, which means 4 buses with 80 learners, 3 buses with 85 learners and 1 bus with 59 learners.
   - $634 = 89 + 87 + 85 + 80 + 75 + 74 + 60$, which means a different number of learners on each of the nine buses.

(b) Three examples:
   - $634 = 8 \times 70 + 1 \times 74 \rightarrow 8$ buses with 70 learners and 1 bus with 74 learners
   - $634 = 8 \times 71 + 1 \times 66 \rightarrow 8$ buses with 71 learners and 1 bus with 66 learners
   - $634 = 8 \times 72 + 1 \times 58 \rightarrow 8$ buses with 72 learners and 1 bus with 58 learners

(c) One example:
   - $634 = 5 \times 71 + 3 \times 69 + 1 \times 72 \rightarrow 5$ buses with 71 learners, 3 buses with 69 learners and 1 bus with 72 learners

7. It won’t work to only look at the given prices of buses and then draw conclusions. Learners must first determine the number of buses per option by dividing 832 learners by the number of seats in each kind of bus. The quotient must be multiplied by the amount as defined by the option.

   Option A:  $832 ÷ 23 = 36$ remainder 4, so 37 buses are needed.  
   Thirty-seven buses will cost $37 \times \text{R210} = \text{R7 770}$.

   Option B:  $832 ÷ 92 = 9$ remainder 4, so 10 buses are needed.  
   Ten buses will cost $10 \times \text{R828} = \text{R8 280}$.

Option A is therefore cheaper.
9.4 Multiply and divide

Mathematical notes
This section provides learners with opportunities to become aware of constant ratios between quantities. This is emphasised from question 7 onwards.

Teaching guidelines
It is critical that learners engage with the structure of Thandi’s beaded mat. To ensure this, you may ask them to count the number of beads of each colour before they start working on the questions. The numbers are:

7 blue beads  14 yellow beads  21 green beads  28 red beads
35 pink beads  42 brown beads

Questions 1 to 6 involve multiplication and division only.

Answers
1. Learners may approach this in different ways.
   Some learners may see: $7 \times 21 = 147$ beads.
   Some may see: $7 + 14 + 21 + 28 + 35 + 42 = 147$ beads.
2. 1 260 red beads
3. (a) 21 mats; 15 beads left over    (b) 147    (c) 588
4. (a) 19 mats; 2 beads left over    (b) 399    (c) 665
5. (a) 322 yellow beads   (b) 805 pink beads
6. 882 ÷ 147 = 6 mats, so she used:
   42 blue beads
   84 yellow beads
   126 green beads
   168 red beads
   210 pink beads
   252 brown beads
Teaching guidelines
The language construction in question 7 conveys the idea of a ratio. There is no need to introduce the word “ratio” before learners have completed question 7.

Question 8 is more demanding than question 7. It may be necessary to do question 8(a) with the whole class, after learners have engaged with it for a while by themselves.

Answers
7. (a) True (b) True (c) False (d) False
   (e) False (f) True (g) True
8. (a) 2 to 5 (b) 5 to 2 (c) 4 to 6 (or 2 to 3)
   (d) 1 to 4 (e) 4 to 1
**Answers**

9.  
   (a) 60 yellow beads  
   (b) 450 brown beads  
   (c) 80 red beads  

10. 360 blue beads; 120 yellow beads; 160 red beads  

11. The ratios are the same for all three mats:  
    
    |   blue   |   yellow   |   red   |   green   |   pink   |   brown   |
    |-------|-------|-------|-------|-------|-------|
    |   5   |    3  |    4  |    3  |    4  |    2   |

Cindy also makes beaded mats. In each of Cindy’s mats:  
- yellow and red beads are in the ratio 3 to 4,  
- blue and brown beads are in the ratio 2 to 5, and  
- yellow and blue beads are in the ratio 1 to 3.  

9. There are 180 blue beads in one of Cindy’s mats.  
   (a) How many yellow beads are there in this mat?  
   (b) How many brown beads are there in this mat?  
   (c) How many red beads are there in this mat?  

10. One day, Cindy has no beads left. She buys 900 brown beads and decides to use all 900 brown beads in one large mat. How many blue, yellow and red beads will she have to buy for this mat?  

Here you can see three mats that Belinda made. Look at them carefully and then answer question 11.  

![Mats A, B, C](image_url)

11. Describe Belinda’s three mats by stating all the ratios between the numbers of beads of different colours.
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**CAPS time allocation** 5 hours

**CAPS page references** 16 and 176 to 177

**Mathematical background**

Fractions are used for different purposes:

- They are used to describe parts of wholes, for example: “5 eighths of the floor is covered with tiles.”
- They are used to describe parts of collections and quantities. For example, if there are 120 people at a wedding and 72 of them are women, we can say 3 fifths of the people at the wedding are women. If somebody says “I spend 3 tenths of my income on housing” and she has an income of R8 000, she spends R2 400 on housing.
- They are used as parts of measuring units, for example: “The wall is 4 and 7 tenths of a metre long.”

Although two number symbols are used to write a fraction in the common fraction notation, for example 5 eighths is represented by the symbol $\frac{5}{8}$, any fraction is a single number. The fractions lie between the whole numbers on the number line.

Mixed numbers can be added and subtracted in two ways:

- by converting the mixed numbers to improper fractions
- by subtracting or adding the whole number parts and the fraction parts separately, replacing one fraction with a useful equivalent in the case of subtraction (if necessary).
1.1 Parts of wholes and parts of collections

**Mathematical notes**
Understanding fractions as part of units of measurement provides the foundation for understanding the decimal notation. It helps us to see fractions as “numbers between the whole numbers”, which we can represent on the number line. Decimal fractions are only introduced in Grade 6.

**Teaching guidelines**
Allow learners to discuss fraction names and provide opportunities for them to say the fraction names properly and fully: \( \frac{7}{10} \) is 7 tenths, not “7 over 10”. If you let learners describe fractions like in the latter, you risk teaching the misconception that a fraction is one whole number over another whole number. It is not. Make sure learners know the difference between the numerator and the denominator. The denominator indicates the kind of fraction part, which depends on the number of equal parts into which the object or unit of measurements is divided.

When we use a number (e.g. 5 eighths) to indicate how long, in metres, a certain piece of string is, we think of a metre as divided into eight equal parts and the string being as long as five of these parts.

Ensuring that learners say the fraction names properly may help to combat the misconception described above. Asking learners to write fractions in words and to represent them with neat, quickly-made fraction strips are powerful ways of promoting understanding of fractions.

**Notes on questions**
In question 3 the logic for (a) and (b) is different to the logic for (c) and (d). In (a) and (b) the bigger the denominator, the smaller each part is, so one twelfth is smaller than one tenth, and so on. In (c) and (d) we must look at both the numerator and the denominator. Five parts out of six is bigger than four parts out of five, as it is closer to the whole. Drawing two fraction strips will help to illustrate this.

**Answers**
1. (a) \( \frac{1}{9} \)
   (b) I counted how many equal parts there are (i.e. 9) and then I counted the number of red parts (i.e. 1). So 1 out of 9 parts is red, which means \( \frac{1}{9} \) of the strip is red.
2. (a) \( \frac{2}{5} \)   (b) \( \frac{4}{10} \)   (c) \( \frac{1}{6} \)   (d) \( \frac{4}{12} \)   (e) \( \frac{1}{4} \)   (f) \( \frac{7}{8} \)   (g) \( \frac{1}{3} \)
3. (a) \( \frac{4}{10} \)   (b) \( \frac{1}{5} \)   (c) \( \frac{5}{6} \)   (d) \( \frac{7}{8} \)
Teaching guidelines
Before learners do question 6, refer to the second tinted passage on page 199 of the Learner Book. Make learners aware of the fact that the three red parts in the tinted passage are not together, but they still make 3 elevenths.

Take the class through the explanation in the tinted passage on page 200 before doing question 8. See if anybody offers the equivalent fraction. \( \frac{1}{3} \) is more compelling because of the way the rectangle has been coloured in.

Notes on questions
It would be valuable to discuss question 8 thoroughly in class, once learners have responded to it individually. It will promote understanding of equivalent fractions.

Answers
4. (a) Jenny  
   (b) \( \frac{1}{8} \) is bigger than \( \frac{1}{8} \); the same logic as in 3(a).

5. (a) \( \frac{1}{12} \)  
   (b) Agree; four of the twelve equal parts are red, and they make up \( \frac{1}{3} \) of the rectangle. Learners may give different explanations of why they agree.  
   (c) Agree; even though the four red parts are not together they still make up four of the twelve parts of the rectangle, which is the same as \( \frac{1}{3} \) of the rectangle. Learners may give different explanations of why they agree.

6. (a) Agree; once again there are four red squares (as in question 5).  
   (b) If we divide the rectangle into 3 equal parts, 4 of the small red blocks will fit into \( \frac{1}{3} \) of the rectangle. This is the same question as 5(b), just perceptually different.

7. (a) Agree; in this case it is very easy to see the four blocks out of 12.  
   (b) The rectangle is divided into 12 equal parts and 4 of the small red blocks are four twelfths of the whole, but here it is very tempting to say \( \frac{1}{3} \).  
   (c) Yes; it was just another way of saying \( \frac{1}{3} \).  
   (d) Yes; different fractions can be used to describe the same part.

8. (a) Agree  
   (b) The rectangle is divided into 9 small blocks and 3 of the 9 blocks are coloured red.
**Teaching guidelines**

Before learners do question 9, ask them what they can say about the four rectangles. They may be able to say immediately that the red and yellow take up equal space in the rectangles. If they do not say this immediately, ask them again after they have done (a) to (d). This is a nice visual representation of equivalent fractions.

Note that question 10 is a little different. The three quarters or three fourths are not so obviously displayed. The whole in (a) is bigger than the whole in (c).

When learners have finished question 11, go through the first tinted passage with the whole class. The information may seem repetitive, but must be stressed. Explain to them that in question 10, for example, there are four parts in the whole. In the fraction \( \frac{3}{4} \), 4 is the denominator for the rectangles, and 3 is the numerator and tells us how many parts there are in this particular fraction. The tinted section at the bottom of the page reinforces this concept.

**Answers**

9. (a) \( \frac{8}{20} \) or \( \frac{2}{5} \)  (b) \( \frac{6}{15} \) or \( \frac{2}{5} \)  (c) \( \frac{4}{10} \) or \( \frac{2}{5} \)  (d) \( \frac{2}{5} \)

10. (a) \( \frac{3}{4} \)  (b) \( \frac{3}{4} \)  (c) \( \frac{3}{4} \)

11. (a) No
   (b) A quarter of a bigger chunk is more than a quarter of a smaller chunk. The rectangles are different sizes.

12. (a) \( \frac{1}{8} \)
    (b) \( \frac{3}{8} \)
1.2 Equivalent fractions

Teaching guidelines

Remind learners again that the bigger the denominator, the smaller the part: one third (\(\frac{1}{3}\)) of a loaf of bread is a much bigger piece than \(\frac{1}{9}\) of the loaf.

Learners should do the questions individually without help. Make sure that they understand what is asked in the different questions.

After questions 1 and 2, go through the tinted passage with the class and confirm that the quantity of cake remains the same, no matter into how many smaller parts you cut it.

Answers

1. (a) \(\frac{1}{3}\) (b) \(\frac{1}{6}\) (c) \(\frac{1}{9}\)
   (d) two sixths; three ninths; four twelfths

2. (a) \(\frac{1}{8}\) (b) \(\frac{1}{12}\)
   (c) two eighths; three twelfths; four sixteenths

The three fractions that you named as equivalent all describe the same quantity, namely one third in question 1 and one quarter in question 2. However, their denominators differ because in each case the fraction was cut up into smaller parts.
Notes on questions
In question 3 we have green strips with light and dark sections. The pink fraction strip helps us to measure these different sections, as well as each whole strip. Question 3(a) has been done for learners to get them started. By now they should know to count the length of the whole strip first.

In responding to question 3(a), some learners may describe the green strip as \( \frac{3}{24} \). The light green strip in (a) is indeed \( \frac{3}{24} \) as long as the pink strip, which is divided into 24 equal parts. However, the question requires expressing the light green strip as a fraction of the green strip (8 segments long), not of the pink strip. The light green strip in (a) is \( \frac{3}{8} \) of the green strip – it forms part of the green strip.

Discussion of the fact that each light green strip on the diagrams can be expressed in two ways as a fraction can promote deeper understanding of fractions:

In question 3(a), \( \frac{3}{8} \) of the green strip = \( \frac{3}{24} \) of the pink strip.

In question 4 the notion of equivalent fractions is taken further. Sometimes more than one step is needed to find the answer.

In question 5, \( \frac{5}{12} \) has no equivalent fraction within the range of fractions learners now work with, yet some learners may move ahead in their minds and state \( \frac{10}{24} \). You may bring this to the attention of the whole class when they have all finished question 5, and ask the learners who gave this answer to explain their thinking.

Answers
3. (a) \( \frac{3}{8} \) (b) \( \frac{7}{10} \) (c) \( \frac{5}{7} \) (d) \( \frac{8}{11} \)
   (e) \( \frac{4}{5} \) (f) \( \frac{8}{12} \) (g) \( \frac{2}{3} \) (h) \( \frac{6}{9} \)
4. (a) True (b) False (c) True (d) True
   (e) True (f) True (g) True
5. (a) \( \frac{5}{12} \) (also \( \frac{10}{24} \); see “Notes on questions” above)
   (b) \( \frac{3}{12} \) or \( \frac{1}{4} \) (c) \( \frac{3}{12} \) or \( \frac{1}{4} \) (d) \( \frac{6}{12} \) or \( \frac{1}{2} \) (e) \( \frac{4}{12} \) or \( \frac{1}{3} \)
   (f) \( \frac{6}{12} \) or \( \frac{1}{2} \) (g) \( \frac{4}{12} \) or \( \frac{1}{3} \) (h) \( \frac{5}{12} \)
1.3 Parts of a measuring unit

Teaching guidelines

Question 1 is specifically intended to help learners make sense of addition of fractions. We call this “unit of measurement” the Brownstick, just to show it is something we have invented to help us measure. It is arbitrary (do not use this word with the learners). The important teaching point is that fractions help us to measure accurately.

Go through the tinted section of the page. The blue strip fits perfectly, so we have no problems there. But now there is the challenge of the red strip. Ask learners how they would measure the part that is longer than one Brownstick but shorter than two Brownsticks.

We can divide our Brownstick into equal fractions. Two possibilities are offered. The first example is division into tenths; the second is division into twelfths. The second one gives us an accurate yardstick for measuring: one and 5 twelfths of a Brownstick.

Notes on questions

Looking at question 1 the class have to identify the fraction parts in order to answer the questions. Question 1(c) can be answered by counting the fraction parts, or else by visualising moving the blue strip leftwards.

Answers

1. (a) Red: 7 eighths of a Brownstick
    Blue: 5 eighths of a Brownstick
(b) 1 1/8 of a Brownstick
(c) The two strips together are 1 1/2 Brownsticks long.
Notes on questions
Questions 2 and 3 provide practice in adding fractions and experiences of equivalent fractions.

Although question 3(a) can be done without consciously thinking of division, it provides learners with an experience of a sharing situation involving fractions.

In question 4, notice that the Brownstick is divided into twelfths, but every second twelfth has a longer line, helping the visual perception of sixths.

Question 5 is practice in forming equivalent fractions.

Answers
2. (a) Blue: $\frac{3}{5}$ or $\frac{6}{10}$ of a Brownstick
   Red: $\frac{4}{10}$ or $\frac{2}{5}$ of a Brownstick
   Green: $\frac{2}{5}$ of a Brownstick
   Yellow: $\frac{3}{5}$ of a Brownstick

(b) 1 Brownstick
(c) 1 Brownstick

3. (a) $\frac{10}{10}$ = 1. Accept either or both.
   (b) $\frac{5}{5}$ = 1. Accept either or both.
   (c) $\frac{7}{10}$
   (d) $\frac{4}{5}$
   (e) $\frac{11}{10}$ = $1\frac{1}{10}$. Accept either or both.
   (f) $\frac{7}{5}$ = $1\frac{2}{5}$. Accept either or both.

4. (a) Both are $1\frac{1}{6}$ of a Brownstick or $1\frac{8}{12}$ of a Brownstick long.
   (b) $\frac{2}{5}$ of a Brownstick or $\frac{4}{12}$ of a Brownstick
   (c) $1\frac{3}{12}$ of a Brownstick

5. (a) 2 twelfths
   (b) 4 twelfths
   (c) 2 tenths
   (d) 6 eighths
1.4 Combining, comparing and ordering fractions

Mathematical notes
In this unit we extend the interpretation of fractions as measures, which we have just dealt with in Unit 1.3, to develop learners’ understanding of fractions as numbers. Questions 1 to 4 are a very simple introduction.

Notes on questions
In question 4 learners must recognise four eighths as equivalent to one half.

In question 5(a) attention must be paid to the numerator, the denominator as well as equivalent fractions. The class might need your help here, but let them try first. In question 5(b) learners must realise when both the numerator and denominator are large, the fraction is larger. There is an easy visual pattern here.

Ask learners in question 6 how they worked out their answers here. Did they draw a fraction strip? Or did they use some other way?

Answers
1. \( \frac{5}{10}; \frac{6}{10}; \frac{7}{10}; \frac{8}{10}; \frac{9}{10}; 1; \frac{1}{10}; \frac{2}{10}; \frac{3}{10}; \frac{4}{10}; \frac{5}{10}; \frac{6}{10}; \frac{7}{10}; \frac{8}{10}; \frac{9}{10}; 2 \)
2. \( \frac{1}{8}; \frac{2}{8}; \frac{3}{8}; \frac{4}{8}; \frac{5}{8}; \frac{6}{8}; \frac{7}{8}; 1; \frac{1}{8}; \frac{2}{8}; \frac{3}{8}; \frac{4}{8}; \frac{5}{8}; \frac{6}{8}; \frac{7}{8}; 2 \)
3. (a) \( \frac{1}{5}; \frac{2}{5}; \frac{3}{5}; \frac{4}{5}; 1; \frac{1}{5}; \frac{2}{5}; \frac{3}{5}; \frac{4}{5}; 2; \frac{2}{5}; \frac{2}{5}; \frac{2}{5}; \frac{2}{5}; \frac{2}{5}; 3 \)
   (b) \( \frac{1}{8}; \frac{2}{8}; \frac{3}{8}; \frac{4}{8}; \frac{5}{8}; \frac{6}{8}; \frac{7}{8}; 1; \frac{1}{8}; \frac{1}{8}; \frac{3}{8}; \frac{3}{8}; \frac{1}{8}; \frac{1}{8}; \frac{7}{8}; 2 \)
4. (a) \( 2; \frac{1}{5}; \frac{3}{5}; \frac{2}{5}; \frac{1}{5}; 0 \)
   (b) \( 3; \frac{2}{8}; \frac{2}{8}; \frac{2}{8}; \frac{2}{8}; \frac{2}{8}; \frac{2}{8}; \frac{2}{8}; \frac{1}{8}; \frac{1}{8}; \frac{1}{8}; \frac{1}{8}; \frac{1}{8}; \frac{1}{8}; \frac{1}{8}; \frac{1}{8} \)
5. (a) \( \frac{1}{6}; \frac{1}{3}; \frac{1}{2}; \frac{2}{6} \)  (b) \( \frac{2}{3}; \frac{4}{3}; \frac{7}{9}; \frac{8}{9}; \frac{10}{11} \)
6. (a) \( \frac{5}{9} \) is bigger than a half  (b) \( \frac{3}{7} \) is smaller than a half
   (c) \( \frac{6}{12} \) is equal to a half  (d) \( \frac{5}{11} \) is smaller than a half
Answers

7. (a) $\frac{2}{3}; 1\frac{1}{4}; 1\frac{2}{6}; 1\frac{3}{5}; 2\frac{1}{3}; 2\frac{2}{4}$

(b) $\frac{3}{5}; \frac{4}{6}; \frac{5}{8}; \frac{1}{2}; \frac{1}{3}; \frac{2}{5}; \frac{2}{5}; \frac{3}{6}; \frac{4}{6}$

(c) $\frac{2}{8}; \frac{3}{8}; \frac{4}{8}; \frac{5}{8}; \frac{6}{8}; \frac{7}{8}; \frac{1}{2}; \frac{1}{3}; \frac{1}{3}; \frac{1}{5}; \frac{2}{5}; \frac{2}{5}; \frac{3}{8}; \frac{4}{8}; \frac{5}{8}$

(d) $\frac{5}{12}; \frac{6}{12}; \frac{7}{12}; \frac{8}{12}; \frac{9}{12}; \frac{10}{12}; \frac{11}{12}; \frac{12}{12}; \frac{13}{12}; \frac{14}{12}; \frac{15}{12}; \frac{16}{12}; \frac{17}{12}; \frac{18}{12}; \frac{19}{12}; \frac{20}{12}$

8. $\frac{1}{4} = \frac{2}{8} = \frac{3}{12}$

$\frac{2}{4} = \frac{3}{6} = \frac{4}{8} = \frac{5}{12}$

$\frac{4}{6} = \frac{1}{2}$

$\frac{3}{8} = \frac{4}{12}$

$\frac{1}{2} = \frac{2}{12}$

$\frac{1}{4} = \frac{2}{8} = \frac{3}{12}$

$\frac{1}{6} = \frac{2}{12}$

$\frac{2}{4} = \frac{1}{2} = \frac{3}{12}$

$\frac{2}{8} = \frac{3}{12}$

$\frac{2}{6} = \frac{3}{12}$

8. Did you notice equivalent fractions as you counted? Make a list of all the equivalent fractions that you see. Compare your list with the lists of your classmates.
1.5 Calculating a fraction of a quantity

Mathematical notes
This work develops the foundation for multiplication with fractions, which learners will engage with in Grade 7. You can ask the class how they got their answers to questions 3, 4 and 5. Correct any mistakes, but simply comment on good methods as “correct”. Do not teach any formulas for solving such problems. Hopefully learners will show how they used the answers to questions 1(a), (b) and (c) to work out answers to questions 3, 4 and 5.

Answers
1. (a) 5; 5\(\frac{1}{2}\); 6; 6\(\frac{1}{2}\); 8; 11; 19
   (b) 10; 11; 12; 13; 16; 22; 38
   (c) 10; 11; 12; 13; 16; 22; 38
2. (a) They produce the same answers.
   (b) They are equivalent fractions.
3. 28 learners
4. 40 learners
5. 30 circles
1.6 Addition and subtraction of fractions

Teaching guidelines
Please see “Mathematical notes” on the next page.

Question 1 is intended to make learners aware of a challenge, and the expectation should not be that they manage to produce an answer now. Some learners may come up with the idea of rewriting $3\frac{1}{11}$ as $2\frac{12}{11}$, but this will not necessarily happen.

Once learners have engaged with the question for about 5 minutes, you may write the following questions on the board. Ask learners to answer the questions individually; then resume their discussions about question 1.

A. How many elevenths are equal to 1 whole?
B. How many elevenths are equal to 2 wholes?
C. How many elevenths are equal to 3 wholes?
D. How many elevenths are equal to $3\frac{1}{11}$ wholes?

Allow learners to engage with question 1 for another 5 to 10 minutes, then ask them to let go of it for now and proceed to question 2. You may tell them that by doing question 2 they may get an idea of how to meet the challenge that question 1 presented them with.

After learners have completed question 2, let them engage with question 1 again, individually this time, for about 5 minutes. Then demonstrate to them that it will help to rewrite $3\frac{1}{11}$ as $2\frac{12}{11}$, or to rewrite both fractions in the following way:

$3\frac{1}{11} = \frac{33}{11} + \frac{1}{11}$ and $1 \frac{5}{11} = \frac{11}{11} + \frac{5}{11} = \frac{16}{11}$

Answers
1. and 2. Yes, first subtract 1 from 3 and then subtract 1 eleventh from 5 elevenths.

3. (a) $\frac{15}{7}$ or $2\frac{1}{7}$ (b) $\frac{35}{8}$ or $4\frac{3}{8}$ (c) $\frac{15}{12}$ or $1\frac{3}{12}$ or $1\frac{1}{4}$ (d) 4
   
   (e) $\frac{9}{7}$ (f) $\frac{5}{6}$ (g) $\frac{9}{9}$ or 1 (h) $\frac{2}{3}$

4. (a) $\frac{20}{12}$ or $1\frac{8}{12}$ or $1\frac{3}{4}$ (b) $\frac{13}{9}$ (c) $\frac{3}{2}$
   
   (d) Let learners share their explanations. You may use some of their explanations to further consolidate subtraction with mixed numbers.
   
   (e) $\frac{5}{5} = 1\frac{3}{5}$

4. Calculate:
   
   (a) $\frac{5}{12} + \frac{5}{12} + \frac{5}{12}$ (b) $2 - \frac{1}{9}$
   
   (c) $\frac{3}{7} + \frac{6}{7} - \frac{4}{7}$
   
   (d) How will you subtract $3\frac{7}{12}$ from $5\frac{1}{12}$?
   
   Lindi does it like this: $\frac{1}{12} - 3 \rightarrow 2 \frac{12}{12} - \frac{7}{12} \rightarrow 1 \frac{13}{12} - \frac{7}{12} = \frac{6}{12}$
   
   (e) Now do this one: $7\frac{2}{5} - 5\frac{4}{5}$.
Mathematical notes

Mixed numbers can be added and subtracted in the two ways described below:

• By subtracting or adding the whole number parts and the fraction parts separately, replacing one fraction with a useful equivalent in the case of subtraction if necessary (similar to what is done in subtraction of whole numbers), for example:
  \[
  5\frac{7}{20} - 2\frac{13}{20} = 4\frac{22}{20} - 2\frac{13}{20} = 2\frac{14}{20}
  \]
• By converting the mixed numbers to improper fractions, for example:
  \[
  5\frac{7}{20} - 2\frac{13}{20} = \frac{107}{20} - \frac{53}{20} = \frac{54}{20} = 2\frac{14}{20}
  \]

Notes on questions

In question 8 some learners may be trapped into thinking the answer is three quarters of 10. It is not.

To help learners who fall into this trap, you can draw a number line that is 10 units long, with each unit subdivided into quarter-units, on the board. Ask learners to count how many sections of three quarters each there are on this line.

You can also suggest that they count up in three quarters:

\[
\frac{3}{4}, \frac{1}{2}, \frac{2}{4}, 3, \frac{3}{4}, \frac{4}{2}, \frac{5}{4}, 6, \frac{6}{4}, 7\frac{1}{2}, 8\frac{1}{4}, 9, \frac{9}{4}
\]

and there is one quarter metre material left over.

Answers

5. (a) Blue: \(\frac{2}{11}\) or \(\frac{4}{22}\) Red: \(\frac{3}{11}\) or \(\frac{6}{22}\) White: \(\frac{6}{11}\) or \(\frac{12}{22}\)

(b) Blue: \(\frac{4}{12}\) or \(\frac{1}{3}\) Red: \(\frac{4}{12}\) or \(\frac{1}{3}\) White: \(\frac{4}{12}\) or \(\frac{1}{3}\); or perhaps even \(\frac{8}{24}\)

(c) Blue: \(\frac{5}{10}\) or \(\frac{6}{20}\) Red: \(\frac{5}{10}\) or \(\frac{1}{2}\) White: \(\frac{2}{10}\) or \(\frac{1}{5}\)

6. (a) \(\frac{11}{11} = 1\) (b) \(\frac{8}{11}\)

7. (a) \(\frac{1}{7}\) (b) \(\frac{7}{7}\) (c) \(\frac{5}{7}\) (d) \(\frac{7}{7} = 1\)

(e) \(\frac{8}{7} = 1\frac{1}{7}\) (f) \(\frac{9}{7} = 1\frac{2}{7}\) (g) \(1\frac{5}{7}\) (h) \(2\frac{5}{7}\)

8. He can make 13 flags. (\(\frac{1}{4}\) m of material will be left over.)

9. She will have \(\frac{2}{8} = \frac{1}{4}\) m of material will be left over.

5. Look at the strips below. What fraction of each strip is blue, what fraction is red and what fraction is white?

Name each of the fractions in more than one way.

(a) (b) (c)

6. Calculate the following:

(a) \(\frac{2}{11} + \frac{6}{11} + \frac{3}{11}\) (b) \(1 - \frac{3}{11}\)

7. What number is missing in each of these number sentences?

(a) \(\ldots + \frac{2}{7} = \frac{3}{7}\) (b) \(\frac{2}{7} + \frac{2}{7} = \ldots\)

(c) \(\frac{3}{7} + \frac{2}{7} = \ldots\) (d) \(\frac{5}{7} + \frac{2}{7} = \ldots\)

(e) \(\frac{5}{7} + \frac{2}{7} = \ldots\) (f) \(1 + \frac{2}{7} = \ldots\)

(g) \(\ldots + \frac{2}{7} = 2\frac{1}{7}\) (h) \(\ldots + \frac{2}{7} = 3\)

8. Leon uses 3 quarters of a metre of material to make one flag. How many flags can he make if he has 10 m of material available?

9. Mary has \(2\frac{3}{4}\) m of lace. Her friend, Sethu needs \(\frac{5}{8}\) m of that lace. How many metres will Mary have left if she agrees to give \(\frac{5}{8}\) m to Sethu?
Mathematical background

Length, mass, area, capacity and volume are different properties of objects. Length, area, capacity and volume are called *spatial measures*. We can often see how much space something takes up, how much area it covers, or what length something is.

Mass is not a spatial measure. It is called a *physical measure*. The mass of an object is the property that we feel in our hands – we say the object feels heavy, or not very heavy. From experience, we can remember how heavy a bucket of water is, but we cannot always guess how heavy an object is by looking at its size. Young learners often assume that the bigger something is, the heavier it must be. A small piece of iron may, however, be much heavier than a large piece of plastic foam; this tells us that the density of iron is greater than the density of plastic foam.

The heaviness of an object is really the force of gravity with which the object and the Earth pull on each other. We can measure the heaviness of an object on an instrument such as a bathroom scale. The scale is marked in grams and/or kilograms and so we can report the *mass* of the object: we can report that a brick has a mass of 1 kg or that Andile has a mass of 60 kg. A number (1 kg) for the mass of a brick is useful, for example if we need to calculate how many bricks we can safely load onto a 1-ton bakkie.

As explained in Term 2 Unit 4: *Length*, learners go through four stages when learning to measure: (1) identifying and understanding the property they are measuring; (2) comparing and ordering examples of a particular measure; (3) using informal or non-standard units to measure; (4) using formal or standard units to measure.

In Grade 5 learners work with standard units (grams and kilograms) when measuring mass. They need time to practise reading the scales of the measuring instruments (see Section 2.4).

**Resources**

We suggest that you read through the entire unit before you start teaching it and draw up a checklist of the resources that you will need for each lesson.
2.1 Models of kilograms and grams

Mathematical notes
Learners should develop a good sense of how much 1 kg is and how much 1 g is. This will help them to make sensible estimates of the mass of objects before measuring. Working with a balance scale can help to develop learners’ sense of how heavy 1 kg and 1 g are.

The mass of a cube of water, 1 cm × 1 cm × 1 cm (i.e. 1 cm³) is 1 g. (Scientists defined the gram very strictly: the water must be pure, and at a temperature of 4 °C. Why 4 °C? It is because water becomes less dense at 3 °C, 2 °C, and so on, and at 0 °C it is ice and it floats on the rest of the water because ice is less dense than water.)

Empty plastic bags also have mass, so the small bag of water will have a mass of a little more than 1 g and the large bag of water will have a mass of a little more than 1 kg. Although all measurements are approximate, they are close enough for learners to get a sense of how heavy 1 g is and how heavy 1 kg is. Because the units that learners will make are not exactly 1 kg, nor exactly 1 g, it is important to always say about 1 kg or about 1 g.

Resources and teaching guidelines
Organise the following for each learner before you teach this section:

- Clear ziplock bags that hold 1 ℓ. If you cannot get ziplock bags, you can use 1 ℓ plastic bottles. These will also have a mass of a bit more than 1 kg when they are filled with water, but they will still give learners a sense of how heavy 1 kg is.
- Very small bags that can hold 1 ml (20 drops of water). You could also use the small bags that banks use to hold coins. Alternatively, use bottle tops from cooldrink bottles or beer bottles. Their mass is between 2 g and 3 g. Adjust the activities accordingly.

You can use the photograph and the tinted text on page 212 of the Learner Book as a guide to demonstrate to learners how to make a simple balance scale. (Hint: Tape down the learners’ pencils on their desks with masking tape, or use clay or sticky putty.)

Let learners use any light objects that are available. They can substitute nails, clothes pegs, etc. for the objects mentioned in the Learner Book.

Notes on questions
The aim of questions 2 and 3 is for learners to get a sense of the mass of 1 g, how heavy or how light it is. They can then use this to estimate the mass of other objects. A gram is very light and it is therefore very difficult to develop a sense of its mass. Learners can use other everyday objects such as a clothes peg or a pen or a box of matches to get a sense of the mass of objects in grams.
Answers
Learners’ answers may differ from those given below because different paper clips, pens, erasers and bottle tops have different masses. Also, the balance scale will not be very accurate.

3. (a) About 2 paper clips (b) $\frac{1}{2}$ g
   (c) About 6 g to 12 g (d) Less than 10 g to over 30 g
   (e) Tops of 1 ℓ and 2 ℓ plastic bottles are usually about 3 g. Metal bottle tops (from glass cooldrink and beer bottles) and the plastic tops of 500 ml or smaller plastic bottles usually have a mass of about 2 g.
   (f) Learners’ answers will differ. Some objects with a mass of 1 g are a 10c coin, a dried butter bean, and a large button.
   (g) Learners’ answers will differ. Approximate masses of other light objects: empty matchbox, about 3 g; full box of matches, about 10 g; wooden clothes peg, about 5 g to 8 g; ballpoint pen, about 5 g to 12 g; key, about 10 g to 12 g.

2.2 Estimating and measuring mass

Mathematical notes
Learners can use their 1 kg models to estimate masses in kilograms. They can use their 1 g and 1 kg models to choose appropriate units of mass and linked to this, appropriate scales.

The word “scale” in English has two meanings: we talk of the scale marked on a ruler – the millimetre and centimetre markings; and we talk of a bathroom scale – an instrument that people stand on to weigh themselves.

Resources and teaching guidelines
It is important that these activities are done practically. Make a checklist of all the apparatus required in Section 2.2. Arrange to bring all the necessary items to class.

Notes on questions
When learners do question 4(b) on page 213 of the Learner Book, check that they know that they must stand directly in front of the dial. If they stand too far to the right or left of the dial, they will get a wrong reading.

In question 4(c) on page 213 of the Learner Book you might need to help learners decide on an appropriate scale for their graphs, and to think through what to do about masses that are less than 1 kg.
In question 5 learners could compare a cup or half a cup of these substances using a mass meter or a balance scale. Learners could also experiment with pouring some liquid soap into water and seeing whether it rises to the surface of the water or sinks to the bottom. They could test oil and liquid soap in the same way.

**Answers**

1. (a) kilograms  (b) grams  (c) grams  (d) grams
2. (a) Kitchen scale  (b) Kitchen scale  (c) Bathroom scale
3. See the answers to question 3 in Section 2.1.
4. (a) Learners’ estimates will differ because there are different stacks of books, schoolbags, pairs of shoes, bricks (often 2 kg to 4 kg) and potted plants.
   (b) Learners’ estimates will differ.
   (c) Learners will probably make a bar graph. The bar graphs will differ from class to class. Learners should give the graph a heading and label the axes.

**Mass of objects**

<table>
<thead>
<tr>
<th>Mass in kg</th>
</tr>
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<tbody>
<tr>
<td>10</td>
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<td>9</td>
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</tr>
</tbody>
</table>

**Objects**

5. You want learners to realise that they can only compare masses if they take equal quantities of each substance!
   (a) It depends how much sugar and how much rice we are comparing. If we fill tins of the same size with sugar and rice, their masses will be similar.
   (b) A tin of sand is heavier than a same-sized tin of sugar.
   (c) Yes, for same amounts
   (d) Yes, for same amounts
   (e) Yes, for same amounts
**Answers**

6. (a) Learners’ estimates will differ.
   (b) and (c) Water: about 250 g or $\frac{1}{4} \text{ kg}$
   Liquid soap: about 500 g or $\frac{1}{2} \text{ kg}$
   Clay or play dough: about 375 g or $\frac{375}{1000} \text{ kg}$

    Sand: about 375 g or $\frac{375}{1000} \text{ kg}$
    Flour: about 130 g or $\frac{130}{1000} \text{ kg}$

7. Learners’ answers will differ. There are many possible answers.

**2.3 The relationship between grams and kilograms**

**Mathematical notes**

In the Intermediate Phase learners only work with grams and kilograms.

Learners can learn the conversion factors off by heart. However, they may sometimes forget them and use an incorrect conversion factor. It may be better for learners to understand how the relationship between metric units works in general.

In our base-ten place value system, each unit of a higher power is ten times the value of an adjacent unit of a lower power. 10 units (ones) make 1 ten; 10 tens make 1 hundred; 10 hundreds make 1 thousand, etc. The metric system also works with groupings or powers of tens. This is why, since the 1790s, it is called the decimal metric system. Page 143 of the Learner Book shows a table of the standard metric units for measuring length. Such units (kilo-, hecto-, deca-, deci-, etc.) also exist for measuring mass and capacity/volume.

**Teaching guidelines**

<table>
<thead>
<tr>
<th>kilogram (kg)</th>
<th>hectogram</th>
<th>decagram</th>
<th>gram (g)</th>
<th>decigram</th>
<th>centigram</th>
<th>milligram (mg)</th>
</tr>
</thead>
</table>

Learners can use a table like the one above to do conversions. They simply work as follows:

- They write the number in the correct column.
- They mark the unit they are converting to.
- If converting from a unit of a higher power to a unit of a lower power, they multiply by 10 each time they move to the next unit of a lower power, for example 25 kg = (25 × 10 × 10 × 10) g = 25 000 g.
- If converting from a unit of a lower power to a unit of a higher power, they divide by 10 each time they move to the next unit of a higher power, for example 4 000 g = (4 000 ÷ 10 ÷ 10 ÷ 10) kg = 4 kg, and 500 g = (500 ÷ 10 ÷ 10 ÷ 10) kg = $\frac{5}{10} \text{ kg} = \frac{1}{2} \text{ kg}$. 
If you want learners to be able to work with all the metric units for mass between milli- and kilo-, then it is useful to teach them a mnemonic to help remember the units (names, sequences and numerical relationships between them). You can make any sentence you like with words that start with the letters: k, h, d, g, d, c, m. Refer to page 416 in the Addendum for an example suggested by the Department of Basic Education.

**Answers**

1. | **Mass** | **Groceries** |
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Less than $\frac{1}{4}$ kg</td>
<td>100 g box of tea</td>
</tr>
<tr>
<td>$\frac{1}{4}$ kg</td>
<td>250 g packet of sugar</td>
</tr>
<tr>
<td>Between $\frac{1}{2}$ kg and $\frac{1}{2}$ kg</td>
<td>410 g tin of beans; 400 g box of cornflakes</td>
</tr>
<tr>
<td>$\frac{1}{2}$ kg</td>
<td>500 g packet of flour</td>
</tr>
<tr>
<td>Between $\frac{1}{2}$ kg and 1 kg</td>
<td>750 g tin of coffee</td>
</tr>
<tr>
<td>1 kg</td>
<td>1 kg cylinder of salt</td>
</tr>
<tr>
<td>Between 1 kg and 2 kg</td>
<td>None of the items</td>
</tr>
<tr>
<td>More than 2 kg</td>
<td>2.5 kg packet of sugar</td>
</tr>
</tbody>
</table>

2. (a) 3 000 g  
(b) 7 000 g  
(c) 10 000 g  
(d) 500 g  
(e) 250 g  
(f) 100 g  
(g) 2 500 g  
(h) 3 750 g  
(i) 300 g

3. (a) 2 kg  
(b) $\frac{1}{2}$ kg  
(c) $\frac{1}{4}$ kg  
(d) $1\frac{1}{2}$ kg  
(e) $2\frac{1}{2}$ kg  
(f) $\frac{1}{10}$ kg

4. (a) 2 kg and 650 g  
(b) 3 kg and 840 g  
(c) 7 kg and 25 g

**2.4 Counting in grams and kilograms, and reading scales**

**Answers**

1. (a) 3 kg and 500 g + 250 g → 3 kg and 750 g + 250 g →  
4 kg and 0 g + 250 g → 4 kg and 250 g + 250 g →  
4 kg and 500 g + 250 g → 4 kg and 750 g  
(b) 1 kg and 800 g + 200 g → 2 kg and 0 g + 200 g →  
2 kg and 200 g + 200 g → 2 kg and 400 g + 200 g →  
2 kg and 600 g + 200 g → 2 kg and 800 g
Teaching guidelines

Learners often assume that there are 10 unnumbered intervals between numbered intervals on all scales. However, some kitchen scales have five unnumbered intervals between each numbered interval (see question 3(f)). Other kitchen scales have four unnumbered intervals between each numbered interval (see question 3(g)).

Learners can use the following steps to find out the mass at the dial/needle/pointer.

- Find the value of the interval between numbered lines.
  Subtract the number just before the pointer from the number just after the pointer.
  In question 3(g) it is $3 - 2 = 1$, so the value between numbered intervals is 1 kg.

- To find the value of the unnumbered intervals, count the number of unnumbered intervals (the spaces, not the lines) between numbered intervals.
  In question 3(g) it is 4.
  Divide this number into the value of the numbered intervals.
  In question 3(g) it is $1000 \text{ g} ÷ 4 = 250 \text{ g}$.

- Count on from the numbered interval before the pointer (e.g. in question 3(g) you will count: 2 kg and 250 g, 2 kg and 500 g, 2 kg and 750 g) or count back from the numbered interval after the pointer (e.g. in question 3(f) you will count: 3 kg, 2 kg and 800 g, 2 kg and 600 g).

Answers

2.

2. Copy the number lines below. Count the number of spaces between each kilogram. Calculate the value of each space in grams. Fill in the kilograms and grams at each mark on your number lines.

3. Write the mass on each scale in kilograms and grams.

   (a) 24 kg and 500 g  
   (b) 64 kg and 500 g  
   (c) 119 kg and 500 g  
   (d) 100 g  
   (e) 120 g  
   (f) 3 kg and 400 g  
   (g) 2 kg and 750 g
2.5 Solving problems about mass and quantity

Teaching guidelines
Suggest to learners that they quickly make a rough sketch of the situation described in question 1. They should not spend more than 5 minutes on making the sketch, since the purpose is only to help them understand the situation, not to produce a work of art!

Answers
1. (a) $200 \times 80 = 16\,000 = 16\,kg$ This is the mass of the oranges in one box.
   (b) $16\,kg \times 60 = 960\,kg$ This is the mass of 60 boxes of oranges.
   (c) $960\,kg \times 12 = 11\,520\,kg$ This is the mass of 12 crates with 60 boxes of oranges in each crate.
   (d) $11\,520\,kg \times 30 = 345\,600\,kg$ This is the mass of oranges in 30 containers.

2. (a) $50\,g$ (mass of half of 60 nails)
(b) $25\,g$ (mass of half of 30 nails)
(c) $5\,g$ (mass of $\frac{1}{10}$ of 30 nails)
(d) $500\,g$ (mass of 5 × 60 nails)
(e) 300 nails
(f) 1200 nails (1 kg has 600 nails, so 2 × 1 kg = 1200 nails)
(g) Examples:
   $3 \times 500\,g$ bag (900 nails) + $2 \times 100\,g$ bag (120 nails) = 1020 nails
   $1 \times 1\,kg$ bag (600 nails) + $1 \times 500\,g$ bag (300 nails) + $2 \times 100\,g$ bag (120 nails) = 1020 nails
   $9 \times 100\,g$ bags (120 nails) = 1080 nails

3. (a) $1\frac{1}{2}\,kg = 1\,500\,g$ 
   $1\,500\,g + 200\,g = 7\frac{1}{2}$ cups of sugar
(b) $3\,kg = 3\,000\,g$ 
   $3\,000\,g + 125\,g = 24$ cups of flour
(c) $1\,kg = 1\,000\,g$ 
   $1\,000\,g + 225\,g = 4\frac{1}{2}$ cups of butter
(d) $60\,g + 300 = \frac{1}{3}$ cup salt

4. (a) $5\,000\,g + 20 = 250\,g$
(b) $250\,g \times 12 = 3\,000\,g$ or 3 kg
Grade 5 Term 3 Unit 3  Whole numbers

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.1 Compare and order numbers</td>
<td>Thinking of large numbers</td>
<td>218 to 220</td>
</tr>
<tr>
<td>3.2 Represent and compare numbers</td>
<td>Representing numbers with number names and place value expansions</td>
<td>221 to 222</td>
</tr>
<tr>
<td>3.3 An investigation</td>
<td>Large numbers in a practical context</td>
<td>222</td>
</tr>
</tbody>
</table>

**CAPS time allocation**
1 hour

**CAPS page references**
13 to 15 and 181

**Mathematical background**
The following critical aspects of number concept for whole numbers up to one million are addressed in this short unit:
- developing a sense of large quantities, specifically of large collections of objects
- arranging numbers in ascending and descending order
- the composition of numbers with place value parts.
3.1 Compare and order numbers

**Teaching guidelines**

Questions 2 and 3 were designed to help learners to engage with large quantities in their minds, with a view to empower them to make sense of larger numbers. Doing questions 2 and 3 purely by making rough guesses will already serve the purpose of making learners think of large quantities of objects.

When learners engage with question 2(b) you may suggest to them that they first estimate how many red squares are about equal to a yellow square (ten), and then use their estimate for the number of yellow squares to form an estimate for the number of red squares that will cover the back of the book.

(If time is available now, or when you revisit these questions in another period when time is available, it can be valuable to challenge learners to make good estimates of the answers to questions 2 and 3 by taking rough measurements and doing some calculations.)

Once learners have produced their answer for question 3, you may ask them to estimate how many yellow stickers and how many red stickers will be needed to cover your classroom floor. When reflecting on this sensibly, learners may imagine numbers of the order of half a million and several millions.

**Answers**

1. (a) 309 778
   (b) 209 778 278 545 288 103 309 778 312 215

2. (a) 500
   (b) 5 000

3. The number of tiles could be between 1 000 and 100 000.
   (The grey square is 5 cm by 5 cm in the Learner Book; hence 400 grey squares cover 1 square metre. A typical classroom is about 10 m by 10 m.)
Answers

4. 120 000  126 000  132 000  138 000  
   144 000  150 000  156 000  162 000  
   168 000  174 000  180 000  

5. 321 965  339 365  347 677  366 152  
   395 923  398 899  398 987  

6. 493 586  465 153  431 999  431 001  
   427 180  420 122  420 121  

7. Numbers | Rounded off to the nearest: 
            | (a)      | (b)      | (c)      | (d)      |
            | five     | ten      | hundred  | thousand |
427 180    | 427 180  | 427 180  | 427 200  | 427 000  |
493 586    | 493 585  | 493 590  | 493 600  | 494 000  |
465 153    | 465 155  | 465 150  | 465 200  | 465 000  |
420 122    | 420 120  | 420 120  | 420 100  | 420 000  |
420 121    | 420 120  | 420 120  | 420 100  | 420 000  |
431 999    | 432 000  | 432 000  | 432 000  | 432 000  |
431 001    | 431 000  | 431 000  | 431 000  | 431 000  |

8. (a) one hundred; 100  
    (b) one million; 1 000 000  
    (c) ten thousand; 10 000  
    (d) one hundred thousand; 100 000  
    (e) one thousand; 1 000
Answers

9. (a) 90 000; 100 000; 110 000; 120 000; 130 000; 140 000; 150 000; 160 000; 170 000
   (b) 440 000; 450 000; 460 000; 470 000; 480 000; 490 000; 500 000; 510 000; 520 000
   (c) 430 000; 480 000; 530 000; 580 000; 630 000; 680 000; 730 000; 780 000; 830 000; 880 000
10. 120 000; 121 500; 123 000; 124 500; 126 000; 127 500; 129 000; 130 500; 132 000
11. (a) 4 000  (b) 7 000  (c) 10 000  (d) 13 000  (e) 16 000  (f) 19 000  (g) 22 000
12. (a) 160 054 > 123 654  123 654 < 160 054
   (b) 987 121 > 789 121  789 121 < 987 121
   (c) 404 872 < 440 782  440 782 > 404 872
   (d) 144 544 < 414 454  414 454 > 144 544
### 3.2 Represent and compare numbers

**Answers**

<table>
<thead>
<tr>
<th>Number symbol</th>
<th>Number name</th>
<th>Expanded notation</th>
</tr>
</thead>
<tbody>
<tr>
<td>423 772</td>
<td>four hundred and twenty-three thousand</td>
<td>400 000 + 20 000 + 3 000 +</td>
</tr>
<tr>
<td></td>
<td>seven hundred and seventy-two</td>
<td>700 + 70 + 2</td>
</tr>
<tr>
<td>611 954</td>
<td>six hundred and eleven thousand nine</td>
<td>600 000 + 10 000 + 1 000 +</td>
</tr>
<tr>
<td></td>
<td>hundred and fifty-four</td>
<td>900 + 50 + 4</td>
</tr>
<tr>
<td>545 756</td>
<td>five hundred and forty-five thousand seven</td>
<td>500 000 + 40 000 + 5 000 +</td>
</tr>
<tr>
<td></td>
<td>hundred and fifty-six</td>
<td>700 + 50 + 6</td>
</tr>
<tr>
<td>701 205</td>
<td>seven hundred and one thousand two</td>
<td>700 000 + 1 000 + 200 + 5</td>
</tr>
<tr>
<td>801 630</td>
<td>eight hundred and one thousand six</td>
<td>800 000 + 1 000 + 600 + 30</td>
</tr>
<tr>
<td></td>
<td>hundred and thirty</td>
<td></td>
</tr>
<tr>
<td>306 301</td>
<td>three hundred and six thousand three</td>
<td>300 000 + 6 000 + 300 + 1</td>
</tr>
<tr>
<td></td>
<td>hundred and one</td>
<td></td>
</tr>
<tr>
<td>200 036</td>
<td>two hundred thousand and thirty-six</td>
<td>200 000 + 30 + 6</td>
</tr>
<tr>
<td>870 102</td>
<td>eight hundred and seventy thousand one</td>
<td>800 000 + 70 000 + 100 + 2</td>
</tr>
<tr>
<td></td>
<td>hundred and two</td>
<td></td>
</tr>
<tr>
<td>909 009</td>
<td>nine hundred and nine thousand and nine</td>
<td>900 000 + 9 000 + 9</td>
</tr>
<tr>
<td>859 560</td>
<td>eight hundred and fifty-nine thousand five</td>
<td>800 000 + 50 000 + 9 000 +</td>
</tr>
<tr>
<td></td>
<td>hundred and sixty</td>
<td>500 + 60</td>
</tr>
<tr>
<td>102 040</td>
<td>one hundred and two thousand and forty</td>
<td>100 000 + 2 000 + 40</td>
</tr>
<tr>
<td>110 300</td>
<td>one hundred and ten thousand three</td>
<td>100 000 + 10 000 + 300</td>
</tr>
<tr>
<td></td>
<td>hundred</td>
<td></td>
</tr>
<tr>
<td>606 109</td>
<td>six hundred and six thousand one hundred</td>
<td>600 000 + 6 000 + 100 + 9</td>
</tr>
<tr>
<td></td>
<td>and nine</td>
<td></td>
</tr>
<tr>
<td>800 001</td>
<td>eight hundred thousand and one</td>
<td>800 000 + 1</td>
</tr>
<tr>
<td>200 909</td>
<td>two hundred thousand nine hundred and nine</td>
<td>200 000 + 900 + 9</td>
</tr>
</tbody>
</table>

---

3.2 Represent and compare numbers

1. Copy the table and complete it.

<table>
<thead>
<tr>
<th>Number symbol</th>
<th>Number name</th>
<th>Expanded notation</th>
</tr>
</thead>
<tbody>
<tr>
<td>423 772</td>
<td>four hundred and twenty-three thousand</td>
<td>400 000 + 20 000 + 3 000 +</td>
</tr>
<tr>
<td></td>
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<td>700 + 70 + 2</td>
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<tr>
<td>611 954</td>
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<td>545 756</td>
<td>five hundred and forty-five thousand seven</td>
<td>500 000 + 40 000 + 5 000 +</td>
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<td></td>
<td>hundred and fifty-six</td>
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<tr>
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</tr>
<tr>
<td>801 630</td>
<td>eight hundred and one thousand six</td>
<td>800 000 + 1 000 + 600 + 30</td>
</tr>
<tr>
<td></td>
<td>hundred and thirty</td>
<td></td>
</tr>
<tr>
<td>306 301</td>
<td>three hundred and six thousand three</td>
<td>300 000 + 6 000 + 300 + 1</td>
</tr>
<tr>
<td></td>
<td>hundred and one</td>
<td></td>
</tr>
<tr>
<td>200 036</td>
<td>two hundred thousand and thirty-six</td>
<td>200 000 + 30 + 6</td>
</tr>
<tr>
<td>870 102</td>
<td>eight hundred and seventy thousand one</td>
<td>800 000 + 70 000 + 100 + 2</td>
</tr>
<tr>
<td></td>
<td>hundred and two</td>
<td></td>
</tr>
<tr>
<td>909 009</td>
<td>nine hundred and nine thousand and nine</td>
<td>900 000 + 9 000 + 9</td>
</tr>
<tr>
<td>859 560</td>
<td>eight hundred and fifty-nine thousand five</td>
<td>800 000 + 50 000 + 9 000 +</td>
</tr>
<tr>
<td></td>
<td>hundred and sixty</td>
<td>500 + 60</td>
</tr>
<tr>
<td>102 040</td>
<td>one hundred and two thousand and forty</td>
<td>100 000 + 2 000 + 40</td>
</tr>
<tr>
<td>110 300</td>
<td>one hundred and ten thousand three</td>
<td>100 000 + 10 000 + 300</td>
</tr>
<tr>
<td></td>
<td>hundred</td>
<td></td>
</tr>
<tr>
<td>606 109</td>
<td>six hundred and six thousand one hundred</td>
<td>600 000 + 6 000 + 100 + 9</td>
</tr>
<tr>
<td></td>
<td>and nine</td>
<td></td>
</tr>
<tr>
<td>800 001</td>
<td>eight hundred thousand and one</td>
<td>800 000 + 1</td>
</tr>
<tr>
<td>200 909</td>
<td>two hundred thousand nine hundred and nine</td>
<td>200 000 + 900 + 9</td>
</tr>
</tbody>
</table>

---

**GRADE 5: MATHEMATICS [TERM 3]**
Answers

2. (a) 909 009
   (b) 102 040

3. 120 000; 160 000; 200 000; 240 000; 280 000; 320 000; 360 000; 400 000;
   440 000; 480 000; 520 000

4. (a) 99 000
   (b) 108 000
   (c) 117 000
   (d) 126 000
   (e) 135 000
   (f) 144 000
   (g) 153 000
   (h) 162 000
   (i) 171 000
   (j) 180 000
   (k) 189 000

5. (a) 16 154 < 16 654
   (b) 16 654 > 16 154
   (b) 23 121 < 23 322
   (c) 23 322 > 23 121
   (c) 44 872 > 44 782
   (d) 44 782 < 44 872
   (d) 14 544 < 41 454
   (e) 41 454 > 14 544

3.3 An investigation

Teaching guidelines
Learners will have to do this project over a number of days in their own time. Ask them
for brief feedback about their progress from time to time.

Answer
Learners’ approximations will differ; they need to show how they reasoned and show how
they got to the number. An estimate between 6 000 and 14 000 bricks will be reasonable.
Grade 5 Term 3 Unit 4 Whole numbers: Addition and subtraction

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.1 Revision, and adding in columns</td>
<td>Introduction of the column format for recording addition</td>
<td>223 to 225</td>
</tr>
<tr>
<td>4.2 Subtracting in columns</td>
<td>Introduction of the column format for recording subtraction</td>
<td>226 to 227</td>
</tr>
<tr>
<td>4.3 Less writing when adding in columns</td>
<td>Refinement of the column format for recording addition</td>
<td>228 to 230</td>
</tr>
<tr>
<td>4.4 Another way of subtracting in columns</td>
<td>Subtraction in columns with transfer between place value positions</td>
<td>231 to 232</td>
</tr>
<tr>
<td>4.5 Solve problems</td>
<td>Word problems involving addition and subtraction</td>
<td>232</td>
</tr>
</tbody>
</table>

**CAPS time allocation**

5 hours

**CAPS page references**

13 to 15 and 182 to 183

**Mathematical background**

Doing addition in columns and doing subtraction in columns are not new methods or methods different to the breaking down and building up methods that learners have used previously. Working in columns is simply an *alternative format* for setting out the work, and it has the advantage that it can be abbreviated by not recording all the thinking steps.

The transition from addition and subtraction by breaking down and building up, as learners have done it up to now, to the so-called “column methods” is not a change of method; it is a change of formatting style and a reduction in the extent to which the actual mathematical steps or thinking is recorded in writing.

The activities in this unit provide learners with opportunities to make a gradual transition from the detailed documentation of thinking steps that they did in Terms 1 and 2, to the more economical column format of setting out addition and subtraction.
4.1 Revision, and adding in columns

Teaching guidelines
Inform learners that they will learn a different way of setting out their thinking for addition and subtraction.

Possible misconceptions
The misconception that working in columns is a different method to breaking down the numbers into place value parts, and rearranging and calculating the parts separately before adding the answers up, should be resisted. Working in columns is just one of the various ways in which the method can be set out in writing. Several important thinking steps, such as breaking the numbers down into place value parts, are not written down in the traditional column format.

Answers
1. (a) \[8 000 + 200 + 50 + 4 + 3 000 + 400 + 30 + 2 = 11 686\]
   (b) \[5 000 + 600 + 80 + 7 + 2 000 + 700 + 30 + 6 = 8 423\]
2. The mistakes in Steve’s work are highlighted in red:
   \[5 687 = 5 000 + 400 + 80 + 7\]
   \[2 736 = 2 000 + 700 + 30 + 6\]
   \[5 687 + 2 736 = 8 000 + 110 + 110 + 13\]
   \[= 9 000 + 200 + 3\]
   \[= 9 213\]
   The following example of a note explains what Steve did wrong. These mistakes should be mentioned in learners’ notes. Learners’ wording may of course differ.
   Steve, you broke down the 5 687 incorrectly: the 400 should be 600.
   You added the thousands incorrectly: 5 000 + 2 000 = 7 000 and not 8 000. You also forgot to add one ten, probably the ten in 110.
   The correct answer is 8 423 (as in question 1(b)).
3. Learners use the method shown in the tinted passage.
   (a) 1 337  (b) 1 301  (c) 12 394  (d) 82 621
Possible misconceptions
Care must be taken to prevent learners from forming the misconception that “adding in columns” as demonstrated in the second tinted passage is a different method of addition to the method demonstrated in the tinted passage at the top of the page. Both passages show addition by breaking down into place value parts and building up the answers. There is no mathematical difference, no difference in the way of thinking between the two passages.

Teaching guidelines
At this stage learners are used to documenting addition as shown in the tinted passage at the top of the page. Tell them that they will now learn a shorter way to set out the work. In the shorter way, some of the things that happen in your mind when you do addition are not written down. This can be shown clearly by writing the work in the tinted passage (or similar work with different numbers) on the board, and then deleting the parts that are not written down in column notation.

\[
\begin{align*}
6524 &= 6000 + 500 + 20 + 4 \\
3245 &= 3000 + 200 + 40 + 5 \\
6524 + 3245 &= 9000 + 700 + 60 + 9 \\
&= 9769
\end{align*}
\]

(You may write the parts that will be deleted with a different coloured chalk.)

Now delete the grey parts:

\[
\begin{align*}
6524 &= 6000 + 500 + 20 + 4 \\
3245 &= 3000 + 200 + 40 + 5 \\
6524 + 3245 &= 9000 + 700 + 60 + 9 \\
&= 9769
\end{align*}
\]

Then do another addition on the board, for example with the numbers in the second tinted passage, without writing the expansions and the reasons for the part answers. However, state the expansions and reasons for the part answers verbally.

Answers

4. Learners should set out their work as shown in the first tinted passage.
   (a) 10 967  (b) 77 887

5. (a) 5 436  
    (b) 23 572  
    (c) 35 254  
    (d) 23 234  
   + 3 352  
   + 53 215  
   + 42 623  
   + 32 123  
   8 788  
   76 787  
   77 877  
   + 11 442  
   66 799

In a case such as 6 524 + 3 245 you do not need to make any transfers, so you need only three steps.

\[
\begin{align*}
6524 &= 6000 + 500 + 20 + 4 \\
3245 &= 3000 + 200 + 40 + 5 \\
6524 + 3245 &= 9000 + 700 + 60 + 9 \\
&= 9769
\end{align*}
\]

Step 1: Break down.  
Step 2: Add the parts.  
Step 3: Build up.

When you want to explain to someone else how you thought, it is good to write down the separate place value parts in Step 2. But if you are just interested in getting to the answer, you can combine the place value parts in your mind and write the answer directly as shown below.

\[
\begin{align*}
6524 &= 6000 + 500 + 20 + 4 \\
3245 &= 3000 + 200 + 40 + 5 \\
6524 + 3245 &= 9000 + 700 + 60 + 9 \\
&= 9769
\end{align*}
\]

4. Do these calculations by writing as in the example printed in colour above:
   (a) 7 435 + 3 532  
   (b) 43 364 + 34 523

When you are not explaining but just trying to find the answer, you can write even less if no transfers are needed.

Look at this example for the calculation of 4 345 + 3 253:

\[
\begin{align*}
4345 + 3253 \\
7598
\end{align*}
\]

Think of 4 345 as 4 000 + 300 + 40 + 5 but do not write it.  
Think of 3 253 as 3 000 + 200 + 50 + 3 but do not write it.  
Think of 5 + 3 = 8, 40 + 50 = 90, 300 + 200 = 500 and 4 000 + 3 000 = 7 000 and 7 000 + 500 + 90 + 8, but only write 7 598.

When you write like this to do addition, we say you **add in columns**.
**Possible misconceptions**
The introduction of column addition is done gradually in order to protect learners against losing sight of place value when adding in columns, for example acting on the misconception that single-digit numbers are added in each column. Also see “Possible misconceptions” on page 132 of this Teacher Guide.

**Teaching guidelines**
For cases that require transfers between columns to produce the final answer, an extended form of adding in columns is introduced in the tinted passage. (The traditional condensed form of column exposition, in which the answer is produced in one line, is only introduced at the end of Section 4.3, i.e. on page 230 of the Learner Book.)

The tinted passage can be used as the basis for a lesson and demonstration.

**Answers**
6. Learners add in columns to get to the answer 1 337.

7. (a) 26 987
   + 54 654
   81 641
(b) 44 887
   + 47 596
   92 483

   7. (a) 26 987
   + 54 654
   81 641
(b) 44 887
   + 47 596
   92 483

8. Below is an example of a note. Learners explain in their own words.

   *Thuli, you did not write the ten and hundred parts correctly. You should have written 70 + 90 = 160 and 600 + 800 = 1 400.
   When you added up, you did not keep the place values in mind correctly.
The correct answer is 1 400 + 160 + 11 = 1 571.*

9. Learners add in columns.
   (a) 82 534  (b) 60 123  (c) 64 644
   (d) 98 887  (e) 6 608  (f) 39 066
4.2 Subtracting in columns

**Teaching guidelines**

You can develop the two representations of calculating $876 - 254$ simultaneously side by side on the board, writing the descriptions of the various steps in the middle. The format that learners used previously (in Term 2) is on the left. The first two lines are exactly the same:

<table>
<thead>
<tr>
<th>The “old” way of writing</th>
<th>A new way of writing</th>
</tr>
</thead>
<tbody>
<tr>
<td>$876 = 800 + 70 + 6$</td>
<td>$876 = 800 + 70 + 6$</td>
</tr>
<tr>
<td>$254 = 200 + 50 + 4$</td>
<td>$254 = 200 + 50 + 4$</td>
</tr>
<tr>
<td>$876 - 254 = 600 + 20 + 2$</td>
<td>Subtract corresponding parts.</td>
</tr>
</tbody>
</table>

Once the above is on the board, you may explain that the last step can be written down in a different way, and demonstrate it on the right as shown in red below:

<table>
<thead>
<tr>
<th>The “old” way of writing</th>
<th>A new way of writing</th>
</tr>
</thead>
<tbody>
<tr>
<td>$876 = 800 + 70 + 6$</td>
<td>$876 = 800 + 70 + 6$</td>
</tr>
<tr>
<td>$254 = 200 + 50 + 4$</td>
<td>$254 = 200 + 50 + 4$</td>
</tr>
<tr>
<td>$876 - 254 = 600 + 20 + 2$</td>
<td>Subtract corresponding parts.</td>
</tr>
</tbody>
</table>

To encourage learners to apply their minds to your presentation, you may at this stage ask them to copy what you have written into their books, and to complete the calculations in both the “old” and new ways of writing.

Note that question 3 requires learners to use the new “vertical” format, but to write the place value expansions of the numbers down. In question 4, on page 227 of the Learner Book, learners are invited to try to do the calculations by just keeping the place value expansions in their mind, and not writing them down.

**Answers**

1. (a) 622  (b) 3314  (c) 4378  (d) 55134

2. Learners describe what they did in question 1(b) and (d) by following the instructions.

3. Learners follow the instructed method to find the answers:
   (a) 2643  (b) 25260

When you calculate $876 - 254$ by breaking down the numbers into place value parts and building up the answer, you can write this to show how you are thinking:

- $876 = 800 + 70 + 6$
- $254 = 200 + 50 + 4$
- $876 - 254 = 600 + 20 + 2$

This way of writing is sometimes called “the expanded column notation”, because the numbers are written in expanded notation.

You can also record your thinking in the “vertical” way shown below.

- $876 = 800 + 70 + 6$
- $254 = 200 + 50 + 4$
- $876 - 254 = 600 + 20 + 2$

This way of writing subtraction is called **subtraction in columns**.
Teaching guidelines
The requirement not to write the place value expansions in Grade 5 should not be rigidly enforced. Learners who need to write expansions in order to have clarity on what calculations to do should be allowed to do so.

Answers
4. Learners are to set out the work as instructed.
   (a) 5 412    (b) 9 503    (c) 52 322    (d) 41 524
5. (a) 4 402    (b) 6 353    (c) 35 261    (d) 44 223
6. (a) 40 000    (b) 5 437
7. 63 352 = 3 353 + 59 999
   63 352 − 27 685 = 59 999 − 27 685 + 3 353
   = 32 314 + 3 353
   = 35 667
8. Learners do the calculations by writing in columns.
   (a) 5 664    (b) 26 556    (c) 42 315    (d) 42 550
9. 38 965 other kinds of vehicles
4.3 Less writing when adding in columns

**Mathematical notes**

Traditionally, addition with carrying was set out as shown on the right for $4\,697 + 8\,956$. The blue marks, from right to left, actually indicate 10, 100 and 1 000. When the marks are read as “1”, “1” and “1” and the thinking for the tens column is “$1 + 9 + 5 = 15$”, for the hundreds column “$1 + 6 + 9 = 16$”, and for the thousands column “$1 + 4 + 8 = 13$”, learners’ awareness and understanding of place value and of the actual numbers four thousand six hundred and ninety-seven and eight thousand nine hundred and fifty-six may be seriously undermined.

With a view to maintain learners’ awareness and understanding of place value and of the actual numbers involved, the transition from separate recording of the column totals (part answers) to the traditional condensed form of the column format is introduced gradually through the phases demonstrated below.

\[
\begin{array}{cccc}
4\,697 & + 8\,956 & \rightarrow & 13 653 \\
\downarrow & \downarrow & \Rightarrow & \downarrow \\
4\,697 & + 8\,956 & \rightarrow & 13 653 \\
140 & 10 & \rightarrow & 1500 \\
1\,500 & 100 & \rightarrow & 1000 \\
12\,000 & 1\,000 & \rightarrow & 13\,653 \\
13\,653 & 1\,000 & \rightarrow & 13\,653 \\
\end{array}
\]

Page 228 of LB  Page 228 of LB  Page 229 of LB  Page 230 of LB

**Form A**  **Form B**  **Form C**  **Form D**

**Teaching guidelines**

You may write Forms A and B above on the left and right sides of the board respectively and explain the various steps as shown in the tinted passage, indicating that Form A and Form B are just two different ways of capturing the same thinking in writing. A more detailed description of how the presentation may proceed is given on page 229.

It is advisable to repeat the above presentation with different numbers, for example for $6\,857 + 4\,685$.

Note that in order to be able to add multi-digit numbers, learners can use Form A, i.e. add the different place value parts individually and then add up the column totals. The value of taking the trouble to learn to use Form D is that it may proceed a bit faster than Form A if performed confidently, and it also saves writing space. Learners who lose the capacity to use Form A, and use Form D without confidence and understanding, and make mistakes, are worse off than learners who do not progress beyond Form A.
Teaching guidelines

Let learners do question 1. Note that the writing format forces them to break down the part answer (column total) for each column before they write something down. They have not done this before, hence they may find it a bit difficult to adapt to this way of working.

Suggest to learners who really struggle that they first do question 1(a) by writing the column totals separately as they did in Section 4.1, then rewrite their work in the form indicated in the example for $4,697 + 8,956$. You may also repeat the presentation in which Form A (see previous page, writing each column total down separately) is compared to Form B (writing the place value parts of the column totals separately), for $8,956 + 7,688$, or other numbers.

It serves little purpose to proceed to Form C as described in the tinted passage with learners who are not confident in using Form B. Learners who still lack confidence when they do question 1(c) should be allowed additional practice in using Form B, for example the following:

\[
\begin{array}{ccc}
6,489 + 8,745 & 7,765 + 8,588 & 4,865 + 4,567 + 5,243 \\
47,586 + 9,565 & 35,657 + 47,754 \\
\end{array}
\]

Learners who are able to use Form B confidently when they have finished question 1, may be allowed to proceed on their own by reading the tinted passage and engaging with the exercises that follow.

Answers

1. (a) $7,688 + 45,847$ (b) $38,586$ (c) $8,867$ (d) $26,783$ (d) $55,378$

\[
\begin{array}{cccc}
+8,567 & +37,586 & +26,795 & +7,968 \\
15,145 & 72,323 & 54,271 & 16,835 \\
10 & 10 & 10 & 10 \\
100 & 100 & 100 & 100 \\
1,000 & 1,000 & 1,000 & 1,000 \\
10,000 & 10,000 & 10,000 & 10,000 \\
16,255 & 83,433 & 65,381 \\
\end{array}
\]

2. (a) $45,886 + 38,657$ (b) $26,783 + 48,894$ (d) $55,378 + 28,257$

\[
\begin{array}{cccc}
12,543 & 100 & 13,653 \\
\end{array}
\]

3. $7,668 + 8,897$

\[
\begin{array}{c}
16,565 \\
\end{array}
\]

Do not pressurise learners who do not manage this.
Teaching guidelines
Once learners have completed question 4, let them calculate 34 697 + 48 956, thinking and writing any way they prefer. Let them then look at the tinted passage and identify which of A, B, C and D best describes their own work.

Answers
4.  
45 886 = 40 000 + 5 000 + 800 + 80 + 6 
38 657 = 30 000 + 8 000 + 600 + 50 + 7 
45 886 + 38 657 = 70 000 + 13 000 + 1 400 + 130 + 13 
= 80 000 + 4 000 + 500 + 40 + 3 
= 84 543 

5. (a) 94 525  
(b) 64 623  
(c) 89 047  
(d) 67 894  
(e) 85 762  
(f) 65 956
6. R47 029 
7. 76 343 houses

4. Show how your work for question 2(b) can be written in the way you wrote in Terms 1 and 2 (the “expanded column notation”), before you learnt to write in the vertical way.

Here are four different ways to write the work vertically when you calculate 34 697 + 48 956:

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>34 697</td>
<td>34 697</td>
<td>10 000</td>
<td>11 11</td>
</tr>
<tr>
<td>+</td>
<td>48 956</td>
<td>48 956</td>
<td>1 000</td>
<td>34 697</td>
</tr>
<tr>
<td></td>
<td>13</td>
<td>83 653</td>
<td>100</td>
<td>83 653</td>
</tr>
<tr>
<td>+</td>
<td>1 500</td>
<td>1 500</td>
<td>48 956</td>
<td></td>
</tr>
<tr>
<td></td>
<td>12 000</td>
<td>10 000</td>
<td>83 653</td>
<td></td>
</tr>
<tr>
<td></td>
<td>70 000</td>
<td>10 000</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>83 653</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The symbols “1”, “1”, “1” and “1” at the top of D actually mean 10, 100, 1 000 and 10 000, as shown in C.

You can use any of the above ways of writing, but you should try to get used to making transfers and writing like in B, C or D.

In fact, it would be good if you can learn to make the transfers without any writing to remind you of the 10, 100, 1 000 or 10 000, as shown on the right.

34 697
+ 48 956
83 653

5. Calculate.
(a) 57 685 + 36 867 
(b) 27 858 + 36 765 
(c) 65 483 + 23 564 
(d) 13 537 + 33 148 + 21 209 
(e) 27 334 + 58 428 
(f) 43 569 + 22 387

6. Ben earns R14 786 each month, Sally earns R16 787 and Zweli earns R15 456. How much do they earn together?

7. There are 57 866 houses in a large township. How many houses will there be if 18 477 more houses are built?
4.4 Another way of subtracting in columns

Mathematical notes
It is important to realise that learners are not dependent on the breaking down and building up method of subtraction in column format, or any other format, to be able to subtract with multi-digit numbers. Adding on as demonstrated at the top of the tinted passage is a highly effective method of subtraction. It works in the same way for all numbers and does not present technical difficulties like those that require transfer (“borrowing”) in the traditional breaking down and building up method.

Teaching guidelines
Three different methods of subtraction are demonstrated in the tinted passage:

- adding on method
- change-and-compensate method
- transfer method or borrowing method.

Demonstrate the three methods for 63 543 – 27 688 on the board. You may skip the different shorter ways of writing up the transfer method, given at the bottom of the tinted passage.

Let learners then engage with questions 1, 2, 3 and 4 on the next page.
Answers
1. Learners do the calculations using the borrowing method.
   (a) 2 464
   (b) 33 646
2. Learners check their answers for question 1 using the adding on method.
3. Learners do the calculations using the borrowing method.
   (a) 44 547
   (b) 55 869
4. Learners check their answers for question 3 using the change-and-compensate method.

4.5 Solve problems

Teaching guidelines
You may suggest to learners that if they are unclear about what calculation to do, they could first write a number sentence to represent the situation. The number sentence may help learners to make a correct calculation plan. Number sentences that describe the situations in some of the questions are given below.

Question 1: \( \square + 35 255 = 89 034 \), which indicates the calculation plan \( 89 034 - 35 255 \).

Question 2: \( 35 794 + \square = 45 880 \), which indicates the calculation plan \( 45 880 - 35 794 \).

Question 3: The number sentence is \( \square - 10 550 = 79 600 \). However, in this case learners may have less trouble to identify the calculation plan \( 79 600 + 10 550 \) directly, without describing the situation with a number sentence first.

For questions 4 and 5 the appropriate calculation plans 21 876 + 35 889 and 19 655 – 18 564 are easy to identify, and it serves no purpose to write number sentences.

Question 6: If learners do not see immediately that they have to subtract 79 093 from 85 084, it may help them to write the number sentence 79 093 + \( \square \) = 85 084.

Answers
1. 53 779 hectares
2. 10 086 chickens
3. 90 150 impalas
4. 57 765 m
5. R1 091
6. 5 991 km
Grade 5 Term 3 Unit 5  Viewing objects

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>5.1 Different views of the same object</td>
<td>Objects look different when viewed from different positions</td>
<td>233</td>
</tr>
<tr>
<td>5.2 What you see from different places</td>
<td>More about the way objects look when seen from different positions</td>
<td>234 to 235</td>
</tr>
</tbody>
</table>

**CAPS time allocation**
3 hours

**CAPS page references**
23 and 184

**Mathematical background**
This unit is about taking more careful notice of how the same object can look very different when it is viewed from different positions.

This awareness is important when one aims to develop learners’ spatial sense of three-dimensional objects. It is also important when one has to draw a three-dimensional object, especially if the object is not a simple one. One will then draw such an object as seen from a number of different positions. Together the drawings become a useful tool to understand the total spatial form of the object. Such drawings are routinely used in the technical fields (e.g. civil and mechanical engineering) during the design process.
5.1 Different views of the same object

Mathematical notes
This section introduces the importance of being able to imagine what an object looks like from different positions.

Teaching guidelines
Although this section focuses on being able to reason from given drawings, it would be very rewarding to make some simple objects available to learners to draw (perhaps some of the paper objects they folded in Term 2 Unit 6).

You could set the learners up in small groups around a table on which you place an object. Some may lean over the object and some may sit below it (i.e. lower than the table), while others sit around it. Ask each learner to draw the object as they see it. Once all learners have done their drawings, allow them to compare them. Let the learners shift their positions to allow them to confirm the view seen by other members in the group.

Question 3 is tough. It is acceptable if learners do not get it right at this stage. Learners may return to this question once they have completed the unit.

Answers
1. Learners’ own work. Elements in the learners’ paragraph could include: the mug is held upside down with the ear of the mug towards the right, the mug is being turned clockwise, the mug is turned 1 fifth of a half turn from picture to picture until the mug is upright in Picture F. Allow learners to articulate themselves what it is that they see.

2. As in Picture B

3. [Diagram of a mug being held in different positions]
5.2 What you see from different places

Mathematical notes
The ideas in the previous section are formalised here. Depending on the object being viewed, there could be certain views that are more useful than others. Top and bottom views are often very helpful, as well as side views showing different faces, or side views that show the symmetry of the object. Sometimes, however, we may have to represent an object from a less obvious position, which could result in many of the properties of the object being hidden (e.g. question 1(b) Picture 4).

Teaching guidelines
Again, time and resources permitting, allow your learners to draw actual objects and plans (in the classroom, on the playground, in the school hall, etc.). Now, however, engage them in a discussion about which positions are the most useful to show the properties of the objects, especially when it comes to faces and symmetries of the objects, and to plans of room layouts. Alternatively, talk to them about how a room’s layout or an object may appear from a particular position (a greater challenge).

Answers
1. (a) Picture 4
   (b) Person B: Picture 3
       Person E: Picture 1
       Person F: Picture 2
   (c) 

![Diagram](image)
Teaching guidelines
Allow learners to explain their answers for question 2 to each other. It will be important for you to observe the kind of descriptions that they are giving.

Answers
2. (a) Piet is standing at A.
   (b) Jaamiah is standing at C.
   (c) Tebogo is standing at B.
Grade 5 Term 3 Unit 6 Properties of two-dimensional shapes

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.1  Draw figures on grid paper</td>
<td>Making the case for the need for tools to make good drawings of shapes</td>
<td>236 to 237</td>
</tr>
<tr>
<td>6.2  Figures with equal sides and right angles</td>
<td>Exploring the possibilities resulting from these two requirements</td>
<td>238 to 239</td>
</tr>
<tr>
<td>6.3  Figures inside circles</td>
<td>Drawing circles, choosing points on them and joining them to form polygons</td>
<td>240 to 241</td>
</tr>
</tbody>
</table>

**CAPS time allocation**
4 hours

**CAPS page references**
21 to 22 and 184

**Mathematical background**
The issue of how to draw good copies of given shapes may have arisen in your class in Term 1 Unit 8 (Section 8.5). Even if it did not, at this point some of your learners may be asking how they can draw better versions of shapes. This is the focus of Section 6.1. One way is to make use of square grid paper.

The requirement “shapes with equal sides and right angles” is raised in Section 6.2. By a process of elimination learners are led to the conclusion that only squares fit the bill. The process of coming to this conclusion is important. Many mathematical ideas are discovered by asking a simple question and investigating the possibilities that result. So, do not refer to squares or any specific polygons while learners are going through this process.

In Section 6.3, the usefulness of circles in drawing certain polygons is introduced. If one draws a circle and marks off some points on its circumference and then joins these points with straight lines, polygons are formed. This is an important germ idea that leads to a great deal of important mathematics later. This introduction will focus on drawing squares, rectangles and regular hexagons.

**Resources**
Square grid paper (see pages 412 and 413 in the Addendum); loose sheets of paper; round objects such as tins, small lids or saucers (see Section 6.3 on page 264 of this Teacher Guide)
6.1 Draw figures on grid paper

Mathematical notes
This section focuses on drawing polygons (primarily triangles and quadrilaterals) on square grid paper. Often the angles at the corners of polygons drawn on such a grid can easily be checked to see if they are smaller than right angles, bigger than right angles or exactly right angles.

Mathematics often involves finding out what sorts of things meet a set of mathematical conditions. Finding out usually takes time and several attempts. Mathematics is not always about knowing the answer quickly, nor about always knowing immediately how to work out the answer. Sometimes a lot of mathematics is learnt through trial and error.

Teaching guidelines
The material in this section is sophisticated, because learners are asked to decide whether a given figure meets some conditions (question 2). Learners are also asked to try to draw figures with certain conditions or characteristics (questions 1 and 3). Sometimes it is not possible to draw figures with the required conditions. Allow your learners to work through these conditions carefully. Resist the temptation to help them to the “answer”. Explain to them that they are not expected to know the answers straightaway and that they should expect to make several attempts before drawing an answer or reaching a conclusion. Support learners’ struggles by engaging them in conversation that allows them to make headway under as much of their own power as possible. They will benefit greatly from the experience.

In question 2 learners use grid paper to help them decide whether a figure meets certain conditions. In question 3 they use grid paper to draw figures that must have a particular set of characteristics. If you have access to the internet, you can download and print copies of grid paper. You could also photocopy the grid paper provided in the Addendum on page 412 or 413, or you could remind learners how they were shown to make their own grid paper on page 102 of the Grade 4 Learner Book (see the extract alongside).

Answers
1. (a) to (e) Learners’ own drawings
**Answers**

2. (a) The red quadrilateral
   (b) The black quadrilateral

3. (a) Impossible
   (b) Learners' own drawings; these may differ.
   (c) Impossible
   (d) Learners' own drawings; these may differ.
   (e) Impossible
   (f) Impossible

---

You can make your own grid paper by drawing vertical lines on ruled paper. Your vertical lines must be the same distance from each other as the lines on the ruled paper are.

The black triangle above has only one right angle. It has two angles that are smaller than right angles.

2. (a) Which quadrilateral above has only two right angles?
   (b) Which quadrilateral has four equal sides?

3. Try to draw the figures described below. Use grid paper. If you find that it is impossible, state it in writing.
   (a) a triangle with two right angles
   (b) a quadrilateral with only one right angle
   (c) a quadrilateral with only three right angles
   (d) a triangle with three angles all smaller than a right angle
   (e) a quadrilateral with four angles all smaller than a right angle
   (f) a quadrilateral with four angles all bigger than a right angle
6.2 Figures with equal sides and right angles

Mathematical notes
As mentioned in Section 6.1, mathematics often involves finding out what sorts of things meet a set of mathematical conditions. This section offers examples of such problems.

The only two-dimensional shapes that have equal sides and right angles only are squares. But do not tell your learners this until the end of the section.

The definitions of rectangles and squares are quite sophisticated. A rectangle is any quadrilateral with four equal angles. These are always right angles. According to this definition a square is also a rectangle: all squares have four right angles. So it makes sense to define squares as rectangles with four equal sides.

Possible misconceptions
Some learners will resist the idea of a square being a special rectangle. The issue here is: “Does a square have four equal angles?” Well, yes. “Does a square have other characteristics that rectangles do not have in general?” Yes, its sides are equal. Then a square must be a special rectangle, one with four equal sides. Part of the problem is that many learners have been taught that a rectangle is a shape with two long sides and two short sides. This is not a good definition of a rectangle.

Teaching guidelines
You can start by reminding learners that although we often categorise things in the world around us into separate categories, for example dogs and cats, we do not always do this. Sometimes one grouping is a sub-grouping of another. You can give them examples where one group is a special kind of another group. You can, for example, ask them: “Are all girls people?”, “Are all people girls?”, “Are all chickens birds?”, “Are all birds chickens?”, “Is red a colour?”, “Are all colours red?” Ask them to think of other examples. Then discuss the given definitions of rectangles and ask them whether squares also have these characteristics.

Learners may find it easy to identify right angles where the sides of figures coincide with the grid lines, for example in Figures D and F. However, they may find it more difficult to identify right angles in figures where the sides do not coincide with grid lines. In these examples learners should use right-angle templates (see Learner Book page 99) to check for right angles. Learners can also check the lengths of sides in these examples by making length templates, i.e. marking off lengths on the edge of a sheet of paper.

Answers
1. (a) Four equal sides: A, B, E, F  (b) Four right angles: B, D, F  
   (c) Four equal sides and right angles: B, F
2. (a) Rectangles: B, D, F  (b) Squares: B, F  
   (c) Rectangles only: D  (d) Four equal sides, but not squares: A, E
**Teaching guidelines**

Your learners may need a great deal of support to make proper sense of this section, especially from question 3 onwards. As far as possible, help learners to understand the instructions so that they attempt each question meaningfully. It is more important that learners experience making sense of instructions than rushing to get all the questions done. You can remind learners to ask themselves: “Is there anything that I have done or seen before that can help me here?” It is important that learners see mathematics as connected and not as isolated, disconnected bits of information.

Question 5 is a challenging question that can be used for extension. You might like to prepare for this question by trying to find some counter-examples to each statement. These will prove the statements false. However, do not teach or show these to learners; let them find examples for themselves.

**Possible misconceptions**

Sometimes learners think that if they find one correct answer the statement is true. This is not correct. A statement is only true if *all* possible examples of it are true. However, a statement is false if *one* example of it is false. You only have to find one counter-example to show that a statement is false.

**Answers**

3. (a) to (e) Learners’ own drawings; drawings will differ from learner to learner.

4. (a) to (d) Learners’ own drawings; drawings will differ from learner to learner.

5. (a) False (b) False (c) True (d) True (e) True (f) True (g) False

3. Make drawings of the following figures on grid paper:
   - (a) a rectangle with two sides longer than the other two sides
   - (b) a quadrilateral with no right angles and four equal sides
   - (c) a rectangle with four equal sides
   - (d) a pentagon with two right angles, and three angles bigger than right angles
   - (e) a pentagon with two right angles, and one angle smaller than a right angle

4. Make drawings of the following figures on grid paper:
   - (a) a quadrilateral with three right angles
   - (b) a quadrilateral with only two right angles
   - (c) a quadrilateral with only one right angle
   - (d) a quadrilateral with no right angles and no equal sides

5. Which of the statements below are false, and which statements could be true?
   It may help you to think about what you did in question 4. In some cases you may need to make new drawings.
   - (a) If a quadrilateral has only two right angles, the other two angles are both smaller than right angles.
   - (b) If a quadrilateral has only two right angles, the other two angles are both bigger than right angles.
   - (c) If a quadrilateral has only two right angles, one of the other angles is smaller than a right angle.
   - (d) If a quadrilateral has only one right angle, one or two of the other angles are smaller than right angles.
   - (e) If all the angles of a figure with straight sides are right angles, it is definitely a quadrilateral.
   - (f) If one angle of a quadrilateral is smaller than a right angle, then one or more of the other angles are bigger than right angles.
   - (g) If one angle of a triangle is smaller than a right angle, then one of the other angles is definitely bigger than a right angle.
6.3 Figures inside circles

Mathematical notes
This section is about using circles as tools to draw polygons. In particular, this section is about squares, rectangles and regular hexagons.

Teaching guidelines
Because learners will need to fold their initial circle to find its centre, it is better if they do this section on loose sheets of paper. The sheets should be pasted into their exercise books afterwards.

Some learners may identify the figures in questions 1(e) and 2(c) by sight. If learners cannot identify the figures by sight, ask them questions such as: “What kinds of quadrilaterals do you know?”, “What properties do the quadrilaterals you have listed have?”, “How can you check or test to see whether these quadrilaterals meet these conditions?”

Answers
1. (a) to (d) Learners’ own work
   (e) Square
2. (a) and (b) Learners’ own work
   (c) Rectangle

A regular hexagon has six equal sides and six equal angles.
A circle can be drawn tightly around a regular hexagon.
You can follow the instructions on the next page to draw a regular hexagon accurately.
Answers

3. (a) to (f) Learners’ own work

3. Follow the instructions to draw a regular hexagon accurately.

(a) Use a round object to draw a circle in the middle of a clean sheet of paper.

(b) Fold the sheet twice to find the centre of the circle.

(c) Draw another circle that passes through the centre of the first circle.

(d) Your two circles meet in two points. Draw a third circle that passes through one of these points, and the centre of your first circle.

(e) Draw another circle in this way so that your drawing looks like this. Mark the midpoints of the three outer circles as accurately as you can.

(f) Draw lines between points on your first circle to form the regular hexagon.
Grade 5 Term 3 Unit 7  
Transformations

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**CAPS time allocation**  
3 hours

**CAPS page references**  
23 and 185

**Mathematical background**
Any relocation of a shape can be achieved by a combination of three types of movement, called “transformations”:

- shifting (translating) it in a particular direction, through a particular distance, without rotating it
- swinging (rotating) it around a particular point outside or on the shape, through a particular angle
- flipping it over (reflecting it), i.e. picking it up, turning it over and placing it down again.

Reflecting a shape always produces symmetry. The axis of reflection (the broken line in the above figure) is the line of symmetry.

If two identical shapes lie on the same flat surface it is always possible to get one of the two shapes to fit exactly on top of the other by performing a translation, rotation or reflection, or a translation and a reflection (a so-called “glide-reflection”).

Translations, rotations and reflections do not change the form or size of a shape. Other kinds of transformations, for example enlargements, do change the size. There are also transformations that change the shape, such as stretching in one direction.

Patterns are formed when the same transformation or set of transformations is repeatedly applied to the same shape, for example:

**Resources**
Loose sheets of paper, cardboard (e.g. from tissue or cereal boxes), glue, scissors, pins
7.1 Making patterns by moving a shape

Mathematical notes
This section is about exploring the three basic transformations before they are identified and defined towards the end of the section.

Teaching guidelines
It is important to first give learners the opportunity to find their own words to describe the different transformations of the shape (glass tile) in Patterns A, B and C. Ensure that your learners engage meaningfully with the activities. Resist the temptation to jump ahead and tell them about translations, rotations and reflections. Allow them to struggle with describing the patterns.

Describing their own observation of how the position of a shape is changed is an important part of developing an understanding of the different transformations.

It is very important that learners actually write down their attempts to describe the three patterns. (They will return to these descriptions and try to improve them at the end of the section when they do question 7.)

If time permits, it would be valuable if learners could tell each other in small groups or pairs how they described the patterns.

Answers
You cannot expect learners to use the terms translation, reflection and rotation when they respond to question 1. It will be very valuable for you to read or listen to as many of the learners' answers as possible, but it makes no sense to try to assess their answers. The question serves to get learners to begin to form language that can be used to describe the patterns. Some of the things learners may say are given below.

1. (a) Pattern A: The tile is repeated five more times; it is simply moved along a straight line towards the right.
Pattern B: The tile is also repeated, but it is only repeated four more times. However, it is not simply moved along as in Pattern A but turned to the right each time in such a way that after the first and third turns, it is rests on one of its long sides.
(b) Pattern A: The tile is repeated five more times; it is moved along a straight line without being turned or turned over.
Pattern C: The tile is also repeated five more times but it is turned over (flipped) each time.

1. (a) Describe how Patterns A and B differ from each other.
(b) Describe how Patterns A and C differ from each other.
**Teaching guidelines**

You will need a larger template with the same shape to do the questions on the board at some stage during the lesson.

Learners may focus primarily on putting the template down into each of the positions without being aware of how they may move the template from the position on the left to the position on the right in each question.

Learners may manage to move the template from the positions on the left to the positions on the right in many ways, and they will not necessarily become aware of the simple movements: slide along a straight line (translate), swing around a point (turn, rotate) and turn over (reflect) in a line.

After learners have engaged with questions 3 to 5 on their own, tell them that the questions can be done with very simple movements. Then demonstrate on the board that question 3 can be done by keeping your elbow fixed at a point some distance below and between the two positions, and swinging the template from the one position to the other.

Similarly demonstrate that for question 4 the template can be slid in a fixed direction without turning it, but that for question 5 you have to lift the template off the board and turn it over to land on the second position.

Ask learners to copy your movements for the three questions. You may have to repeat the demonstrations on the board a few times. Continue until all learners get it right. Only then ask them to do question 6. Do not provide them with terms that may be used to describe the three kinds of movement: allow learners to come up with their own ways of describing the movements.

Learners may find question 6 challenging. It is quite important that they persevere and manage to write some descriptions of the three kinds of movement down. The attempt to describe the movements in words will support the formation of the concepts of translation, rotation and reflection in their minds.

**Answers**

2. to 5. Learners’ own work

6. Refer to “Teaching guidelines” above; guide the learners to find the correct articulation.

6. Describe the different ways in which you moved your template when you did questions 3(b), 4(b) and 5(b).
**Teaching guidelines**
Demonstrate questions 3, 4 and 5 again and now tell learners what the three kinds of movement are called: rotation, translation and reflection.

For homework or additional practice, you may ask learners to try to improve their answers for question 1.

**Answers**
7. (a) Pattern B  
   (b) Pattern C  
   (c) Pattern A

---

**Answers**
7. (a) Which of the three patterns can be made by repeatedly rotating the glass tile?  
   (b) Which of the three patterns can be made by repeatedly reflecting the glass tile?  
   (c) Which of the three patterns can be made by repeatedly translating the glass tile?
7.2 Rotations

Mathematical notes
Rotations involve turning a shape around a fixed point (the centre of rotation).

Teaching guidelines
The rotation tool is very useful in getting the key properties of rotations across to your learners: there is a point around which rotations occur, and the rotated shapes are all the same distance from that point. Perhaps it would be wise to make other rotation tools available (with other shapes). The value of this tool is that your learners will do rotations instead of just looking at them.

For enrichment, in question 5 you may repeat the triangle rotation activity in two other ways:

- First, make a small hole in the triangle and pin the triangle to the page. Rotate it and draw the triangle in a number of positions.
- Second, glue a strip of cardboard to the triangle and make a hole at the end furthest from the triangle. Pin it through the hole and rotate, drawing the triangle in a number of positions. This activity will highlight to learners that a centre of rotation can be in many positions.

Possible misconceptions
There is a risk that learners will confuse the three types of transformation. Ask them if any of the drawings they made have translations or reflections in them. A short discussion should lead to a general consensus that rotations do not involve reflections or translations of the shapes they have used in questions 1 to 6.

Answers
2. (b) Circle
Notes on questions
You can ask learners to first familiarise themselves with the given pentagon. This will allow them to notice the different side lengths in order to identify the specific transformations in Figures A to E. Learners must be given the opportunity to find the words to describe the transformations they observe. Refer them to the description of the different transformations on page 244.

Answers
3. Figure A: 3 times  Figure B: 4 times
   Figure C: 7 times  Figure D: 3 times

4. (a) The rotation in the two figures is the same, but in Figure E the pentagons are also reflected.
   (b) Learners' own work, for example:
       Pin the rotation tool to the middle of a sheet of paper. Trace around the pentagon. Unpin the rotation tool, turn it over (reflect it) and re-pin it with the pin in the same as position as before. Turn the rotation tool a bit to the right (or the left, if you prefer) and trace around the pentagon. Repeat six more times, always working in the same direction.
   (c) Learners' own work
**Teaching guidelines**
You may advise learners who experience difficulties with questions 6(b), (c) and (d) to move their cut-out triangle on the coloured drawing, to try to figure out what the answers to the questions are.

**Answers**
5. Learners’ own work
6. (a) Learners’ own work
   (b) The yellow triangle is a translation of the red triangle.
   (c) Yes, combined with a translation.
   (d) No, it is a reflection combined with a translation.
7.3 Reflections and translations

Mathematical notes
This section aims to clarify the special characteristics of translations and reflections. Translations involve moving a shape from one position to another without changing its orientation. Reflections involve flipping a shape over a line of symmetry.

Teaching guidelines
A reflection tool is introduced. It is a piece of paper folded in half. The fold is the line of symmetry. A shape is drawn on one side of the fold and “transferred” with pinpricks to the other side, creating a mirror image.

A translation tool is also introduced. It is a piece of paper with a shape on it that is shifted along a line on a sheet of paper to another position where the shape is transferred by pin pricks.

As with the rotation tool in Section 7.2, the aim is to give learners a chance of doing the transformation, and not just seeing it. Give them ample time to do so meaningfully. Their understanding of the three transformations will be richer for it.

Possible misconceptions
Ask learners questions such as: “Can a rotation of this shape ever be the same as a reflection of the same shape?”, “Can a translation ever be a rotation?”

Note: With most shapes, the three transformations are quite different. However, with some, for example circles, a translation could be seen as a rotation or as a reflection. This has to do with the perfectly regular/smooth shape of a circle. When it comes to transformations of an individual point, the same is true. In general, however, the three transformations behave differently.

Answers
1. (a) to (d) Learner’s own work
2. (a) The blue hexagon
   (b) The blue hexagon and the black hexagon
Answers

3. Learners’ own work

4. (a) to (e) Learners’ own work

3. Draw a hexagon on a rectangular piece of paper about this size, and punch small holes at the six corners of the hexagon.
You will use this template to draw translations, reflections and rotations.

4. Follow these instructions to draw translations of the hexagon on your template.
(a) Draw a straight line across the width of a blank sheet of paper.
(b) Put the bottom edge of your template against the line as shown below.
(c) Make marks through the six holes, so that you can later draw a copy of the hexagon by joining the marks with lines.
(d) Slide your template to a new position, but keep the bottom edge against the line that you have drawn.
(e) Make marks through the six holes again, for another copy of the hexagon.
Answers
4. (f) Learners’ own work
5. Learners’ own work
6. No. It has to be reflected in a vertical line of symmetry.
7. Learners’ own work
8. The pattern can be made by a rotation together with a reflection of the hexagon.
Answers

9. Translation

10. (a) Reflection (b) Reflection
    (c) Rotation (d) Reflection
    (e) Rotation (f) Reflection

11. (a) Figure A (b) Figures A and B
    (c) Figures A and B (d) Figures A and C
Grade 5 Term 3 Unit 8  
Temperature

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**CAPS time allocation**  
2 hours

**CAPS page references**  
28 and 186

**Mathematical background**
In Term 2 we saw that a unit of length is very useful when we need to tell someone, for example, how long a piece of dress material must be. If everyone agrees on the same unit of measurement, then people can communicate without getting confused.

In the same way we can communicate about temperature if everyone agrees on a unit of temperature – the degree Celsius (°C). Then everyone can understand a recipe book that says “heat the oven to 140 °C”.

The mathematics involves the following:
- reading scales on thermometers, marked in degrees
- understanding fractions of a degree
- recording and reporting on temperature measurements
- understanding that each type of thermometer has a temperature range; most thermometers cannot measure very high or very low temperatures.

We can subtract temperatures to find differences, which tell us how much a temperature has increased or decreased. We cannot add temperatures. (If we have a cup of hot water at 60 °C and another at 40 °C, and we pour the water into a jug, we don’t get water at 100 °C.) We also don’t multiply a temperature by a temperature, nor divide a temperature by a temperature.

**Resources**
Long thermometer from the school’s science kit, if available; smartphone, if available
8.1 Estimating and measuring temperature

**Teaching guidelines**

You should do some language work on this text.

Ask learners to give examples of the environment. The environment is all of the world around us, excluding us. So the learners’ desks and books are part of their environment, and so are the walls of the classroom and the air in the classroom. For each learner, the other people around him/her are part of his/her environment.

A *sealed* glass tube is a hollow tube, like a plastic or paper straw, that has been melted in a hot flame so that it is closed or *sealed*.

Try to borrow a long thermometer from the school’s science kit. Show it to the learners. They should see the liquid inside the glass tube, and see that most of the liquid is in the pointy end, called the *bulb*.

Notice that the markings go from minus 10 °C up to 110 °C; this is called the *range* of the scale: −10 to 110 °C. (Some thermometers only go up to 50 °C.)

The liquid inside the tube is usually red-coloured alcohol. When the liquid gets hot, it gets bigger (it *expands*) and it pushes along the tube. For example, if you hold the bulb in your fist, it warms up until it is at the same temperature as your skin.

When learners are looking at the thermometer, it is showing the temperature of the air in the classroom. If they put it into a cup of hot tea, the liquid expands until it shows the temperature of the tea.

Thermometers work if they are on their sides or if they are held upright. Try this with a real thermometer.

**Answers**

1. to 4. Practical activity
Teaching guidelines

The picture shows a real medical thermometer and the scale is not easy to read. Some learners might be completely lost and unhappy. So, before you ask for the answer to question 5, spend a few minutes helping learners to study the picture. Ask them, what is the number that they see to the right of the 35? (Answer: It is a 6.)

What is the next number they see? (Answer: 37, and it has a black arrow in the middle. We’ll explain later what this arrow means.)

What are the next three numbers? (Answer: 8, 9 and 40.)

This looks like a strange sort of scale; we expect it to go 35, 36, 37, 38, 39, 40.

The reason why some digits are missing is that there was not enough space on the thermometer to print them all – i.e. more print (digits) would have made it more difficult to read the scale. So the 6 really means 36, the 8 means 38 and the 9 means 39.

Then we see 40. Now ask learners to work out what the last number on the scale is. The answer is 42 °C.

Why spend time on studying the picture? Well, you are showing learners that when they meet a picture or diagram that is hard to understand, they should not give up and think: “I can’t do this.” Often they will be able to work out what information is missing in a strange diagram.

Answers

5. (a) 42 °C
   (b) Doctors and nurses use medical thermometers. They know that a living person cannot have a temperature lower than 35 °C. Also, they know that if a person’s temperature is as high as 42 °C the person is very, very sick with a fever. If his temperature goes past 42 °C, he or she will die.

6. (a) A: 36 °C  B: 41\(\frac{1}{2}\) °C  C: 39\(\frac{9}{10}\) °C
    D: 37\(\frac{3}{4}\) °C  E: 38\(\frac{4}{10}\) °C  F: 43\(\frac{7}{10}\) °C
   (b) A: 36 °C  B: 42 °C  C: 40 °C
    D: 38 °C  E: 38 °C  F: 42 °C
Answers

7. (a) 36 °C = A
   (b) 35 °C = E
   (c) $39\frac{1}{2}$ °C = H
   (d) $37\frac{1}{10}$ °C = F
   (e) $41\frac{8}{10}$ °C = J
   (f) $40\frac{1}{2}$ °C = C
   (g) two degrees below 40 °C = 38 °C = B
   (h) three and a half degrees higher than $35\frac{1}{2}$ °C = 39 °C = G
   (i) $40\frac{1}{4}$ °C = I
   (j) 41 °C = D
8.2 Weather temperatures

Teaching guidelines
Give learners enough time to think about their answers – ask the question and then silently count to ten by yourself before you take any answers. If you do this, you usually get better-quality answers and more thinking by the learners.

Answers
1. (a) Possible answers: People want to know whether they should put on warm clothes when they go out to school or to work. Farmers want to know whether their crops or animals will get so hot or so cold that they will suffer. People working outside want to know whether they should take water along to drink during the day.

(b) The question is asking learners to estimate the temperature of the air. Learners who don’t know about temperature may give very high or low estimates. Remind them of the information in the tinted passage on page 252. For example, a healthy person’s temperature is about 37 °C. Answers could be anything from 25° to 42 °C. It depends on your location.

(c) Answers could be anything from 20 °C down to minus 20 °C. It depends on your location.

(d) The temperature was probably lower in the morning than it is now.

(e) No, because the weather could change in the middle of the day or the middle of the night. A cold front could blow in at midday. The night-time temperature is usually lowest just before the sun comes up.

(f) You can have some very cold days in summer and some very warm days in winter, so the question is really asking about average temperatures in summer and in winter.

2. (a) 3 °C  (b) 5 °C

(c) Upington: 18 °C Bloemfontein: 13 °C Pretoria: 14 °C

Durban: 7 °C East London: 5 °C

(d) East London (e) Upington
Notes on questions
In question 4, learners are to record the temperature at 12 o'clock each day. Why take the air temperature at, say, 12 o'clock each day? The reason is that the temperature changes throughout the day. If we measure temperature at different times, we cannot say anything sensible about how the midday temperature changed during the days from Monday to Friday.

For this activity you will need one of those long thermometers that can measure from −10 °C to 110 °C. The school’s science kit might have one. An alternative to a thermometer is a smartphone, if available. Some smartphones have a temperature sensor and can show you the temperature at any time.

Answers
3. (a) 3 °C less than 0 °C. Ask learners how that feels. What unusual things would they notice as they walk to school? (They could notice white frost on the grass and some roofs, and people breathing out white clouds of water vapour.)
(b) 6 °C
(c) Pretoria: 19 °C Durban: 11 °C East London: 9 °C
(d) Durban, because the day and night temperatures are higher than in the other towns.
   Learners’ answers (preferences) may differ. Consider their arguments, for example:
   Durban, because it has the highest day/maximum temperature.
   Durban, because it is the town in which both the minimum and maximum temperatures are the highest.
   East London, because the difference between the maximum and minimum temperatures is the smallest.

4. Practical activity
Data handling

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| 9.2 Collecting and organising numerical data | Bar graph and pictograph of the same data tell different stories  
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**CAPS time allocation**
9 hours

**CAPS page references**
30 to 31 and 187 to 188

### Mathematical background

Data are bits of information about a particular context. We ask questions about a situation or context that lead to the collection of information. The way in which the data are organised and represented (and the further questions we ask) allows us to see trends in the data.

In data handling we work with large amounts of information related to particular contexts. Instead of focusing on each bit of information separately, the way we organise, represent and analyse the data gives us ways of talking in general about the data. We look at the data in a global way and draw out trends or characteristics which describe the data.

Data handling differs from other parts of Mathematics in three respects:

- **The answer to data questions is produced by analysing lots of data.**
  Data handling is necessary where measurements and frequencies vary and therefore one measurement cannot provide accurate information about a situation. Lots of different data can be confusing, so we organise the data we collect in different ways to get a “picture” of the situation. Different representations make different trends more visible.

- **The numbers we use in data handling always have some description of a category they belong to or some unit of measurement.**
  Learners work mostly with abstract numbers in Mathematics. In data handling, however, the numbers must be interpreted in a context. The same number 44 can be 44 learners or R44, depending on the question.

- **Data questions are always answered with a story about the context.**
  Data handling starts when we need to answer a question about a situation where the property we look at varies. The numerical answers we get by data handling must be interpreted to answer the question about the situation.
9.1 Collecting and organising data in categories

**Mathematical notes**

The fundamental purpose of data handling is to reorganise and represent data in such a way that it becomes easier to identify properties of the data that may be useful in making decisions in practical situations.

For example, the data on page 258 is very difficult to interpret in the form in which it is given. The questions in this section provide learners with opportunities to organise and represent the data in different ways, and to experience that this makes it easier to consider options and make decisions.

**Teaching guidelines**

Let learners look at the table on page 258 at the start of the lesson, and ask them to make short statements that describe the data. This will make them experience that the data in this form is difficult to interpret. Tell them that while doing the questions in this section, they will learn how to organise and represent data in different ways, which will make it easier to describe the data.

**Answers**

1. (a)

<table>
<thead>
<tr>
<th></th>
<th>Tallies</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Male</td>
<td></td>
<td>22</td>
</tr>
<tr>
<td>Female</td>
<td></td>
<td>37</td>
</tr>
<tr>
<td>Black</td>
<td></td>
<td>44</td>
</tr>
<tr>
<td>Blue</td>
<td></td>
<td>15</td>
</tr>
<tr>
<td>Zip</td>
<td></td>
<td>42</td>
</tr>
<tr>
<td>Pullover</td>
<td></td>
<td>17</td>
</tr>
</tbody>
</table>

(b) Learners’ reports will vary. The report should include the following information:

The total sample was 59 students. There were 37 females and 22 males.

Far more Grade 12s favoured black hoodies than blue hoodies: 44 students chose black hoodies and only 15 students chose blue hoodies.

Hoodies with zips were much more popular (42 students’ choice) than pullovers (17 students’ choice).
Mathematical notes
This table is typical of the form in which data obtained from a questionnaire may be recorded before it is analysed.

There are many ways in which the data can be reorganised to make hidden features visible. For example, separate tables can be made for males and females, and in each table all the responses that include black as the colour choice can be listed first.

Teaching guidelines
The main aim of this section is for learners to interpret and report on the data. In order to do so, they need to represent and analyse the data. More time should be spent analysing the data than counting the data in each category. You could divide the categories among learners, so that each learner tallies one category (there are six categories in question 1 and eight categories in question 3). Learners who have tallied the same categories can check their counts with each other.
Teaching guidelines
In question 3 you can ask learners what the purpose of the totals in the bottom rows and right-hand side columns of the tables is.

Once learners have completed question 4, you can ask them to compare the results that were shown in the tables in question 1 and question 3. Ask them what kinds of hoodies the Student Council would have purchased had they used the results from the table in question 1, and how this differs from the hoodies they would have purchased based on the tables in question 3. You can also ask learners why the first table shows that black hoodies with zips are most popular, while the later tables show that male students mostly prefer pullover hoodies.

Possible misconceptions
Some learners may not fill in 0 in the tables where the count is zero. This is wrong. They tend to reason “nobody wants that”, rather than give the numerical answer to “how many want that?”

Answers
2.  (a) Yes, 15 students want blue hoodies.

   (b) No. The tally table shows the number of female students, and the number of Grade 12s that like blue hoodies, but not the number of female students in Grade 12 that like blue hoodies.

3. 

<table>
<thead>
<tr>
<th>FEMALES</th>
<th>Black</th>
<th>Blue</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zip</td>
<td>30</td>
<td>5</td>
<td>35</td>
</tr>
<tr>
<td>Pullover</td>
<td>0</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>Total</td>
<td>30</td>
<td>7</td>
<td>37</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>MALES</th>
<th>Black</th>
<th>Blue</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zip</td>
<td>7</td>
<td>0</td>
<td>7</td>
</tr>
<tr>
<td>Pullover</td>
<td>7</td>
<td>8</td>
<td>15</td>
</tr>
<tr>
<td>Total</td>
<td>14</td>
<td>8</td>
<td>22</td>
</tr>
</tbody>
</table>
Answers

4. (a) The more popular of the two styles for females is the hoodie with a zip.
   (b) Seven out of 22 males preferred hoodies with zips. That is about one third of the males. Pullovers were more popular with males (15 out of 22).
   (c) Only 7 out of 37 females preferred blue hoodies. That is about one fifth of the females.
   (d) Black was the more popular colour amongst male students. Fourteen out of 22 male students chose black hoodies. That is more than half of the males.

5. Reports will vary. The report should include the following information:
   
   In total, there were 59 students who responded.
   There were 37 females who responded.
   Colour preference: By far the most females (30 out of 37) preferred black hoodies. Only seven females preferred blue hoodies. (Compare the totals at the bottom of the columns.)
   Style preference: By far the most females liked hoodies with a zip (35 out of 37). (Compare the totals on the right of the rows.)
   Possible recommendation: If the Student Council wants to order one kind of hoodie for all the females it should be black hoodies with a zip (preferred by 30 females out of 37). (Compare the cell values.)

There were 22 males who responded.
Colour preference: By far the most males (14 out of 22) preferred black hoodies. Only eight males preferred blue hoodies. (Compare the totals at the bottom of the columns.)
Style preference: By far the most males liked pullover hoodies (15 out of 22). (Compare the totals on the right of the rows.)
Possible recommendation: If the Student Council wants to order one kind of hoodie for all the males it should be blue pullover hoodies (preferred by 8 males out of 22). (Compare the cell values.)

9.2 Collecting and organising numerical data

Mathematical notes

In the previous section learners saw that different representations can make different aspects of the data more visible. The focus on what is made more visible in different representations is continued in this section but the form of representation switches from tables to graphs.
In Term 1 we mentioned that graphs provide a picture of data. This picture facilitates the analysis of the data. We can also analyse data by examining how spread out or clustered it is and what a typical value is. In this section learners continue to use the concept of mode to examine the typical value or centre of the data. They also find the middle value of the set of data points – from Grade 6 onwards they will learn that this is called the median. Learners also look at the spread of data in this section.

Much of data handling involves reasoning in uncertain situations. This can make learners feel insecure, because there tends to be much greater certainty in other areas of Mathematics: there are usually one or more definite answers. In data handling learners need to use their analysis of the data as evidence to back up an argument. This is the case in question 1(e).

The months are categories in this data set. The amounts of the accounts are numerical data. The amounts are not frequencies; they are measurements of the amount of electricity Mrs Mholo has used, to which a monetary value has been attached.

**Teaching guidelines**

Prepare the table and graphs on the board or on a poster for use during class discussions.

Most of the questions in this section require interpretation: very few are simply facts. Learners need to use the data to motivate their answers. Allow sufficient time for learners to discuss their answers. Sometimes, for example in question 2(c), the class will be able to agree on an answer. Be aware however, that learners are likely to express their answers differently. There are questions, for example question 1(e), where learners may not be able to agree on an answer.

**Answers**

1. (a) R403 in August last year  
   (b) R529 in June this year  
   (c) July, March, April, May, June: all of these accounts were higher than R450.  
   (d) Mrs Mholo can expect to use more electricity for heating in the winter months because it is colder. She can also expect to use more electricity for lighting in winter, as there are fewer daylight hours. Her accounts in winter differed by as much as R29. In summer she is likely to use less electricity for heating and lighting. Her accounts in summer did not differ by more than about R12.  
   (e) Learners’ answers may differ here. Some might say: “Yes, the account for June this year is R43 more than for July last year, and that is a big increase compared to the other increases.” Others might say: “No, she can expect to use more electricity in the winter months, and the increase between May and June this year is not even bigger than the increase between March and April this year.” We need more information to decide.
Critical knowledge

It is important that learners understand that when we analyse data we are looking for general trends. Sometimes a few data points may deviate from the overall pattern; we tend to overlook these points as we focus on the general impression. For example, in question 2(e) there has been a general increase in the amount of money that Mrs Mholo has paid since February. Learners should not be distracted by the fact that there was no increase between October and November and that what she paid in January was R4 less than what she paid in December. The overall trend is an increase. It is important that learners do not just look at the initial amount and the final amount, but at the pattern as a whole.

Answers

2. (a) No, because 10 out of the last 12 accounts were between R400 and R500.
(b) Yes, because none of the accounts of the past year have been less than R400.
(c) Not really. The last two accounts were R500 and more. Mrs Mholo thinks this is a mistake. However, her invoices have steadily increased from February this year.
(d) Yes, because none of the accounts of the past year have been more than R530.
(e) The overall trend in the bar graph shows an increase in the amount of money that Mrs Mholo paid for electricity since August last year. Since August last year her account has increased from R403 almost every month up to R529 in June this year.

3. (a) You don’t see how much she paid in which month. You don’t see whether the amounts only increased over time, only decreased over time, or increased for some months and decreased for other months.
(b) Answers will differ. Some learners may choose R412, which is the mode. Other learners may choose an amount in the middle. A suitable middle amount is R416, or R424, or even R420.
(c) R416 (The six highest accounts are all more than R416.)
(d) R486 (The three highest accounts are all more than R486.)
**Mathematical notes**

Graphs give a picture of data. Different graphs give a different picture: they reveal different parts of the story.

The bar graph shown after question 1 allows you to see that Mrs Mholo uses more electricity in the winter months. From a very careful look at the bar graph you can see that Mrs Mholo paid less than R450 for about half of the months and more than about R450 for the other half of the months.

The pictograph shows clearly that the amounts she paid are spread between just over R400 and just under R500 and that half of the payments were less than R420.

**Answers**

4. (a) The mode is R412. This is where the most dots are. (See the first arrow above.)
   (b) R420 is halfway between the sixth and the seventh value. (See the second arrow above.)

5. (a) True
   (b) Not true. Only five accounts are lower than R416. Correct the statement by saying: “lower or equal to R416”.
   (c) Not true. The lowest amount is R403, which is R9 lower.
   (d) Not true. One account was R529. That is R117 higher.
   (e) Not true. The accounts in winter are much higher.
   (f) True

6. Mrs Mholo can show a pictograph (like the one above) and argue that in summer her accounts ranged between R403 and R420, and that while her accounts went up during the winter months, it was never by more than R30 a month. The big jump from R529 to R650 – more than R120 – from June to July is likely to be a mistake.
Grade 5 Term 3 Unit 10 Numeric patterns

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<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
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<td>Diagonal sequences, i.e. patterns with an increasing difference</td>
<td>264</td>
</tr>
<tr>
<td>10.2 Patterns in tables</td>
<td>Families of sequences with a constant difference</td>
<td>265</td>
</tr>
<tr>
<td>10.3 Using patterns to solve problems</td>
<td>Equivalence between tables, rules and flow diagrams</td>
<td>266 to 268</td>
</tr>
</tbody>
</table>

**CAPS time allocation** 5 hours

**CAPS page references** 18 to 19 and 189 to 191

Continuing sequences or completing tables according to a pattern not only provides opportunities to develop understanding of patterns, but also contributes to the development of the **Mental Mathematics** section of the CAPS.

**Mathematical background**

Numeric patterns (number patterns), as part of the Content Area “Patterns, Functions and Algebra”, should serve as building blocks to develop the basic concepts of algebra in the Senior and FET phases. The study of numeric patterns should develop the concepts of **variable, relationships** and **functions**. The function concept is captured in the idea of applying a fixed rule to one set of numbers, to produce another set of numbers:

\[
\text{Input numbers} \rightarrow \text{Rule} \rightarrow \text{Output numbers}
\]

Much of our pattern work focuses on methods to find the calculation plan (rule), because a calculation plan is very useful to find missing **output numbers** and **input numbers**.

The following two important empowering approaches to pattern work should be emphasised throughout:

- **Recursive (“horizontal”) patterns** in sequences describing the relationship between any two consecutive numbers in a sequence, and then continuing the sequence, for example:

  \[
  3 \quad 6 \quad 9 \quad 12 \quad 15 \quad \ldots
  \]

- **Functional (“vertical”) patterns** describing the constant relationship between two sets of numbers, and then applying this pattern to calculate further-lying values (e.g. the 100th number), for example:

  \[
  \begin{array}{cccccc}
  \text{Position no. (Input):} & 1 & 2 & 3 & 4 & 5 & 100 \\
  \text{Sequence no. (Output):} & 3 & 6 & 9 & 12 & 15 & \ldots
  \end{array}
  \]

These two ideas (**recursive** and **functional relationships**) are important for future mathematical concepts. Recursion leads to the important mathematical concepts of the gradient of a straight line and the derivative of a function. The function concept underlies all of high school algebra and calculus.
10.1 More sequences

**Teaching guidelines**

The focus of this section is the introduction of new kinds of sequences that are different to the constant differences patterns we have studied so far. You should allow learners ample time to analyse the sequences, to describe the patterns in their own words, and to calculate numbers in the sequences.

As with the “families of sequences” in Term 1 Unit 4, learners should in question 2 notice and use the relationships between the sequences to make the work easier. For example, Sequence F, which consists of the square numbers, should be easy; the numbers in Sequence G are simply one more, and in Sequence H two more than the square numbers.

**Answers**

1. (a) \( R 4 800 \div 30 = R 160 \)
   (b) \( R 4 800 \div 15 = R 320 \)
   (c) Number of passengers | 5 | 10 | 20 | 40 | 80 | 160
   Cost for each passenger (R) | 960 | 480 | 240 | 120 | 60 | 30
   (d) Cost per passenger = Cost of hiring the bus \( \div \) number of passengers

2. A (a) Start with 1 and then double each number to get the next number.
   (b) \..., 64, 128, 256, 512, 1 024
B (a) Start with 512 and then halve each number to get the next number.
   (b) \..., 16, 8, 4, 2, 1
C (a) Start with 3 and then double each number to get the next number.
   (b) \..., 192, 384, 768, 1 536, 3 072
D (a) Start with 1 and then multiply each number by 3 to get the next number.
   (b) \..., 243, 729, 2 187, 6 561, 19 683
E (a) Start with 2 and then multiply each number by 3 to get the next number.
   (b) \..., 486, 1 458, 4 374, 13 122, 39 366
F (a) Square numbers, i.e. numbers multiplied by itself: \( 1 \times 1, 2 \times 2, 3 \times 3, \ldots \)
   (b) \..., 49, 64, 81, 100, 121
G (a) Start with 2, then +3, +5, +7, \ldots \) or: The numbers are 1 more than in Sequence F.
   (b) \..., 50, 65, 82, 101, 122
H (a) Start with 3, then +3, +5, +7, \ldots \) or: The numbers are 1 more than in Sequence G.
   (b) \..., 51, 66, 83, 102, 123

---

**UNIT 10 NUMERIC PATTERNS**

**10.1 More sequences**

1. The cost of hiring a mega bus to travel from Johannesburg to Polokwane and back is \( R 4 800 \).
   (a) If 30 people go on the trip, how much must each passenger pay if they share the cost equally?
   (b) If 15 people go on the trip, how much must each passenger pay if they share the cost equally?
   (c) Complete the table:
   (d) Write a calculation plan to show how to calculate the cost for each passenger for any number of passengers travelling on the bus.

2. For each of Sequences A to H:
   (a) Describe the patterns in your own words.
   (b) Continue the pattern for five more numbers.

Sequence A: \( 1, 2, 4, 8, 16, 32, \ldots \)
Sequence B: \( 512, 256, 128, 64, 32, \ldots \)
Sequence C: \( 3, 6, 12, 24, 48, 96, \ldots \)
Sequence D: \( 1, 3, 9, 27, 81, \ldots \)
Sequence E: \( 2, 6, 18, 54, 162, \ldots \)
Sequence F: \( 1, 4, 9, 16, 25, 36, \ldots \)
Sequence G: \( 2, 5, 10, 17, 26, 37, \ldots \)
Sequence H: \( 3, 6, 11, 18, 27, 38, \ldots \)
10.2 Patterns in tables

Teaching guidelines

These activities are very dependent on your discussing with learners appropriate thinking to analyse the given information, and to make sure they adequately engage with the problems so that they can reason about the situations.

For example, the task in question 1 is not to complete the table for the sake of completing the table, but for learners to interpret the information they generate in the table in order to answer the question: Which company is cheaper?

Notes on questions

Question 1 requires that learners will analyse the relationship between the two cost sequences by comparing the corresponding values. They will find that for 200 km the cost is the same, for less than 200 km AfriCars is cheaper and for more than 200 km Image Car Rental is cheaper.

To find the cost in the table for travelling a certain distance, learners must implement the formulation in words as a calculation rule for each company:

- **Cost for Image Car Rental** = \(2 \times \text{Distance travelled} + 180\)
- **Cost for AfriCars** = \(2,50 \times \text{Distance travelled} + 80\)

Question 2 is an example of a **decreasing** sequence, where we subtract to find the next number.

Learners can solve the problem by continuing the sequence 60, 56, 52, ... until they reach zero (the tank is empty). However, this will be cumbersome. It is important that learners realise this and understand that they should try to find a shorter, more efficient method. It will be better to reason it out:

From the table you can see that the car uses 4 ℓ of petrol to drive 40 km.

So with 1 ℓ it drives 10 km, so with 60 ℓ (a full tank) it drives \(60 \times 10 \text{ km} = 600 \text{ km}\).

**Answers**

1. (a)  
<table>
<thead>
<tr>
<th>Distance (km)</th>
<th>0</th>
<th>50</th>
<th>100</th>
<th>150</th>
<th>200</th>
<th>250</th>
<th>300</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cost: Image (R)</td>
<td>180</td>
<td>280</td>
<td>380</td>
<td>480</td>
<td><strong>580</strong></td>
<td>680</td>
<td>780</td>
</tr>
<tr>
<td>Cost: AfriCars (R)</td>
<td>80</td>
<td>205</td>
<td>330</td>
<td>455</td>
<td><strong>580</strong></td>
<td>705</td>
<td>830</td>
</tr>
</tbody>
</table>

(b) It depends on the distance he wants to travel. For less than 200 km AfriCars is cheaper. For 200 km they cost the same. For more than 200 km Image Car Rental is cheaper.

2. 600 km
# 10.3 Using patterns to solve problems

## Notes on questions
Learners have met the party tables before in the unit on geometric patterns in Term 2.

To calculate the number of people for a large number of tables will be cumbersome if we use the horizontal +2 pattern. It will be more useful to find a calculation plan. We again outline the thinking required to see the structure in the picture (from page 179 of the Learner Book) that enables us to formulate a calculation plan.

The way to “see” structure is to understand that in Figure 4 we try to see a unit of 4, in Figure 3 a unit of 3 in the same way, in Figure 2 a unit of 2, etc. as illustrated below:

1 table

2 tables

3 tables

4 tables

The challenge is then to generalise the structure so that we can easily calculate how many people will sit at 45 small tables:

\[
\begin{align*}
T_1 &= 2 \times 1 + 2 \\
T_2 &= 2 \times 2 + 2 \\
T_3 &= 2 \times 3 + 2 \\
T_4 &= 2 \times 4 + 2 \\
T_{45} &= 2 \times 45 + 2 \\
\end{align*}
\]

So \( T_{45} = 2 \times 45 + 2 \)

\[
\text{No. of people} = (2 \times \text{No. of tables}) + 2
\]

## Answers
1. (a) Complete this table to show how the number of people changes as the number of tables changes.

<table>
<thead>
<tr>
<th>No. of tables</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>15</th>
<th>20</th>
<th>45</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of people</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>10</td>
<td>12</td>
<td>14</td>
<td>16</td>
<td>32</td>
<td>42</td>
<td>92</td>
</tr>
</tbody>
</table>

(b) Learners’ answers may differ.

(c) Learners discuss their patterns.

2. (a) A \( \rightarrow [x - 2] - [x + 2] \rightarrow \)

B \( \rightarrow [x - 1] - [x + 2] \rightarrow \)

(b) Both flow diagrams are correct.
Notes on questions

Questions 2 and 3 focus on two equivalent descriptions for the number of tables, represented in the form of flow diagrams, tables and calculation plans.

We illustrate below how to “see” a different structure from that in question 1:

\[ \begin{align*}
\text{1 table} & \quad 2 \times (1 + 1) \\
\text{2 tables} & \quad 2 \times (2 + 1) \\
\text{3 tables} & \quad 2 \times (3 + 1) \\
\text{4 tables} & \quad 2 \times (4 + 1)
\end{align*} \]

The challenge is then to generalise the structure so that we can easily calculate how many people will sit at 45 small tables:

\[ \begin{align*}
T_1 &= 2 \times (1 + 1) \\
T_2 &= 2 \times (2 + 1) \\
T_3 &= 2 \times (3 + 1) \\
T_4 &= 2 \times (4 + 1)
\end{align*} \]

\[ T_{45} = 2 \times (45 + 1) \]

No. of people = \( 2 \times (\text{No. of tables} + 1) \)

You should emphasise that equivalent calculation plans are different methods that give the same answers. We can see it in the pictures, in the flow diagrams and in the tables. We should also see it in the numerical expressions. For example, we can write the number sentence:

\[ 2 \times (45 + 1) = 2 \times 45 + 2 \]

We can show that both calculation plans give the same answer (92), but we should also know that these two calculation plans are equivalent because of the distributive property of multiplication over addition.

Answers

3. \[ \begin{array}{cccccccccc}
\text{No. of tables} & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 15 & 20 & 45 \\
2 \times \text{No. of tables} + 2 & 4 & 6 & 8 & 10 & 12 & 14 & 16 & 32 & 42 & 92 \\
2 \times (\text{No. of tables} + 1) & 4 & 6 & 8 & 10 & 12 & 14 & 16 & 32 & 42 & 92 \\
\end{array} \]

They are both correct.
**Mathematical notes**

Writing the inverse of a flow diagram is very important because it provides the most efficient method to find unknown input numbers, i.e. to solve equations.

Inversing a flow diagram involves inverse operations in reverse order, for example:

Flow diagram:  
\[ ? - \times 2 + 2 \rightarrow 48 \]

Inverse flow diagram:  
\[ 23 \leftarrow \div 2 - 2 - 48 \]

This describes exactly the procedure to formally solve the equation \(2x + 2 = 48\):

\[
2x + 2 = 48 \\
x = (48 - 2) \div 2
\]

This is exactly what the first inverse flow diagram in question 4 shows.

The second inverse flow diagram shows the solution of the equation \(2(x + 1) = 48\):

\[
x = 48 \div 2 - 1
\]

**Teaching guidelines**

Do not let learners rewrite the flow diagrams. Question 4(a) only asks them to specify the operators for the inverse flow diagrams.

**Answers**

4. (a)  
\[ -\times 2 + 2 \rightarrow \text{and} \]
\[ +2 -1 \rightarrow \]

(b)  
\[ 48 -\times 2 \rightarrow 23 \text{ or} \]
\[ 48 +2 -1 \rightarrow 23 \]

In questions 2 and 3 Anand calculated the number of people as output number. It will be easier to have a flow diagram with the known number of people as input number to calculate the unknown number of tables needed.

4. Below are the two flow diagrams that you used in question 2.

(a) Change the operators so that the number of people is the input number.

(b) Then calculate the number of tables needed if Anand knows there will be 48 people at the party (including himself).
Grade 5 Term 3 Unit 11       Whole numbers: Multiplication

<table>
<thead>
<tr>
<th>Sections in this unit</th>
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<td>Use factors to multiply Multiplication by factorising one of the numbers</td>
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<tr>
<td>11.4</td>
<td>Multiplication practice Practising multiplication of 2-digit numbers by 3-digit numbers</td>
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<tr>
<td>11.6</td>
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<td>278 to 279</td>
</tr>
</tbody>
</table>

**CAPS time allocation** 7 hours

**CAPS page references** 13 to 15 and 192 to 193

**Mathematical background**

The key to effective multiplication of whole-digit numbers is to replace the given product, for example $42 \times 54$, with a number of smaller products for which the answers are known (remembered) or can be found easily.

Because multiplication distributes over addition, $42 \times 54$ can be replaced with $42 \times 50 + 42 \times 4$, and this can be replaced with $40 \times 50 + 2 \times 50 + 40 \times 4 + 2 \times 4$.

A person who knows the facts $4 \times 5 = 20$, $2 \times 5 = 10$, $4 \times 4 = 16$ and $2 \times 4 = 8$ can with some skill easily form the facts $40 \times 50 = 2000$, $2 \times 50 = 100$, $40 \times 4 = 160$ and $2 \times 4 = 8$ that are required to execute the calculation plan $40 \times 50 + 2 \times 50 + 40 \times 4 + 2 \times 4$:

$2000 + 100 + 160 + 8 = 2268$.

In the above calculation, the factors 42 and 54 of the original product $42 \times 54$ were broken down into the sums $40 + 2$ and $50 + 4$, and the *product of sums* $(40 + 2) \times (50 + 4)$ was then replaced by the *sum of products* $(40 \times 50) + (2 \times 50) + (40 \times 4) + (2 \times 4)$.

Alternatively, one of the numbers of the original product can be factorised, while the other number is written as a sum, as in the above. For example:

$42 \times 54 = 2 \times 3 \times 7 \times (50 + 4)$

The calculation can then proceed as shown on the right.

$2 \times 3 \times 7 \times (50 + 4)$

$= 2 \times 3 \times 378$ because $7 \times 50 + 7 \times 4 = 378$

$= 2 \times 1134$ because $3 \times 300 + 3 \times 70 + 3 \times 8 = 1134$

$= 2268$
11.1 Count, add, multiply and divide

Teaching guidelines
The extent to which learners spontaneously utilise the mathematics they have learnt is an important indication of the quality of their mathematical knowledge.

In this respect it may be quite informative to begin the work in this section by starting with question 3, i.e. asking learners to find out how many bananas are shown in Picture B on page 272 of the Learner Book. Let them describe how they did it on a loose sheet of paper that you take in to analyse. Here are some of the ways in which learners may do it:

- Counting the bananas one by one
- Counting the bananas in eights: 8 16 24 32 . . . . . . . . . . . . . 560
- Counting the bunches and calculating: 70 \times 8
- Counting or calculating the number of bananas in one row and multiplying this by 10, for example 56 \times 10 or 7 \times 8 \times 10. Alternatively, learners may work with the columns, for example 7 columns of 80 bananas each.

Learners who use the first or second strategy mentioned above clearly do not have a strong sense of how multiplication relates to real situations. Such learners may benefit substantially from the work in this section.

Mathematical notes
This section provides learners with opportunities to deepen their understanding of the meaning of multiplication as repeated addition and counting in groups. At the same time the questions provide concrete experiences of numbers as the products of several factors.

Notes on questions
Question 1 is intended to guide learners towards observing the structure of the three pictures of bunches of bananas.

Answers
1. (a) Learners write down their plans for finding the answer.
   (b) Learners write down their plans for a quicker way to find the answer.
2. (a) Learners write down their plans to find the answer.
   (b) Learners write down their plans for a quicker way to find the answer.
3. (a) 560 bananas
   (b) Learners’ answers may differ.
Teaching guidelines
When learners have completed questions 1 to 3, you may explain various strategies as described in the tinted passage on pages 269 to 270 of the Learner Book, with reference to Picture C on page 273.

It is important that learners try to do question 6 without drawing a picture. Questions 6 and 7 are intended to lift learners’ engagement to a higher level of abstraction.

Note that questions 9 and 10 require division. Question 9 requires learners to determine the size of each share if 640 is divided into 80 equal shares. Question 10 is a grouping question: it requires learners to determine how many groups there are if 720 is divided into groups (bunches) of 6 each.

Answers
4. 630 bananas
5. 140 bananas
6. 400 bananas
7. (a) 480 bananas (b) 480 bananas (c) 480 bananas
8. Learners’ own descriptions
9. 8 bananas
10. 120 bunches
Additional material
You may use copies of the diagrams below for additional activities of the same kind.

---

Picture A

---
Mathematical notes

Multiplication is applicable to a wide variety of different kinds of situations, including those described below:

- Repetition of the same amount/number, for example in the question: “How many apples are there in 23 boxes with 72 apples each?”
- A rectangular array, for example Picture B on the right
- A total based on a rate, for example the cost of 58 ℓ of petrol at R12 per litre
- A ratio (scale) situation, for example when a house is 50 times as big as the building plan.
11.2 Factors and multiples

**Teaching guidelines**
Ask learners to do question 1 and to write down, for each colour, how they calculated the total. Take feedback when learners have finished and write some of the learners’ calculation plans on the board. Some of the plans that learners may have used are:

\[ 4 \times 3 \times 5 \quad 6 \times 2 \times 5 \quad 3 \times 4 \times 5 \]

Let learners then do question 2. Ask them to comment on the connection between questions 1 and 2.

**Answers**

1. Blue: 60; red: 60; yellow: 60
2. \[ 2 \times 3 \times 10; \quad 2 \times 5 \times 6 \]
3. (a) For example: \( 3 \times 4 \times 10; \quad 2 \times 5 \times 12 \)
   (b) For example: \( 2 \times 3 \times 4 \times 5; \quad 2 \times 2 \times 5 \times 6 \)
   (c) For example: \( 1 \times 2 \times 3 \times 4 \times 5; \quad 2 \times 2 \times 2 \times 3 \times 5 \)
   (d) \( 1; 2; 3; 4; 5; 6; 8; 10; 12; 15; 20; 24; 30; 40; 60; 120 \)
4. (a) 1 row of 30 plants; 2 rows of 15 plants; 3 rows of 10 plants
   (b) \( 1 \times 30; \quad 2 \times 15; \quad 3 \times 10; \quad 5 \times 6 \)
5. (a) 1 row of 24 plants \quad 2 rows of 12 plants
   3 rows of 8 plants \quad 4 rows of 6 plants
   6 rows of 4 plants \quad 8 rows of 3 plants
   12 rows of 2 plants \quad 24 rows of 1 plant
   (b) \( 1; 2; 3; 4; 6; 8; 12; 24 \)
   (c) \( 1 \times 24; \quad 2 \times 12; \quad 3 \times 8; \quad 4 \times 6 \)
   (d) \( 2 \times 3 \times 4 \)
   (e) \( 2 \times 2 \times 2 \times 3 \)

**Additional questions**
Question 3 may be extended by asking learners to find all the different ways in which 120 (or some other numbers) can be expressed as a product of two factors, a product of three factors, and so on. You may also ask learners whether 120 can be expressed as a product of six factors that do not include 1.
Teaching guidelines
The method described in the tinted passage involves considering each of the numbers 1, 2, 3, 4, 5, etc. as a possible factor of 24. If a number is a factor of 24, its “partner” is also written down. The method is demonstrated below for finding the factors of 20, using number sentences as an alternative and more complete way of recording the same thinking.

Consider all whole numbers up to half of the “target” number as possible factors:

\begin{align*}
1 \times \ldots &= 20 \\
2 \times \ldots &= 20 \\
3 \times \ldots &= 20 \\
4 \times \ldots &= 20 \\
5 \times \ldots &= 20 \\
6 \times \ldots &= 20 \\
7 \times \ldots &= 20 \\
8 \times \ldots &= 20 \\
9 \times \ldots &= 20 \\
10 \times \ldots &= 20
\end{align*}

Solve the number sentences with numbers that are factors of 20 and cross out the others:

\begin{align*}
1 \times 20 &= 20 \\
2 \times 10 &= 20 \\
3 \times \ldots &= 20 \\
4 \times 5 &= 20 \\
5 \times 4 &= 20 \\
6 \times \ldots &= 20 \\
7 \times \ldots &= 20 \\
8 \times \ldots &= 20 \\
9 \times \ldots &= 20 \\
10 \times 2 &= 20
\end{align*}

Answers

6. \[1 2 3 4 6 9 12 18 36\]

The factor 6 does not have a partner because 6 is multiplied by itself to give 36.

7. 1 row of 36 plants, 2 rows of 18 plants, 3 rows of 12 plants, 4 rows of 9 plants, 6 rows of 6 plants, 9 rows of 4 plants, 12 rows of 3 plants, 18 rows of 2 plants, 36 rows of 1 plant

8. Yes

9. The answer is the same as the number you multiplied 1 by.

10. When a number is multiplied by 1, the value of that number does not change.
**Answers**

11. (a) 20; 25; 30; 35; 40
   (b) 48; 60; 72; 84; 96
   (c) 36; 45; 54; 63; 72
12. 15; 30; 45; 60; 75
13. Yes; 12 is a multiple of 6 and because 6 is a factor of 12, 6 will divide into any multiple of 12 without a remainder.
14. (a) Yes, 1 001 ÷ 13 = 77
   (b) You can write down all the multiples of 13 up to just over 1 000, but that is a tedious method. Rather use repeated subtraction in a clever way:

   \[
   \begin{align*}
   13 \times 100 & \rightarrow 1 300 \\
   \text{halve } 1 300 & \rightarrow 650 = 13 \times 50 \\
   1 001 - 650 & = 351 \\
   13 \times 10 & \rightarrow 130 \\
   \text{double } 130 & \rightarrow 260 = 13 \times 20 \\
   351 - 260 & = 91 \\
   \text{halve } 130 & \rightarrow 65 = 13 \times 5 \\
   91 - 65 & = 26 = 13 \times 2
   \end{align*}
   \]

11.3 Use factors to multiply

**Teaching guidelines**

Demonstrate on the board that if one of the two numbers in a product can be factorised into 1-digit factors, this provides an easy alternative way to evaluate a product.

Example: \(150 \times 72 = 3 \times 5 \times 10 \times 72 = 3 \times 72 \times 5 \times 10\)

\[
= 216 \times 5 \times 10 \\
= 1 080 \times 10 \\
= 10 800
\]

**Answers**

1. (a) 1 820  (b) 1 820  (c) 1 820
   (d) Learners’ opinions may differ.

2. (a) For example: \(2 \times 5 \times 3 \times 17\)  (b) For example: \(3 \times 7 \times 53 \times 2\)
Answers
3. Learners break up one of the numbers when calculating.
   The answers are:
   (a) 2 226  (b) 6 336
   (c) 24 255  (d) 15 972

11.4 Multiplication practice

Answers
1. (a) 3 445  (b) 3 710
   (c) 8 432  (d) 8 432
   (e) 16 864  (f) 9 102
2. (a) 8 328  (b) 14 754
   (c) 21 306  (d) 10 854
   (e) 11 407  (f) 10 736

11.5 Multiplication in real life

Answers
1. 29 638 learners
2. 1 456 km
3. R3 672
4. 5 916 television sets
5. 1 311 oranges

3. Do the following multiplications by breaking up one of the numbers into factors.
   (a) 42 \times 53  (b) 48 \times 132
   (c) 105 \times 231  (d) 242 \times 66

11.4 Multiplication practice

Calculate.
1. (a) 265 \times 13  (b) 14 \times 265
   (c) 248 \times 34  (d) 68 \times 124
   (e) 248 \times 68  (f) 246 \times 37
2. (a) 347 \times 24  (b) 42 \times 347
   (c) 402 \times 53  (d) 54 \times 201
   (e) 671 \times 17  (f) 16 \times 671

11.5 Multiplication in real life

1. A local bus can carry 73 learners to school every day. This bus does 406 trips every year. How many learners can it carry on this route in one year?
2. It takes Fred 13 hours to drive to his parents’ farm. If he travels approximately 112 km every hour, how far does he travel?
3. Steve needs 24 m of fencing to make a camp for his goats. The fencing material that he uses costs R153 per metre. How much will the fencing material cost him?
4. A hotel group has 17 lodges throughout the country. Each lodge has 348 rooms. The managers of the hotel group want to put a new television set in each room. How many television sets do they have to order?
5. A farm stall owner sells oranges. He puts 23 oranges in a pocket. If he fills exactly 57 pockets, how many oranges did he buy from the orange farmer?
Notes on questions

Question 6 is specifically designed to challenge learners to read the problem statement carefully, and not to indiscriminately decide to do a certain operation on certain numbers.

Question 9 is demanding. It helps to work out the number of tins: 6 dozen is $6 \times 12 = 72$.

One way to work out the total cost is to think of 72 as four groups of 18 tins: you only have to pay for three of the groups, so the cost is $3 \times 18 \times 6,15$.

Another way to work out the total cost is to argue that you will pay $3 \times 6,15 = R18,45$ for every 4 tins (because when you buy 4 tins you only pay for 3 tins at R6,15 each). One dozen is 3 groups of 4 tins, so 6 dozen is $6 \times 3 = 18$ groups of 4 tins. So the total cost is $18 \times R18,45$.

Note that question 10 asks for estimates only. Three pods will be about 126 beans, which is close to what is needed for 1 kg of chocolate. So 14 kg of chocolate requires about $14 \times 3 = 42$ cacao pods.

Answers

6. (a) $(20 + 8) \times 12 \times 30$ (b) 10 080 eggs
7. R29 376
8. 5 880 trays
9. R332,10
10. About 42 cacao pods

11.6 More calculations in real life

Teaching guidelines

Warn learners that the questions in this section are tricky and require careful reading. Many of the questions require more than one step.

Notes on questions

Question 1:
Shop B has $18 \times 53 = 954$ glass jars. The two shops together have $954 + 53 = 1 007$ glass jars.

Question 3: You may have to help learners to understand the context.
There are $62 \times 28 = 1 736$ seats in total. Hence $1 736 - 690 = 1 046$ tickets were sold before Saturday night.

Answers

1. 1 007 glass jars
2. R2
3. 1 046 tickets

6. (a) Farmer Tavuk forgot to record how many eggs he sent to the supermarket, but he remembers that 28 crates were loaded into the truck. Each of the 28 crates contained 12 trays, and each tray had 30 eggs.

Which of the following calculations will help Farmer Tavuk to record the correct number of eggs?

$\frac{(28 + 12) \times 30}{(28 \times 30) + 12}$

$\frac{(20 + 8) \times 12 \times 30}{(12 \times 30) + 28}$

(b) How many eggs did he send to the supermarket?

7. The Trano Café sold 432 lunches on Saturday at R68 each. How much money did the café make on Saturday?

8. A nursery has a contract to deliver 168 trays of herb seedlings to a garden centre every week. How many trays will the nursery deliver over a period of 35 weeks?

9. A local supermarket has a special on tins of baked beans. If you buy four tins, you only have to pay for three tins. The price of one tin of baked beans is R6,15. Mr Fourie put 6 dozen tins in his shopping trolley. How much did he pay?

10. There are about 42 beans in one cacao pod. About 123 cacao pods are needed to make 1 kg of chocolate. About how many pods are needed for 14 kg of chocolate?
Teaching guidelines
The situations in questions 4, 5, 6 and 8 are complicated in the sense that they all require more than one operation. Suggest to learners that they read each question carefully and write a calculation plan before they start to do the calculations. Also suggest to them that they do not start calculating immediately when they have written a calculation plan, but first think critically about the plan they have written and check whether it corresponds to the situation described in the question.

Notes on questions
Calculation plans for the different questions are given below.

Question 4: \[ 16 \times 8 \times 3 + 17 \times 7 \times 3 \]
16 (round tables) \times 8 (places) \times 3 (glasses) + 17 (rectangular tables) \times 7 (places) \times 3 (glasses)

Question 5: \[ 124 \times 37 + 192 \times 67 \]

Question 6: \[ 5 \times 28 + 4 \times 24 + 3 \times 25 \]

Question 7(a): \[ 47 \times 18 \]

Question 8: \[ 18 \times 149 - 13 \times 165 \]

Answers
4. \[ 3 \times (16 \times 8 + 17 \times 7) = 741 \text{ glasses} \]
5. R17 452
6. 311 learners
7. (a) 846 T-shirts (b) 9 boxes
8. R537

4. Waiters are setting tables for a dinner function. Sixteen round tables are set with 8 places each and 17 rectangular tables are set with 7 places each. At each of the places, 3 glasses are arranged. How many glasses are put on the tables altogether?

5. Wilhelmina and her daughters knit scarfs and caps for an income. They sell the caps for R124 each and the scarfs for R192 each. They have an order for 37 caps and 67 scarfs. How much is their income from this order?

6. When the National Cycling Championship took place and the cyclists passed Star Primary School, 12 classes went outside to watch. Five classes of 28 learners each, four classes of 24 learners each and three classes of 25 learners each cheered the cyclists on. Altogether, how many learners were outside?

7. Bike Bonanza sponsors T-shirts for first-time entries in the cross-country cycling race. Last year there were 47 cyclists who took part in the race for the first time. This year 18 times more newcomers entered than last year.

(a) How many T-shirts must Bike Bonanza have ready on the day of the race?

(b) The T-shirt company only sells boxes of 100 T-shirts each. How many boxes must Bike Bonanza order?

8. Mrs Singh bought 18 books at a book sale. She paid R149 for each book. She later sold 13 of the books to a secondhand bookshop for R165 each. What is the difference between the total amount of money she bought the books for and the total amount of money she sold the books for?
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**CAPS time allocation**
1 hour

**CAPS page references**
13 to 15 and 196

**Mathematical background**

Any even number can be written in the form \(2n\), where \(n\) is a natural number, and any number that can be written in the form \(2n\) is an even number.

Any odd number can be written in the form \(2n + 1\), where \(n\) is a natural number, and any number that can be written in the form \(2n + 1\) is an odd number.

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<tr>
<td>The sum of any two even numbers, (2m) and (2n), is an even number because (2m + 2n = 2(m + n))</td>
<td>These examples use (m = 15) and (n = 8), but any other whole numbers could have been used for (m) and (n).</td>
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<tr>
<td>The sum of any two odd numbers, (2m + 1) and (2n + 1), is an even number because (2m + 1 + 2n + 1 = 2m + 2n + 2 = 2(m + n + 1))</td>
<td>(2 \times 15 + 1 + 2 \times 8 + 1 = 2 \times (15 + 8) + 1) = (2 \times (15 + 8 + 1)), an even number</td>
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<tr>
<td>The sum of any odd number, (2m + 1), and any even number, (2n), is an odd number because (2m + 1 + 2n = 2m + 2n + 1 = 2(m + n) + 1)</td>
<td>(2 \times 15 + 1 + 2 \times 8 = 2 \times (15 + 8) + 1) = (2 \times (15 + 8 + 1)), an odd number</td>
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<td>The difference between any two even numbers, (2m) and (2n), is an even number because (2m - 2n = 2(m - n))</td>
<td>(2 \times 15 - 2 \times 8 = 2 \times (15 - 8)) = (2 \times (15 - 8)), an even number</td>
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<td>The difference between any two odd numbers, (2m + 1) and (2n + 1), is an even number because (2m + 1 - (2n + 1) = 2m + 1 - 2n - 1 = 2m - 2n = 2(m - n))</td>
<td>(2 \times 15 + 1 - (2 \times 8 + 1) = 2 \times 15 + 1 - 2 \times 8 - 1) = (2 \times 15 - 2 \times 8) = (2 \times (15 - 8)), an even number</td>
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An algebraic treatment of even and odd numbers, like the above, is not required in Grade 5. *The above is given for your benefit only.*

In Section 1.2 learners will engage with the above properties of even and odd numbers by means of examples.
1.1 Order and represent numbers

**Teaching guidelines**
Questions 1 to 6 may be utilised as a **diagnostic assessment** instrument.

**Answers**

1. 120 000 120 400 120 800 121 200 121 600 122 000 122 400 122 800 123 200

2. 222 000 224 000 226 000 228 000 230 000 232 000 234 000 236 000 238 000 240 000 242 000 244 000

3. | 120 000 | 160 000 | 200 000 | 240 000 | 280 000 |
   | 320 000 | 360 000 | 400 000 | 440 000 | 480 000 |
   | 520 000 | 560 000 | 600 000 | 640 000 | 680 000 |
   | 720 000 | 760 000 | 800 000 | 840 000 | 880 000 |
   | 920 000 | 960 000 | 1 000 000 | 1 040 000 | 1 080 000 |

4. 101 000 104 000 107 000 110 000 113 000 116 000 119 000

5. 195 123 201 065 298 829 439 365 477 677 686 132 786 987

6. 903 546 865 199 865 153 831 001 721 122 258 121 127 140
Teaching guidelines

Question 7 is of a different nature than the other questions in this section. It is meant to provide learners with some opportunities to think smartly.

Question 7(a) can be done by writing all the numbers from 1 to 1 000 and counting how many of them are odd. Learners could be challenged to think of a smarter way of finding the number of odd numbers. Learners who do not make progress can be supported by asking them how many numbers in total there are from 1 to 1 000. Some learners may be unsure about this. Ask them how many numbers there are from 1 to 10. They may think that it may be 10, but they may be unsure. In this case they can quickly check by writing the numbers down and counting them:

1 2 3 4 5 6 7 8 9 10

At this point, ask these learners how many numbers they think there are from 1 to 20. They may be more confident now that it is 20. Now ask them how many odd numbers there are between 1 and 10, and between 1 and 20. This may put their minds on a path towards answering question 7(a) with confidence.

Answers

7. (a) 500   (b) 999 (excluding 10 000)
   (c) 499 999 (excluding 1)   (d) 99 999 (excluding 1 000 000)
   (e) 333 333

8. (a) 100 000 + 20 000 + 4 000 + 500 + 60 + 5   124 565
   (b) 200 000 + 10 000 + 700 + 60 + 3   210 763
   (c) 400 000 + 1 000 + 800 + 7   401 807
   (d) 700 000 + 10 000 + 1 000 + 300 + 10 + 2   711 312
   (e) 100 000 + 20 000 + 7 000 + 700 + 90 + 5   127 795
   (f) 900 000 + 90 000 + 6 000 + 600 + 6   996 606

9. and 10. See next page.

7. (a) How many whole numbers between 0 and 1 000 are odd?
   (b) How many whole numbers between 0 and 10 000 are multiples of 10?
   (c) How many whole numbers between 1 and 1 million are odd?
   (d) How many whole numbers between 1 and 1 million are multiples of 10?
   (e) How many whole numbers between 1 and 1 million are multiples of 3?

8. Write the expanded notations and number symbols for these numbers.
   (a) hundred and twenty-four thousand, five hundred and sixty-five
   (b) two hundred and ten thousand, seven hundred and sixty-three
   (c) four hundred and one thousand, eight hundred and seven
   (d) seven hundred and eleven thousand, three hundred and twelve
   (e) one hundred and twenty-seven thousand, seven hundred and ninety-five
   (f) nine hundred and ninety-six thousand, six hundred and six

9. Write the expanded notations and number names for these numbers.
   (a) 216 786   (b) 785 092   (c) 670 548
   (d) 108 805   (e) 632 104   (f) 405 696

10. Round off each of the numbers in question 9 to the nearest:
   (a) five
   (b) ten
   (c) hundred
   (d) thousand.
Answers (continued)

9. (a) 200 000 + 10 000 + 6 000 + 700 + 80 + 6
   two hundred and sixteen thousand seven hundred and eighty-six
(b) 700 000 + 80 000 + 5 000 + 90 + 2
   seven hundred and eighty-five thousand and ninety-two
(c) 600 000 + 70 000 + 500 + 40 + 8
   six hundred and seventy thousand five hundred and forty-eight
(d) 100 000 + 8 000 + 800 + 5
   one hundred and eight thousand eight hundred and five
(e) 600 000 + 30 000 + 2 000 + 100 + 4
   six hundred and thirty-two thousand one hundred and four
(f) 400 000 + 5 000 + 600 + 90 + 6
   four hundred and five thousand six hundred and ninety-six

10. Rounded off to the nearest...

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<td>five</td>
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<td>216 786</td>
<td>216 785</td>
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<td>(f)</td>
<td>405 696</td>
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</table>

7. (a) How many whole numbers between 0 and 1 000 are odd?
   (b) How many whole numbers between 0 and 10 000 are multiples of 10?
   (c) How many whole numbers between 1 and 1 million are odd?
   (d) How many whole numbers between 1 and 1 million are multiples of 10?
   (e) How many whole numbers between 1 and 1 million are multiples of 3?

8. Write the expanded notations and number symbols for these numbers.
   (a) hundred and twenty-four thousand, five hundred and sixty-five
   (b) two hundred and ten thousand, seven hundred and sixty-three
   (c) four hundred and one thousand, eight hundred and seven
   (d) seven hundred and eleven thousand, three hundred and twelve
   (e) one hundred and twenty-seven thousand, seven hundred and ninety-five
   (f) nine hundred and ninety-six thousand, six hundred and six

9. Write the expanded notations and number names for these numbers.
   (a) 216 786 (b) 785 092 (c) 670 548
   (d) 108 805 (e) 632 104 (f) 405 696

10. Round off each of the numbers in question 9 to the nearest:
    (a) five
    (b) ten
    (c) hundred
    (d) thousand.
1.2 Investigate even and odd numbers

**Teaching guidelines**

As an introduction you may ask learners to mention some even numbers and some odd numbers, and write them in separate places on the board. Then say to learners that you have a number in mind and will write it on the board later. Ask them to identify a question that they could ask you that will enable them to determine whether the number you have in mind is an odd number or an even number. Allow learners to discuss this in small groups and agree on a question to ask. Visit the groups and ask each group to tell you the question they have decided on. This will provide insight into your learners' understanding of the difference between odd and even numbers.

Explain the following two methods to decide whether a number is odd or even, as well as any other correct strategies mentioned by learners:

- Look at the last digit: if the last digit is 0; 2; 4; 6 or 8, the number is even. If the last digit is 1; 3; 5; 7 or 9, the number is odd.
- Ask whether the number is the double of another number: if it is, it is even; if it is not, it is odd.

To further develop learners' understanding of even and odd numbers, you may write a set of consecutive whole numbers on the board, for example:

```
15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34
```

Then double each number:

```
30 32 34 36 38 40 42 44 46 48 50 52 54 56 58 60 62 64 66 68
```

Then add 1 to each number:

```
31 33 35 37 39 41 43 45 47 49 51 53 55 57 59 61 63 65 67 69
```

If there is time, ask learners to explain why each of the true statements in questions 3 and 4 is true. For question 3 they may argue that an odd number is an even number plus one, hence an odd number + an odd number = an even number + 1 + another even number + 1 = sum of two even numbers + 2. They may then argue that the sum of two even numbers is an even number.

**Answers**

1. Any whole number is either odd or even. No number can be both odd and even.
2. (a) 94 156 722 (b) 95 157 723
3. Yes; any five examples in which two odd numbers are added, e.g. 9 + 11 = 20
4. (a) True; e.g. 5 + 4 = 9 (b) False; e.g. 13 + 1 + 3 = 17
   (c) True; e.g. 1 + 3 = 4; 13 + 15 + 17 + 19 = 64
   (d) True; e.g. 3 + 7 + 9 = 19; 1 + 17 + 33 + 5 + 11 = 67
   (e) False; e.g. 45 − 13 = 32 (f) True; e.g. 44 − 12 = 32

---

**1.2 Investigate even and odd numbers**

An **even number** is formed when any whole number is doubled (multiplied by 2), for example:

\[ 2 \times 37 = 74, 2 \times 459 = 918 \text{ and } 2 \times 344,924 = 689,848 \]

74 and 918 and 689,848 are all even numbers.

The **units part** of any even number is 0, 2, 4, 6 or 8.

An **odd number** is formed by adding 1 to an even number, for example:

\[ 74 + 1 = 75, 918 + 1 = 919 \text{ and } 689,848 + 1 = 689,849 \]

75 and 919 and 689,849 are all odd numbers.

The **units part** of any odd number is 1, 3, 5, 7 or 9.

1. Can you think of a number that is not odd, and also not even?
2. (a) In each case, form an even number by doubling.
   47 78 361
   (b) Add 1 to each of your even numbers to form an odd number.
3. Is it true that when two odd numbers are added, the result is always an even number? Give five examples to support your answer.
4. Decide whether the statement is true or false. Give one example if the statement is false and five examples if the statement is true.
   (a) When an odd number and an even number are added, the result is always an odd number.
   (b) When any three odd numbers are added, the result is an even number.
   (c) When any even number of odd numbers are added, the result is an even number.
   (d) When any odd number of odd numbers are added, the result is an odd number.
   (e) The difference between two odd numbers is an odd number.
   (f) The difference between two even numbers is an even number.
Grade 5 Term 4 Unit 2 Whole numbers: Addition and subtraction

<table>
<thead>
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<th>Content</th>
<th>Pages in Learner Book</th>
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</thead>
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<td>Revision and practice of subskills for addition and subtraction</td>
<td>286 to 288</td>
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<tr>
<td>2.2 Add and subtract in context</td>
<td>Solving word problems</td>
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<tr>
<td>2.3 Rounding off in context</td>
<td>An investigation that involves estimation, rounding off and calculation</td>
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</table>

**CAPS time allocation**

- 5 hours

**CAPS page references**

- 13 to 15 and 197

**Mathematical background**

When adding and subtracting multi-digit numbers by breaking down and building up, it is often necessary to replace the place value expansion of a number with a different expansion or to replace an expansion with the standard place value expansion. For example:

- When calculating $8253 - 3768$, the place value expansion $8000 + 200 + 50 + 3$ of $8253$ is inconvenient because it is problematic to subtract $8$ from $3$, $60$ from $50$ and $700$ from $200$. Hence it is useful to replace $8000 + 200 + 50 + 3$ with $7000 + 1100 + 140 + 13$.
- During the calculation of $5687 + 8865$ by breaking down and building up, the expansion $13000 + 1400 + 140 + 12$ of the sum is replaced by the standard place value expansion $10000 + 4000 + 500 + 50 + 2$, in order to write the answer as the single number $14552$.

Replacements like the above were explicitly shown in the exposition formats that learners used in Terms 1 and 2; hence it was easy for learners to keep in touch with the underlying logic when doing calculations. However, in the abbreviated exposition formats learners may be using by Term 4 (vertical column exposition) they may easily lose sight of the replacements that provide the logical basis for the various steps, and the actual meaning of the digits they act upon (i.e. lose sight of place value).
2.1 Revision and practice

**Teaching guidelines**

Questions 1 to 4 provide opportunities to engage learners in some sharp thinking.

To utilise these opportunities, ask learners to read the whole of question 1 and to identify whether they expect any of the sub-questions (a), (b), (c), (d) and (e) to have the same answers. Once they have begun to consider this possibility, ask them to look specifically at questions (d) and (e), and to try to anticipate whether these two calculation plans may produce the same answer, or not.

Allow learners a few minutes to engage with 1(d) and (e). Then show them how the answers can be obtained by making transfers between place value positions. This can be done in various ways, for example:

1. (d) \[ 40 000 + 13 000 + 1 700 + 340 + 17 \]
   \[ = 40 000 + 14 000 + 700 + 350 + 7 \]
   \[ = 50 000 + 4 000 + 1 000 + 50 + 7 \]
   \[ = 50 000 + 5 000 + 50 + 7 = 55 057 \]

2. (e) \[ 40 000 + 3 000 + 10 700 + 1 340 + 17 \]
   \[ = 43 000 + 11 700 + 340 + 17 \]
   \[ = 54 000 + 700 + 300 + 50 + 7 \]
   \[ = 54 000 + 1 000 + 50 + 7 = 55 057 \]

**Answers**

1. (a) 30 406 (b) 34 060 (c) 34 006 (d) 55 057 (e) 55 057

2. (a) 30 000 (b) 73 848 (c) 90 000 (d) 30 000 (e) 130 000 (f) 30 000

3. (a) 63 951 (b) 63 951 (c) 63 951 (d) 63 951 (e) 63 951

4. (a) 54 901 (b) 62 744 (c) 25 876 (d) 25 876 (e) 60 001
Teaching guidelines
Apart from practice in estimation, question 5 also serves the purpose of inducing learners to apply their minds to careful reading and interpretation of the problem statements, and to alert them again to different meanings of subtraction.

Question 5(a), (b) and (c) may challenge learners for two reasons:

• They may be unsure how to go about making estimates instead of doing the calculations.
• They may find it difficult to figure out what operations to use.

If learners do not make good progress, you may suggest that they round off the given numbers to the nearest ten thousand and write number sentences as a way of interpreting the problem statements. You may demonstrate with (a):

A certain number + 20 000 = 60 000

Answers
5. (a) 40 000  (b) 80 000  (c) 80 000
6. (a) 36 022; 40 000  (b) 83 556; 80 000  (c) 83 556; 80 000
7. (a) and (b)  Not useful  
   (c) The calculation can be done as shown on the right.

   The calculations in (d) and (e) can be done as shown below. Learners may record the same reasoning differently.

   (d) 50 000  12 000  1 800  140  11  11  100  40  11
        -10 000  -9 000  -800  -20  -6
        40 000  3 000  1 000  120  5

   (e) 50 000  13 000  900  40
        -10 000  -9 000  -800  -20  -6
        40 000  4 000  100  20  5

8. (a) 6 + 6 + 7 + 5 = 24  
   (b) 70 + 40 + 80 + 40 = 230
   (c) 800 + 200 + 300 + 800 = 2 100
   (d) 3 000 + 9 000 + 8 000 + 7 000 = 27 000
   (e) 20 000 + 20 000 = 40 000
   (f) 69 354
9. (a) Example: 3 800 × 10 + (23 + 12 + 7 + 35 + 23 + 32 + 61 + 14 + 41 + 21)
   (b) 38 000 + 269 = 38 269

5. Do not calculate the answers to these questions now. Just estimate the answers to the nearest 10 000.
   (a) 23 767 is added to a certain number and the answer is 59 789. What is this number?
   (b) 23 767 is subtracted from a certain number and the answer is 59 789. What is this number?
   (c) A certain number is 23 767 more than 59 789. What is this number?

6. Calculate the exact answers for question 5. Then round off your answers to the nearest 10 000.

7. Which of the following will be useful replacements for 63 951 if you have to calculate 63 951 − 19 826? Explain your choices by showing how you would do the calculation with each of your choices.
   (a) 63 951 = 60 000 + 3 000 + 900 + 50 + 1
   (b) 63 951 = 952 + 62 999
   (c) 63 951 = 3 952 + 59 999
   (d) 63 951 = 50 000 + 12 000 + 1 800 + 140 + 11
   (e) 63 951 = 50 000 + 13 000 + 900 + 40 + 11

8. 23 876 + 9 246 + 28 387 + 7 845 can be calculated as shown on the right.

State which numbers were added to obtain each of the part answers in red.

Also write the final answer.

9. (a) Can you think of a quick way to find the answer for 3 823 + 3 812 + 3 807 + 3 835 + 3 823 + 3 832 + 3 861 + 3 814 + 3 841 + 3 821?
   (b) Find the answer.
Teaching guidelines

It is important that learners write their predictions for question 12 down, so that they can check them once they have done question 13.

Questions 12 and 14 provide very good opportunities for learners to talk about computation. Expressing their own ideas about numbers and computation can substantially enrich learners' understanding, knowledge and skills.

Assemble learners who have finished question 12 individually in small groups, before they do question 13. Ask them to tell each other why they believe some calculation plans will produce the same answer and others not. They do not need to reach agreement.

Also assemble learners who have completed question 14 individually in groups. Ask them to explain to each other how they developed the answer for each column. Some possible ways of doing it are described below.

Notes on questions

Allow learners to look for short methods themselves when doing question 14. Learners who do not identify short methods can do the questions by calculating normally.

14. (a) The first four numbers can be added, and the answer can be doubled.
14. (b) The sum of the first five numbers is $5 \times 8\,554 - (2 + 4 + 6 + 8)$
   The sum of the last five numbers is $5 \times 8\,554 + (2 + 4 + 6 + 8) + 10$
   So the sum of all the numbers is $10 \times 8\,554 + 10 = 85\,540 + 10 = 85\,550$
   There are also other ways to shorten the work, and to record it.
14. (c) $10 \times 7\,234 = 72\,340$
14. (d) $10 \times 6\,762 - 6\,762 = 67\,620 - 6\,762 = 60\,858$
14. (e) $6\,324 + 3\,676 = 10\,000$ and $10\,000 \times 5 = 50\,000$

Answers

10. (a) $52\,643 + 32\,849 = 85\,492$, so the answer is incorrect.
   (b) The smaller digits were subtracted from the larger digits.
11. (a) No, it should be 24\,579.
   (b) The person forgot to add 2\,844, because $42\,843 = 39\,999 + 2\,844$.
12. (b) and (c) will have the same answers.
   (a) and (d) will have the same answers.
13. (a) 53\,906 (b) 45\,436 (c) 45\,436 (d) 53\,906
14. See “Notes on questions” above for more information on this question.
   (a) 130\,616 (b) 85\,550 (c) 72\,340 (d) 60\,858 (e) 50\,000
2.2 Add and subtract in context

**Teaching guidelines**

Some learners may read question 1 without comprehension and add the two numbers to produce 139 131, which is wrong. Suggest to these learners that they write number sentences to represent the situations described in questions 1 and 2. Ask learners to now describe the difference between these two number sentences.

After learners have spent some time working on questions 1 and 2, you may write the following general number sentence on the board and ask learners to describe the difference between questions 1 and 2 by referring to this number sentence:

\[ 58\,700 - 2\,600 = 56\,100 \]

They may do this by talking in small groups.

**Notes on questions**

For question 4(a) some learners may round the given figures off to the nearest 10 000:

\[ 20\,000 + 10\,000 + 20\,000 + 10\,000 + 20\,000 = 80\,000 \]

Other learners may round off to the nearest thousand:

\[ 24\,000 + 12\,000 + 19\,000 + 14\,000 + 16\,000 = 85\,000, \]

which rounded to the nearest ten thousand gives 90 000.

The actual sum is 84 913.

**Answers**

1. 3 397
2. 63 226
3. (a) 20 389  
   (b) End of 2013: 79 021  
       End of 2014: 72 643  
       End of 2015: 63 939  
   (c) 63 939 + 20 389 = 84 328 or 84 328 − 20 389 = 63 939
4. (a) 80 000 votes  
   (b) A, C, E  
   (c) 84 913 votes  
   (d) 9 386 votes  
   (e) 1 662 votes
5. 89 102 learners
2.3 Rounding off in context

Teaching guidelines

This section comprises an investigation that provides extensive practice in rounding off, estimation, and calculation. Engaging in this activity may also lead to learners forming a rough idea of what they will later come to know as the mean or “average” of a set of numbers. The purpose of the activity is to explore ways in which a good estimate of the sum of all the numbers in the table can be made without actually adding the numbers up.

Learners can begin working on this investigation in class, but they should preferably spend substantial time at home taking their work further.

It is important that all learners quickly get a sense of the range of data in the table. You may help them to do this by asking them how many schools are represented in the table (6 \times 13 = 78), and to identify the smallest and the largest numbers (301 and 879). Once that is done, you may ask them to consider whether the total number of learners in all 78 schools is:

- smaller than 78 \times 300
- between 78 \times 300 and 78 \times 900 or
- bigger than 78 \times 900.

Reflecting on this question, and discussing it, will prepare learners for engaging with questions 1 to 7 on the next page.

The table below is for your convenience. It contains the same numbers as the table on Learner Book page 290 (see alongside), but here the numbers are arranged from smallest to largest in each column.

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How can you quickly make a good estimate of the total number of learners in these schools?
Teaching guidelines
Note that questions 1(a) and 2(a) are very different: 1(a) asks for the quickest plan, while 2(a) asks for the plan that will produce the best estimate.

There can be little argument that Plan A is the quickest.

Once learners have completed or are working on question 2(b), interrupt their work and ask them to explain to two classmates why they believe the plan they have chosen will produce a good estimate of the total number of learners in all 78 schools.

If learners find it too challenging to choose a representative number when they try to implement Plan C (question 4(b)), you may let them make a table in which the numbers are arranged from smallest to largest in each column, as in the table provided on the previous page of this Teacher Guide. When considering the middle row in this reorganised table, learners may think of selecting a number between 500 and 600.

Notes on questions
Plans A to D will produce the following answers.

Plan A: $6 \times 13 \times 500 = 78 \times 1000 = 78000$
Plan B: $6 \times 13 \times 600 = 78 \times 600 = 46800$
Plan C: The estimate depends on the number chosen as a representative number. If the number chosen is between 300 and 800, the answer will be between 23400 and 62400.
Plan D: Column totals from left to right: 6004, 7250, 7223, 7869, 7408 and 6109

The estimates based on the different column totals are: 36024, 43500, 43338, 47124, 44448 and 36114.

Plan E: A table with rounded numbers is given on page 324 of this Teacher Guide.

Plan F: A table with the hundreds parts only is given on page 325 of this Teacher Guide.

Answers
1. There can be little argument that Plan A is the quickest plan.
2. Learners choose a plan for the best estimate and carry out the plan.
   Answers will differ.
3. Learners choose a plan for the worst estimate and carry out the plan.
   Answers will differ.
4. Different plans are used and hence answers will differ.
5. 41773
6. Learners choose their best estimate.
7. Consider learners’ plans.
**Plans E and F**

Learners may use tables like the one below to list the rounded off numbers for Plan E, and the hundreds parts only of the numbers for Plan F.

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Plan E: The numbers rounded off to the nearest 100

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The rounded numbers can be analysed like this:

Number of learners to the nearest 100

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Number of schools in each category

The above information can be used to estimate the total number of learners as:

\[9 \times 300 + 18 \times 400 + 17 \times 500 + 17 \times 600 + 5 \times 700 + 9 \times 800 + 3 \times 900,\] which is 42 000.
**Plan F:** The hundreds parts of the learner numbers

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The numbers can be analysed like this:

**Number of learners to the nearest 100**

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**Number of schools in each category**

The above information can be used to estimate the total number of learners as:

\[19 \times 300 + 20 \times 400 + 20 \times 500 + 3 \times 600 + 9 \times 700 + 7 \times 800\]

which is 37 400.
Grade 5 Term 4 Unit 3  Properties of three-dimensional objects

Learner Book Overview

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<th>Content</th>
<th>Pages in Learner Book</th>
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<td>A more in-depth look at prisms, in particular rectangular prisms</td>
<td>292 to 293</td>
</tr>
<tr>
<td>3.2 Nets of rectangular prisms</td>
<td>Making a rectangular prism from its net</td>
<td>293 to 295</td>
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<tr>
<td>3.3 Nets of other prisms</td>
<td>Making more prisms (e.g. triangular, pentagonal and hexagonal prisms)</td>
<td>296 to 297</td>
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<tr>
<td>3.4 Nets of a square-based pyramid</td>
<td>Making a square-based pyramid from its net</td>
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<tr>
<td>3.5 Nets of a cylinder and a cone</td>
<td>Making circular cylinders and circular cones from their nets</td>
<td>299 to 300</td>
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</table>

CAPS time allocation 5 hours

CAPS page references 22 and 198

Mathematical background

Paper models of any prism, cylinder, pyramid or cone can be made from single sheets of paper. The net of a 3-D object has all the flat surfaces (faces) and curved surfaces of the object laid out flat in such a way that they are all connected along at least one side/edge, or at least one point/vertex. This is because the surfaces of three-dimensional objects are two-dimensional.

This unit builds on the work done in Term 2 Unit 6 where four basic kinds of objects were investigated by folding, rolling or curling sheets of paper. The idea of the net of a three-dimensional object is mathematically important because the net includes all the faces or surfaces, something the folded, rolled or curled sheets of paper in the previous unit did not do.

Resources

Boxes that are rectangular prisms, including cubes – ask learners to bring small empty boxes from home (e.g. cereal boxes, tea boxes, biscuit boxes, facial cream boxes, etc.)
Scissors
Sheets of paper
Photocopies of nets (optional) and squared paper – provided in the Addendum on pages 413, 421 and 422
Large round objects such as plates or saucers, or a paper plate for each learner
Sticky tape and glue sticks
3.1 Rectangular prisms

**Mathematical notes**
Rectangular prisms have six rectangular faces. Opposite pairs of faces are exactly the same shape and size. If all six faces are squares, they will automatically be the same size. Such a prism is called a cube. Cubes are special rectangular prisms in three dimensions, in much the same way that squares are special rectangles in two dimensions.

**Teaching guidelines**
Question 3 is quite challenging. Bring to learners’ attention that it is not stated that the object has six faces – it can have more, or fewer. Suggest to learners that if they find question 3 very challenging, it may help them if they first do question 4.

**Possible misconceptions**
Learners who did not believe that squares are special kinds of rectangles will probably also not believe that cubes are special rectangular prisms. This is not a serious issue. It is better that they doubt the truth of this than blindly take your word for it. At some point in the future they will suddenly realise that it is perfectly sensible. For now, just lodge the idea in their minds.

**Answers**
1. (a) ![Diagram](image1)
   (b) ![Diagram](image2)

2. (a) Yes, a rectangular prism has six faces.
   (b) No, all the faces might not be rectangles.

3. (a) Yes, it is possible; but we are not told that the object has only six faces and that they are all rectangular, so we cannot be sure.
   (b) Yes, it is possible; but we cannot be sure because some faces could have different quadrilateral shapes and we also do not know how many faces the object has.
   (c) Yes, it is possible; but we do not know how many faces the object has and some or all of the other faces might be triangles or other polygons.
   (d) Yes, it is possible; but we cannot be sure because even if the object has six faces, the other two faces might have other quadrilateral shapes.

4. (a) All of them because they all have more than one rectangular face; we are not told how many faces the object has or what the other faces look like.
   (b) All of them because they all have at least two rectangular faces; we are not told how many faces the object has or what the other faces look like.
Answers

4. (c) All of them because they all have at least three rectangular faces; we are not told how many faces the object has or what the other faces look like.
   (d) B, C and D because they all have at least four rectangular faces; we are not told how many faces the object has in total or what the other faces look like.

3.2 Nets of rectangular prisms

Mathematical notes
The net of a three-dimensional object has all of its faces (and curved surfaces, if applicable) laid out flat but connected in some way. It is important to be able to see which faces in a net are connected along their sides to form the edges in the 3-D object, and which faces may be opposite each other. Understanding how the net of the object relates to the object itself is very important in developing a fuller grasp of the spatial arrangement of the edges and faces of the object.

Teaching guidelines
Most boxes are rectangular prisms. Many of your learners have probably seen an “exploded” cardboard box that has been laid out flat. This is a good way to introduce the idea of a net. Allow your learners to investigate which faces are connected along their sides and which faces are opposite each other (each face is connected to four others and there are six faces in total, three pairs of faces that are identical and opposite each other).

Possible misconceptions
The spatial arrangement of the faces of a rectangular prism may be very challenging for young learners. If they struggle to “see” how the faces relate, especially with a cube where all six faces are identical squares, give them some cut-outs of nets. Let them fold the cut-outs into the prism and unfold them again to investigate which sides meet to form the edges and which faces are opposite each other.

Answers

1. (a) to (c) Practical work
Teaching guidelines
Learners may find it challenging to interpret the drawings of Prisms A, B, C and D in question 2. You may help them by demonstrating the positions of the red faces on a box, for example a closed shoebox or an A4 paper box. To save time, you could photocopy the four nets provided on page 421 in the Addendum.

Learners who have real difficulties with question 3 may be given copies of the diagrams so that they can cut them out and fold them to check whether the figure is a net or not.

Answers
2. Practical work
3. (a) to (b) Practical work
   (c) Diagram A will not form a cube – a cube has 6 faces.
      Diagram B will not form a cube – the net will fold to an open-ended cube, i.e. a cube with an open face, because two faces will overlap.
Teaching guidelines

Learners who are challenged by question 4 will probably benefit hugely if they shade one or two faces on the net that they have drawn, then cut it out and fold it to form a cube. They then check to which of the pictures their cube corresponds.

To save time, you could photocopy the six nets provided on page 422 in the Addendum.

Having a set of six cubes with their faces painted red and green, exactly as in the Learner Book, will be helpful too. Place the cubes on your table with labels (a) to (f) at them so that learners know which cube belongs to which sub-question. Invite them to look at the cubes to check their nets.

Answers

4. Examples:

(a) ![Net for Cube A]
(b) ![Net for Cube B]
(c) ![Net for Cube C]
(d) ![Net for Cube D]
(e) ![Net for Cube E]
(f) ![Net for Cube F]

4. Draw the nets of the following cubes on squared paper. Shade the faces that are red on the cubes below. Let $a$ be the face that is the base (it is at the bottom; it stays on the table).

- ![Cube A](a)
- ![Cube B](b)
- ![Cube C](c)
- ![Cube D](d)
- ![Cube E](e)
- ![Cube F](f)
3.3 Nets of other prisms

**Mathematical notes**
All prisms have two polygonal faces opposite each other and rectangles for the remaining faces. For example, a pentagonal prism has two identical pentagons opposite each other and five rectangular faces connecting them.

**Teaching guidelines**
If learners are over-challenged, you may provide them with enlarged copies of the nets to cut out and fold. Encourage them to investigate how the sides come together. Many repetitions of folding and unfolding may be necessary before they begin to develop a “mental map” of the relationships.

**Possible misconceptions**
Insufficient experience viewing 3-D objects, and folding and unfolding their nets to see how the parts fit, will result in learners having a great deal of trouble identifying relationships between faces and edges.

**Answers**
1. (a) C  (b) B  
   (c) E  (d) A
Teaching guidelines

When learners do question 2, alert them to the fact that they have to fold segments of the same width than the lengths of the sides on the bases. Instead of having learners trace the bases in the Learner Book, you may give them copies of the larger figures below.

Answers

2. Practical work:
   (a) Triangular prism, using base D
   (b) Rectangular prism or cube, using base B
   (c) Pentagonal prism, using base C
   (d) Hexagonal prism, using base A

A quick way to make a paper prism

Step 1: Fold sections on a sheet of A4 paper, more or less as shown by the broken lines in the diagram on the right.

Step 2: Fold the sheet into a “tube” with five or six faces along its length.

Step 3: With a little extra work, you can now make a paper prism. You need to draw and cut out two bases so that they fit the openings.

2. Make four prisms using the bases below. You can follow the instructions above to make the “tube” of rectangular faces for each prism.

   (a) a prism with one pair of opposite faces that are triangles
   (b) a prism with one pair of opposite faces that are squares
   (c) a prism with one pair of opposite faces that are pentagons
   (d) a prism with one pair of opposite faces that are hexagons
3.4 Nets of a square-based pyramid

Mathematical notes
Pyramids have a polygon as the base and a number of triangular faces that all come together at a common point.

Answers
1. (a) 5 faces
   (b) 4 triangles and 1 square

2. (a) Diagram B. When the diagram (net) is folded on the dotted lines, the four triangular faces can meet at a common point to form the top (apex) of the pyramid. The bottom side/base of each triangular face will then meet up with one side of the square, which forms the base of the pyramid.
   (b) There are a number of possibilities. Here are two examples:

   ![Diagrams of nets of square-based pyramids]

   (c) Consider and discuss learners’ answers.
3.5 Nets of a cylinder and a cone

Mathematical notes
We only deal with circular cylinders and circular cones.

The nets of cylinders have two circles (the two ends) and a rectangle (the curved surface).

The nets of cones have a circle (the base) and a large section of a circle that looks like a huge pizza slice, for example (the curved surface).

Notes on questions
Note that in question 2, diagrams A, B and F will certainly not form cylinders. C, D and E may form cylinders, so long as the lengths of the quadrilaterals are equal to the length of the circumference of the circle.

Answers
1. Practical work
2. Nets of cylinders: C, D, E

Diagrams A, B and F will not form closed cylinders.
Notes on questions
In question 4 it should be obvious that diagram (a) cannot be a net for a cone (the base/circle is not connected correctly to the “pizza slice”). It may be fairly obvious to the eye that (c) and (d) will not form a closed cone. However, although (b) looks like it may form a cone, this can only happen if the edge of the base (circle) has the same length as the curved edge of the “pizza slice” (curved surface).

Answers
3. (a) to (e) Practical work
   (f) One cone is tall and narrow; the other cone is less tall and has a wider/bigger base.
4. (a) No, the base must be connected to the circular edge.
   (b) Yes, provided that the circumference of the full circle (base) is the same as the length of the curved side of the three-quarter circle.
   (c) No, it will not form a closed cone; the circle (base) must be much smaller.
   (d) No, the part of the net for the curved surface is wrong; the shape is wrong – it should, for instance, not have four straight sides.
Grade 5 Term 4 Unit 4  

Common fractions

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<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
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<tr>
<td>4.1 Fractions of whole numbers</td>
<td>Finding fraction parts of collections and numbers</td>
<td>301 to 303</td>
</tr>
<tr>
<td>4.2 Fractions in diagrams</td>
<td>Fraction parts of shapes, and practice in stating equivalent fractions</td>
<td>304 to 305</td>
</tr>
<tr>
<td>4.3 Fractions on the number line</td>
<td>Fractions as numbers: representing fractions and mixed numbers on the number line</td>
<td>306</td>
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<tr>
<td>4.4 Solving problems</td>
<td>Using fractions in a variety of practical contexts</td>
<td>307 to 309</td>
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CAPS time allocation  
5 hours

CAPS page references  
16 and 199

Mathematical background
In Term 2 the focus was on dividing a whole into fraction parts, representing fractions with fraction strips, measuring length with fractions of a unit, equivalent fractions and representing fractions on the number line.

In Term 3 the focus was on consolidating understanding of equivalent fractions, and introducing addition and subtraction of fractions and mixed numbers.

In the current unit the idea of fractions of collections is extended to fractions of numbers. The unit also focuses on fraction parts of diagrams, specifically of circles in a way that will later support learners’ understanding of angle measure.

Resources
Sheets of paper
Round objects (e.g. tins, cups, saucers, plastic or metal lids)
Scissors
4.1 Fractions of whole numbers

**Teaching guidelines**
Ask learners to look at the array of green cubes in the tinted passage and say what they perceive. Ask them to think how they may find the total number of cubes without counting them one by one. They may say they can see ten columns of five cubes, or five rows of ten cubes. You could write $10 + 10 + 10 + 10 + 10 = 50$ on the board, and then put questions like the following to the class:

A. How much is one fifth of 50?
B. How much is three fifths of 50?
C. How much is five fifths of 50?

You may extend this to the following questions:
D. How much is one tenth of 50?
E. How much is three tenths of 50?
F. How much is eight tenths of 50?

**Notes on questions**
Questions 1(b) and (e) have several equivalent fractions as answers.

**Answers**

1. (a) 30 beads  
   (b) $\frac{6}{30}$ or $\frac{2}{10}$ or $\frac{1}{5}$  
   (c) $\frac{9}{30}$ or $\frac{3}{10}$  
   (d) $\frac{3}{30}$ or $\frac{1}{10}$  
   (e) $\frac{12}{30}$ or $\frac{4}{10}$ or $\frac{2}{5}$

2. (a) 3 beads  
   (b) 9 beads  
   (c) 12 beads  
   (d) 6 beads  
   (e) 48 beads  
   (f) 16 beads
Notes on questions
Question 3 is about a situation similar to the one in the tinted passage on the previous page. The answer to question (b) is three times the answer to question (a).

Question (c) may trigger the idea of a half, and (d) the idea of a quarter. If learners use the trigger, the answer can very easily be found mentally. Otherwise they need to go back to question (a) to help them get the answer.

Answers
3. (a) 5 (b) 15
   (c) 20 (d) 10

4. (a) $\frac{6}{18}$ or $\frac{1}{3}$
   (b) Count all the triangles to find out how many make up the whole.
   Count the number of triangles in the circle to see what part of the whole they make up.
   (c) $\frac{1}{7}$ (There are 7 groups of 5 in the diagram.)

5. She baked 270 biscuits.
   (One sixth is 45 biscuits, so the whole is $6 \times 45 = 270$ biscuits.)

6. He earned R4 200.
   (One tenth is R420, so the whole is $10 \times 420 = R4 200$.)

3. (a) How many beads are $\frac{1}{8}$ of 40 beads?
   (b) How many beads are $\frac{3}{8}$ of 40 beads?
   (c) How many beads are $\frac{1}{4}$ of 40 beads?
   (d) How many beads are $\frac{2}{3}$ of 40 beads?

4. Below are some collections of objects.
   (a) What fraction of the collection of triangles is in the circle?
   (b) Write down the steps that you followed when you found the fraction of the triangles in (a).
   (c) Here are biscuits that look like stars. What fraction of the number of biscuits is in the circle?

5. This is one sixth of the biscuits that Mama Thembu made for the church function. How many biscuits did she bake?

6. R420 was stolen from Biza’s bag. He said: “Someone stole exactly one tenth of the money I earned this month.” How much money did Biza earn this month?
Teaching guidelines
Questions 7 to 9 are demanding because there are no contexts that may support learners’ thinking. These questions are intended to promote more abstract thinking about fractions. However, learners should feel free to think of these questions as practical questions, for example to think of question 7(a) as asking: “How much is two fifths of R250?”

Go through the tinted passage with the class. There is an extra level of complexity here. You might like to write the question on the board. The first thing to ask is: “Is the answer going to be bigger or smaller than 16?” We have a whole number there (i.e. the 2), so it is going to be bigger than 16. The whole number gets multiplied by the whole number (i.e. 2 × 16), and then the fraction part is done.

Possible misconceptions
Learners might think that fraction questions always involve a smaller answer than the whole number given.

Notes on questions
You might like to discuss a few of the sub-questions in question 7 before letting the class work on their own. For example, in (a) somebody might suggest that you work out one fifth of 250 and then multiply the answer by 2. Somebody else might say you can multiply 2 by 250 and then divide by 5. If nobody suggests the second strategy, then don’t teach it. Accept correct strategies, but don’t teach them as formulas.

You might like to do question 9(a) with the class. Then they should work quickly and on their own, without writing down any steps.

Answers
7. (a) 100  (b) 66  (c) 450  (d) 455
   (e) 840  (f) 8 638

8. (a) 250 + 100 = 350
   (b) 99 + 66 = 165
   (c) 1 440 + 450 = 1 890
   (d) 2 457 + 455 = 2 912
   (e) 1 440 + 840 = 2 280
   (f) 24 680 + 8 638 = 33 318
   (g) 1 680 + 360 = 2 040
   (h) 1 440 + 1 200 = 2 640

9. (a) 12  (b) 21  (c) 26
   (d) 55  (e) 170  (f) 69

10. Two thirds of a bar

Nick has to calculate 2\frac{5}{8} of 16. He thinks like this:
2\frac{5}{8} means 2 + \frac{5}{8}. So 2\frac{5}{8} of 16 means two 16s plus \frac{5}{8} of 16.
That is 32 plus 10, which is 42.

8. Use your answers in question 7 and calculate:
   (a) 1\frac{2}{5} of 250
   (b) 1\frac{2}{3} of 99
   (c) 2\frac{2}{8} of 720
   (d) 3\frac{5}{9} of 819
   (e) 1\frac{7}{12} of 1 440
   (f) 2\frac{7}{10} of 12 340
   (g) 2\frac{3}{7} of 840
   (h) 1\frac{4}{6} of 1 440

9. You should be able to do the following mentally. This means you should be able to write down the final answer straight away without writing down anything else.
   (a) \frac{1}{2} of 8
   (b) \frac{2}{3} of 9
   (c) \frac{2}{6} of 12
   (d) \frac{3}{4} of 20
   (e) \frac{2}{5} of 50
   (f) \frac{2}{10} of 30

10. Three friends share two chocolate bars equally. How much chocolate does each one get?
4.2 Fractions in diagrams

Teaching guidelines
Partitioning a circle into fraction parts is not only a way to consolidate the fraction concept and equivalent fractions; it also lays a basis for the introduction of angle measurement in Grade 6.

To save time, you can photocopy the four circles provided in the Addendum on page 423.

Answers
1. See the next page in the Learner Book for the questions.

(a) ![Fraction circle](image1)
(b) ![Fraction circle](image2)
(c) ![Fraction circle](image3)
(d) ![Fraction circle](image4)
Teaching guidelines
First listen to learners’ explanations in question 2(c) before you refer them to the definition given in the Learner Book. Do NOT ask for a definition in a test or exam! If the learners can work with equivalent fractions and recognise them, that is sufficient.

When learners have finished question 3, ask them if they can work out why (c) and (d) have the same answer. They might be able to see (visualise) that the figures have the same shape but different orientations.

Answers
1. The solutions for (a), (b), (c) and (d) are on the previous page.

2. (a) They have the same value. (They have the same size.)
   (b) They have the same value. (They have the same size.)
   (c) They are fractions with the same value (the same size), but different names.

3. (a) \( \frac{10}{24} \) or \( \frac{5}{12} \)   (b) \( \frac{8}{24} \) or \( \frac{2}{6} \) or \( \frac{1}{3} \)
   (c) \( \frac{6}{24} \) or \( \frac{3}{12} \) or \( \frac{1}{4} \)   (d) \( \frac{6}{24} \) or \( \frac{3}{12} \) or \( \frac{1}{4} \)
4.3 Fractions on the number line

**Teaching guidelines**

Learners are already familiar with fractions on number lines. Here they are challenged to see that they are dealing with eighths (first number line), twelfths (second number line), and tenths (third number line), and then with twelfths on a slightly smaller scale (fourth number line). To save time, you can photocopy the number lines on page 424 of the Addendum.

This is an opportunity for learners to explore equivalent fractions on a variety of number lines. You might like to draw the number lines on the board and get learners to offer their answers. Look at the third number line below. You will see that here is a chance to show that $2\frac{5}{10} = \frac{2}{8}$. There are more possibilities than the answers given for question 2 below.

**Answers**

1. $\frac{3}{4} = \frac{6}{8} = \frac{9}{12}$ and $\frac{2}{6} = \frac{4}{12}$; also $1\frac{1}{4} = \frac{5}{8}$, $2\frac{5}{10} = \frac{2}{8}$, etc. (See “Teaching guidelines” above.)

2. Make a list of all the equivalent fractions that you found in question 1.
4.4 Solving problems

Teaching guidelines
This is a consolidation exercise. Rather than doing any teaching to the whole class, circulate among learners and provide support where needed.

Answers

1. (a) $\frac{2}{9}$  
   (b) $\frac{4}{9}$  
   (c) $\frac{1}{9}$  
   (d) $\frac{2}{9}$  
   (e) $\frac{1}{9}$  
   (f) $\frac{1}{10}$  
   (g) $4\frac{7}{10}$  
   (h) $2\frac{4}{7}$

2. $\frac{4}{10}$

3. (a) $20$ thirds $= \frac{60}{3}$ slabs of chocolate  
   (b) $20 \times \frac{2}{5} = \frac{40}{5} = 8$ bottles of juice

4. (a) $\frac{1}{5}$ of $100$ cm $= 20$ cm $\rightarrow \frac{3}{5}$ of $100$ cm $= 3 \times 20$ cm $= 60$ cm  
   (b) $30$ cm  
   (c) $25$ mm  
   (d) $\frac{6}{5} = \frac{3}{\frac{3}{5}} \rightarrow \frac{3}{7}$ of $1000$ m $= 750$ m  
   (e) $\frac{1}{10}$ of $1000$ g $= 100$ g $\rightarrow \frac{6}{10}$ of $1000$ g $= 600$ g  
   (f) $\frac{1}{5}$ of $1000$ g $= 200$ g $\rightarrow \frac{3}{5}$ of $1000$ g $= 600$ g  
   (g) $\frac{1}{8}$ of $1000$ g $= 125$ g $\rightarrow \frac{3}{8}$ of $1000$ g $= 375$ g  
   (h) $\frac{3}{4}$ of $1000$ g $= 750$ g
Answers

4. (i) 400 ml
   (j) 750 ml
   (k) \( \frac{1}{5} \) of 1 000 ml = 125 ml → \( \frac{3}{5} \) of 1 000 ml = 375 ml

Notes on questions

Question 5 is a simple revision of earlier fractions, with opportunities for spotting equivalent fractions. You might like to ask how much bread (how many loaves) is ten tenths, which is the answer to question 5(i). Some learners may have forgotten that there were 12 loaves to start with. You could go on to ask how much bread was given in each of the questions (a) to (h), or give this as homework.

Ask learners how they worked out their answers to question 6. They may indicate that they started by saying \( 8 \times 4 = 32 \) loaves, and then worked out the fraction. Accept any reasonable method.

Answers

5. (a) \( \frac{1}{10} \)
   (b) \( \frac{2}{10} \) or \( \frac{1}{5} \)
   (c) \( \frac{3}{10} \)
   (d) \( \frac{4}{10} \) or \( \frac{2}{5} \)
   (e) \( \frac{5}{10} \) or \( \frac{1}{2} \)
   (f) \( \frac{6}{10} \) or \( \frac{3}{5} \)
   (g) \( \frac{8}{10} \) or \( \frac{4}{5} \)
   (h) \( \frac{9}{10} \)
   (i) \( \frac{10}{10} \) (all of the bread)

6. \( \frac{34}{8} = 4 \frac{2}{8} = 4 \frac{1}{4} \) loaves (See the note regarding question 6 above.)

7. (a) \( \frac{1}{8} \)
   (b) One eighth = R75. Nick will get R75.
      Three eighths = R75 \( \times \) 3 = R225. Faaiez will get R225.
      One half of R600 = R300. Thandeka will get R300.
Notes on questions

Question 8 is an opportunity for finding equivalent fractions.

Answers

8. (a) \(\frac{1}{12}\)  
(b) \(\frac{2}{12}\) or \(\frac{1}{6}\)  
(c) \(\frac{3}{12}\) or \(\frac{1}{4}\)  
(d) \(\frac{4}{12}\) or \(\frac{1}{3}\)  
(e) \(\frac{6}{12}\) or \(\frac{1}{2}\)

9. (a) Juliet coloured one of the six columns in the diagram, so she coloured one sixth of the diagram. In doing so, she coloured two of the twelve blocks in the diagram. So, she also coloured two twelfths of the diagram.

It is very easy to see the equivalent fractions in the diagram: two brown blocks look like one sixth.

(b) 3 small blocks: three twelfths; one quarter  
4 small blocks: four twelfths; two sixths; one third  
6 small blocks: six twelfths; three sixths; two quarters; one half

(c) \(\frac{10}{12}\) or \(\frac{5}{6}\) (Some learners may already state the equivalent fraction before doing (d).)  
(d) \(\frac{10}{12}\) or \(\frac{5}{6}\)  
(e) \(\frac{5}{12}\)  
(f) \(\frac{8}{12}\) or \(\frac{2}{3}\)

8. A chocolate slab is divided into 12 small blocks.
   (a) What fraction of the whole slab is 1 small block?  
   (b) What fraction of the whole slab is 2 small blocks?  
   (c) What fraction of the whole slab is 3 small blocks?  
   (d) What fraction of the whole slab is 4 small blocks?  
   (e) What fraction of the whole slab is 6 small blocks?

9. Juliet draws the chocolate slab in question 8 in two different ways:

   (a) She says: "In question 8(b) I wrote that two small blocks are two twelfths of the whole slab. If I colour the first column in my second drawing I can see that two blocks can also be one sixth of the whole slab."

   Can you explain Juliet’s thinking?

   (b) Look at the two drawings of the slab and find more than one way to write 3, 4 and 6 small blocks as a fraction of the whole slab.

   (c) What fraction of the whole slab is 10 small blocks?  
   (d) Can you write that fraction in a different way?  
   (e) What fraction of the whole slab is 5 small blocks?  
   (f) What fraction of the whole slab is 8 small blocks?
Grade 5 Term 4 Unit 5          Whole numbers: Division

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<td>5.4 Ratio again</td>
<td>An investigation involving ratios between rates</td>
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**CAPS time allocation** 7 hours

**CAPS page references** 13 to 15 and 200 to 201

In Term 2 Unit 9 the focus for division was on grouping and sharing problems, i.e. situations in which a quantity is divided into equal parts. In this unit the focus is on the use of division to solve problems which involve a constant ratio between two quantities.

**Mathematical background**

Constant ratios between two quantities appear in different kinds of situations, for example:

- Enlargement and reduction (e.g. of photographs) and scale drawings (see Sections 5.2 and 5.3). The ratio of enlargement or reduction is also called the **scale factor**. The term “scale factor” is normally used with respect to maps.
- Implementation of recipes. For example, a recipe may specify 3 cups of flour, 2 cups of sugar and 5 ml salt. How many cups of sugar and how much salt should you mix with 6 cups of flour? The term “proportion” is often used with reference to recipes.
- Comparison of rates (see Term 2 Unit 5, Section 5.6 as well as Section 5.4 of this unit).
- Proportions in designs.
5.1 Revision practice

Notes on questions
Questions 1, 3, 4, 5 and 10 are grouping problems. Learners have to determine how many groups of a given size can be formed from a given total.

Questions 2, 6 and 8 are sharing problems. Learners have to determine how big each of a given number of equal shares is.

Question 9 is a ratio situation.

Teaching guidelines
One of the biggest teaching challenges in Mathematics is to empower learners to effectively read and interpret word problems and decide correctly what calculations to do to solve a given problem. The development of this capacity is often undermined by the availability of clues, external to the question itself, which helps the learner to identify the correct operation without having to engage with the problem description.

When learners read page 310 of the Learner Book, the unit title already tells them that the questions require division. Some learners may then simply divide the bigger number by the smaller number in each of the questions without actually reading the questions. In this way they may get all the answers right except for 9(a), without applying their minds to the questions at all!

To reduce the chances that this will happen, you may instruct learners at the beginning to write a short sentence or paragraph for each question, explaining why they believe the calculations they plan to do will provide the answer to the question. Alternatively, they may make a quick freehand sketch to represent the situation and the solution they provide.

Answers
1. Thivha can fill 25 egg boxes and 8 eggs are left over.
2. R416 ÷ 32 = R13
3. 32 bags (13 guavas left over)
4. 342 ÷ 48 = 7 rem 6 → 8 buses
5. 18 shoeaces
6. (a) 21 toffees (b) 5 toffees
7. (a) 33 rem 11 (b) 16 rem 40 (c) 29 rem 17 (d) 24 rem 21 (e) 11 rem 13 (f) 22 rem 13
8. 25 kg
9. (a) 80 kg (b) 5 kg
10. 12 boxes
5.2 Making pictures smaller and bigger

Teaching guidelines

There are three quantities involved in a simple ratio situation, as demonstrated in the following table of measurements for the two pictures described in question 1:

<table>
<thead>
<tr>
<th></th>
<th>x = measurement on big picture</th>
<th>30</th>
<th>120</th>
<th>192</th>
</tr>
</thead>
<tbody>
<tr>
<td>y = measurement on small picture</td>
<td>5</td>
<td>20</td>
<td>32</td>
<td></td>
</tr>
<tr>
<td></td>
<td>( x \div y )</td>
<td>6</td>
<td>6</td>
<td>6</td>
</tr>
</tbody>
</table>

The measurement on the big picture or object, and the measurement on the small picture or object, are variable quantities. The one measurement divided by the other (corresponding) measurement is a constant; it is called the ratio between the two variables.

At least three kinds of questions can be asked about ratio situations:

- The measurement on the **bigger object is given**, as well as the (big to small) ratio, and the corresponding measurement on the smaller object needs to be found, for example questions 1(b) and (c), and 2(b) and (c). This requires division by the ratio/scale factor.
- The measurement on the **smaller object is given**, as well as the (small to big) ratio, and the corresponding measurement on the bigger object needs to be found, for example questions 1(a) and 2(a). This requires multiplication by the ratio/scale factor.
- Some corresponding measurements on both objects are given, and the question requests calculation of the ratio. No question of this kind is included in this unit.

Possible misconceptions

Learners may interpret a constant ratio situation as a constant difference situation. For example, in question 2(a) they may give \( 8 + 60 = 68 \) as the answer.

Answers

1. (a) 30 mm  (b) 20 mm  (c) 32 mm
2. (a) 480 mm  (b) 30 mm  (c) 36 mm
5.3 Ratios of enlargement and reduction

**Teaching guidelines**

The purpose of questions 1 to 5 is to further develop learners’ understanding of ratio in the context of enlargement and reduction. Pictures A, B and C differ in size only, unlike Pictures D and F on page 314 of the Learner Book, which differ in a different way: Picture F is compressed across the width compared to Picture D.

**Answers**

1. Yes
2. It is the same picture, but not the same size.
3. 40 mm high and 60 mm wide
4. Yes, it is.
5. Picture A: 90 mm
   Picture B: 72 mm
   Picture C: 54 mm
**Possible misconceptions**

Enlargement and reduction which involve the same ratio in all directions (as demonstrated by Figures X and Z in question 10) should be distinguished from compression and stretching in one direction only (as demonstrated by the relations between Figures Y and Z, or between Figures X and Y).

Questions 9 and 10 are intended as vehicles to clarify this issue in class.

**Answers**

6. Learners check and correct their work in questions 3 and 5 if necessary.

7. (a) 90 mm high and 135 mm wide  (b) 162 mm

8. (a) 30 mm  (b) 36 mm

9. No

10. Figure Z
**Answers**

11. Learners measure and correct their work in questions 7 and 8 if necessary.

**Additional learning activity (See Addendum page 425)**
Which of the rectangles below are enlargements or reductions of the shaded rectangle? In each case, explain why you think it is, or why it is not.

A

B

C

D

E

11. Take the measurements of Pictures D and E to check your answers for questions 7 and 8.
5.4 Ratio again

**Teaching guidelines**
This section comprises an extended investigation that can be given as a project. Encourage learners to make drawings to support their reasoning about the questions.

Make sure that learners understand at the outset what is meant by “to keep up with his mother”.

**Answers**
1. 40
2. (a) 60  (b) 200
3. (a) 10  (b) 25
Teaching guidelines

Question 6 is tough, since the ratio between Lenka’s step length and Jasper’s step length is not known at this stage. To be able to produce the answer to the question, learners will have to think of using the mother ostrich’s step as an intermediary between Jasper and Lenka:

\[
15 \text{ steps by Lenka} = 9 \text{ steps by the mother} \\
= 9 \times 20 \text{ steps by Jasper} \\
= 180 \text{ steps by Jasper}
\]

This is a challenge that goes beyond the requirements of the Grade 5 curriculum. Learners can gain little by being shown how to get the answer, but their mental development can benefit from trying again after doing questions 7(a), (b) and (c), or if they do not manage then, trying again after doing questions 8 to 11. Please allow them to develop their own plan.

Answers

4. Number of steps by the mother

\[
\begin{array}{c|c|c|c|c|c|c|c|c}
\text{Number of steps by the mother} & 1 & 2 & 3 & 6 & 9 & 15 & 30 & 48 \\
\hline 
\text{Number of steps by Jasper} & 20 & 40 & 60 & 120 & 180 & 300 & 600 & 960 \\
\end{array}
\]

5. Number of steps by the mother

\[
\begin{array}{c|c|c|c|c|c|c|c|c}
\text{Number of steps by the mother} & 3 & 6 & 9 & 15 & 30 & 48 \\
\hline 
\text{Number of steps by Lenka} & 5 & 10 & 15 & 25 & 50 & 80 \\
\end{array}
\]

6. 180
Answers
7. (a) 50  (b) 600  (c) 600  (d) 180
8. (a) 14  (b) 27
9. (a) 120  (b) 210
10. (a) 60  (b) 720
11. (a) 5  (b) 25
12. 180

Teaching guidelines
If learners still do not get question 6 right when they do question 12, you may suggest that they complete the following table by combining the tables they completed in questions 4 and 5.

<table>
<thead>
<tr>
<th>Number of steps by the mother</th>
<th>3</th>
<th>6</th>
<th>9</th>
<th>15</th>
<th>30</th>
<th>48</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of steps by Jasper</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Number of steps by Lenka</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

7. (a) How many steps must Lenka take when the mother takes 30 steps, to keep up?
   (b) How many steps must Jasper take when his mother takes 30 steps?
   (c) How many steps must Jasper take when Lenka takes 50 steps?
   (d) How many steps must Jasper take when Lenka takes 15 steps?
   (You may skip this question again if you wish, and try to do it later.)
8. (a) One day Jasper had to take 280 steps to keep up with his mother. How many steps did she take?
   (b) On another day Jasper had to take 540 steps to keep up with his mother. How many steps did she take?
9. (a) One day Lenka had to take 200 steps to keep up with the mother. How many steps did the mother take?
   (b) One day Lenka had to take 350 steps to keep up with the mother. How many steps did the mother take?
10. (a) How many steps must Jasper take for five steps that Lenka takes, to keep up with her and the mother?
    (b) How many steps must Jasper take for 60 steps that Lenka takes, to keep up with her and the mother?
11. (a) How many steps must Lenka take for 60 steps that Jasper takes, to keep up with him and his mother?
    (b) How many steps must Lenka take for 300 steps that Jasper takes, to keep up with him and his mother?
12. If you have not answered question 6 yet, try to answer it now.
### Grade 5 Term 4 Unit 6  
Perimeter, area and volume

<table>
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<tr>
<th>Sections in this unit</th>
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<td>323 to 326</td>
</tr>
<tr>
<td>6.3 Volume and capacity</td>
<td>The concept of volume as the number of cubes that occupy the same space</td>
<td>327 to 330</td>
</tr>
</tbody>
</table>

**CAPS time allocation**  
7 hours

**CAPS page references**  
28 and 202

**Resources**  
Round objects such as mugs, tins or saucers to trace around to draw circles  
2 cm grid paper – see the Addendum, page 426  
Scissors; rulers; a piece of string about 10 cm long, for each learner

**Mathematical background**  
The picture of the box and the questions on page 318 of the Learner Book are intended to convey an idea of the differences between the concepts of perimeter, area and volume.

When we talk about perimeter, we mean the length of a line around the outer edge of an object (like the ant’s path along the red line on the top edge of the box). When we talk about area, we mean the area covered by a flat shape (like one face of the box, e.g. the area of the green face of the box). When we talk about volume, we mean the amount of space that something takes up (like one of the potatoes that occupy space).

It is not only regular shapes that have perimeter, area and volume, hence it is conceptually dangerous if learners’ ideas about perimeter, area and volume are tied to regular shapes for which these dimensions can be calculated with formulas. Each of the coloured shapes alongside has a certain perimeter and a certain area. Each learner’s own body has a certain volume.
Teaching guidelines
Spend time on these four introductory questions. You want learners to think and talk about aspects of real situations that relate to perimeter, area and volume. It is critically important that learners form their concepts of perimeter, area and volume as a refinement of ideas about real physical objects and not on the basis of formulas for the perimeter, area and volume of regular shapes.

Use “teachers’ wait-time” when you ask a question. Wait-time means you ask the question and then you wait 10 seconds before you accept any answers. During that silence, learners are not allowed to put their hands up; instead, they must think about their answers. They also have time to think about the reason for their answer. This method gets more thinking from more of the learners, and better quality answers.

Possible misconceptions
Learners see substances change their shape, for example a drop of water spreads out on a plate and a ball of clay can be flattened out into a disc. What learners are seeing is a change in surface area, not a change in volume. Solids and liquids keep their volume even when their shape changes.

Notes on questions & Answers
1. The perimeter of the open face of the box is indicated by the red line that the ant walks along. Ask learners to trace the perimeter of the box’s green face with a finger. Walk around and make sure that learners understand what perimeter means in this question. Ask them: “Is this perimeter as long as the red line the ant walked along?” (Answer: No, it is shorter. Two of the sides of the open face are longer than the sides of the green face.)
2. No, it does not look as though 200 of those potatoes would fit in. (You are developing the concept of volume here. The volume of the potatoes would be greater than the capacity of the box.)
3. The potato nearest to the box, maybe. Ask learners how they decided which potato is bigger. The one nearest to the box is shorter but higher. The one further away is longer but not as high. Allow the learners to articulate themselves their reasoning behind which is the bigger.
4. The pink face, because it is bigger. It is just as high/ wide as the green face, but it is longer than the green face.
6.1 Perimeter

Teaching guidelines
These questions are designed to encourage learners to think and talk about perimeter. Encourage them to give reasons for their answers and to think of ways of checking their answers. This section in particular requires learners to think about perimeter and area as two different measures of flat shapes.

Notes on questions & Answers
1. Here you can listen to learners’ answers, not to find out who has the right answer, but to find information about their ideas. Some learners will hear the word “biggest” and decide that the green splash is the biggest. These learners are thinking about “biggest area”, not “biggest perimeter”.

Notice how their thinking might change if you ask them: “Which one has the longest perimeter; which one has the shortest perimeter?” You could also ask them: “If you had to draw a pencil line around the edge of each of the shapes, which shape’s pencil line would take the longest to draw?”

The yellow splash has the biggest perimeter; the green splash has the smallest perimeter.

2. You will need more paint to cover the green splash: it has the biggest area, even though it has the shortest perimeter. The yellow splash needs the least paint, because it has the smallest area even though it has the longest perimeter. This question shifts the learners’ attention from perimeter to area; it reminds them that “biggest area” is not the same as “biggest/longest perimeter”.

3. Perimeter of green splash: 157 mm
   Perimeter of red splash: 161 mm
Mathematical notes
Although this is a cumbersome and apparently primitive method to approximate the perimeter of a figure, it provides learners with an early experience of a strategy that is widely used in higher mathematics: to approximate the perimeter, area or volume of curved shapes with a combination of straight lines, polygons or polyhedra.

For example, the area of the ellipse below is between the areas of the shaded areas on the left and the right below. Because of the outward curvature of the ellipse the error is smaller with the approximation on the right; hence the actual area is bigger than midway between the shaded areas on the left and the right. That means that the actual area is between the average of the two shaded areas, and the shaded area on the right. Horizontal strips will produce an even better approximation. Obviously, narrower strips will also produce better approximations. In advanced mathematics, calculations are done that reveal what the approximation would be for strips as narrow as you want them to be.
Notes on questions
Question 5 is intended to make learners aware of the fact that better approximations can be obtained by measuring shorter straight lines than by measuring longer straight lines.

Answers
4. Answers may differ slightly:
   (a) 183 mm = 18 cm and 3 mm = 18\frac{3}{10} cm
   (b) 195 mm = 19 cm and 5 mm = 19\frac{5}{11} cm or 19\frac{1}{2} cm
5. The blue-edged polygon on the right-hand side
Notes on questions & Answers

6. The four circles must be the same size (i.e. their diameters must be equal, but it does not matter how big they are).

7. The Learner Book does not show a diagram for this question (i.e. for the first circle), but you can refer learners to the polygons on the previous page. The more line segments the polygon has, the closer it resembles the true curved shape. In the same way, learners can draw a polygon inside (or outside) their first circle. The more line segments they draw, the closer the polygon resembles the true shape of the circle.

8. If you add up the lengths of the four sides of the square inside the circle, you will find that their sum is shorter than the perimeter of the circle. If you add up the lengths of the four sides of the bigger square outside the circle, you will find that their sum is longer than the perimeter of the circle. So the true perimeter length of the circle is shorter than the outer square and longer than the inner square. Therefore option (c) is the correct answer.

9. The left-hand diagram in question 9 uses the square as a guide to make it easier to draw the eight-sided polygon outside the circle. (Ask learners to count the eight sides.) The right-hand diagram also uses a small square as a guide to draw the eight sides inside the circle.
6.2 Area

Teaching guidelines
The activities in this section are designed to provoke the idea of covering a surface in learners’ minds, as a basis for the concept of area as the number of identical squares, laid tightly together without overlapping, needed to cover the surface.

The time spent on question 1(b) is worthwhile, because it will provide learners with a powerful concrete experience of the essence of the concept of area.

2 cm grid paper is provided in the Addendum on page 426.

Notes on questions
The two splashes are identical, but they are placed in different positions relative to the grid lines. This may result in learners placing their 2 cm by 2 cm squares differently in the two cases, leading to different approximations.

The stickers need to be placed to line up with the grid lines.

Answers
1. (a) 9 stickers from each splash is the correct estimate. See the diagram below.
(b) 9 stickers can be cut from each of the splashes. The purpose of the question is not to elicit an exact answer (this is not possible), but to make learners go through the physical experience of covering a surface with square pieces without overlapping or leaving gaps.
Notes on questions
In question 2 learners have to take account of the fact that only the wall will be painted, not the doors and the windows. While the wall, windows and door together cover about 30 square patches, the parts that have to be painted (including the chimney) cover about 20 square patches.

Answers
2. Learners’ estimates will differ.
   Encourage learners to explain how they estimated.
   Reasonable estimates could be between 18 and 22 square patches.
   Amount of paint needed: between 4 320 ml and 5 280 ml.

3. Blue covers the biggest area; red covers the smallest area.

4. The blue part of the wall has an area of 22 grid squares.
   The pink part of the wall has an area of 21 grid squares.
   The red part of the wall has an area of 16 grid squares.
Notes on questions
Learners should simply count grid squares to get the answer. They are not expected to work with formulas to calculate the answer.

Learners need to see that each of the four shapes covers some of the grid squares only partially. In these diagrams all the partially covered grid squares are half grid squares.

Answers
5.  (a) Area of the blue triangle: $24\frac{1}{2}$ grid squares
    Area of the purple triangle: $4\frac{1}{2}$ grid squares
    Area of the pink triangle: 8 grid squares
    Area of the light green quadrilateral: 40 grid squares

    (b) 77 grid squares

6. Area of red triangle: 98 grid squares
    Area of blue triangle: 18 grid squares
    Area of dark green triangle: 32 grid squares
    Area of light green quadrilateral: 160 grid squares

7. No, they are the same size.
   Learners can check this by tracing one of the triangles, cutting it out and superimposing it on the other triangle. In question 6, the grid squares are smaller: 4 grid squares in question 6 fit onto 1 grid square in question 5.
**Notes on questions**

In question 8 learners can first estimate the areas by counting all grid squares that are completely covered by Splash A and all grid squares that are partially covered by Splash A. Learners will then see that Splash A has an area of between 37 and 68 grid squares. When they try to make whole grid squares out of part grid squares they should find that Splash A has an area of about 55 grid squares. Similarly, Splash B has between 50 and 65 grid squares. By counting grid squares and making whole grid squares out of parts, they should find that Splash B has an area of about 55 grid squares.

Learners can trace the shape of one of the coloured parts in question 9, cut it out and place it over the other part, to see that they have the same area and perimeter.

Learners can use string to find the length of the curved side, and add this to the lengths of the other three sides.

**Answers**

8. Splash A has an area of about 55 grid squares.
    Splash B has an area of about 55 grid squares.

9. (a) The area of the two colours is equal, i.e. half the area of the rectangle:
    \[ 38 \frac{1}{2} \text{ grid squares}. \]
    (b) Learners could measure the perimeters by using the millimetre scale on their rulers:
    \[ \text{Perimeter} = (\text{half the perimeter of the rectangle}) + (\text{the length of the curved side}) \]
    \[ = 18 \text{ grid square side lengths} + \text{about 12 grid square side lengths} \]
    \[ = 118 \text{ mm} + \text{about 78 mm} = 196 \text{ mm} \]

10. (a) Learners investigate. The dark green triangles have equal areas of approximately 38 grid squares.
    (b) Learners investigate. The perimeters differ.
    \[ \text{Perimeter top left dark triangle: 151 mm} \]
    \[ \text{Perimeter top right dark triangle: 155 mm} \]
    \[ \text{Perimeter bottom left dark triangle: 168 mm} \]
    \[ \text{Perimeter bottom right dark triangle 152 mm} \]
6.3 Volume and capacity

Teaching guidelines
You should remind learners that they have already worked with volume and capacity in Term 1 Unit 9.

Note that there is only one question on pages 327 and 328 of the Learner Book. The material is intended to support classroom discussions about the ideas of volume and capacity. To encourage learners to take note of the situation described in the Learner Book, you may start by asking them to figure out what the pictures and text on page 327 are all about. You may ask them: “What do these pictures show us?”

The purpose of question 1 is to encourage learners to think and talk about volume and capacity. You might ask question 1 in more than one way, depending on the language ability of the learners: “Does the tray on the right have enough space for all the clay?” means the same as “Does the tray have enough room for all the clay?” and “Is the tray big enough to hold all that clay?”

Answers
1. As stated above, the purpose of the question is to encourage learners to think and talk about volume and capacity.
Teaching guidelines
To engage learners in the text and pictures on page 328 of the Learner Book, you may ask questions such as the following:

1. How much space is still available in the container at the top of the page?
2. How many of the half-litre bricks will fill up the 2-litre container?
3. How much clay can be added to the $\frac{3}{2}$-litre brick to fill the tray?
4. How many of the cubes of red clay are needed to make the ball of clay?

An additional classroom activity
At least 16 ml (or 16 cm$^3$) clay or play dough is needed for this practical activity.

The photo of the ball of clay is quite surprising; many learners won’t believe that all eight of those cubes will go into that one ball of clay. So show it, with real clay.

*Before the lesson,* make eight cubes of 1 cm$^3$ and squash them together into a ball. Then make another eight cubes of 1 cm$^3$ each.

In the lesson, refer learners to the photo of the ball and eight cubes of clay and ask them: “If I put those eight cubes together, would they be bigger, smaller, or the same volume as the ball?”

Many learners will answer that the eight cubes have more volume than the ball.

Then ask one of them to squash all eight cubes into another ball. Ask the learner to hold up the ball and compare it with the one you made before the lesson from your own eight cubes – they will be about the same volume. The volumes of the eight little cubes are still the same as before, because none of the clay has been lost.

Mathematical notes
A ball (a sphere) is the object that can hold the greatest volume for the least outer surface area.

You could pack the eight cubes together in a block and measure the outside surface area of the block. But if you squash the cubes together into a ball, the skin of the ball will have a smaller surface area than the skin of the block. However, the volume of the block and the ball would be the same!
**Teaching guidelines**

Apart from the fact that learners may take much time to build the stacks as they are shown in the pictures, it is not necessarily useful to let learners work with actual cubes when they do these questions.

**Answers**

2. (a) 4 cubes  
   (b) 6 cubes  
   (c) 12 cubes  
   (d) 12 cubes  

3. 8 cubes
Notes on questions
Make sure that learners understand that question 4 is about one stack that is shown from two different positions.

You could ask learners to work out the answer to question 5 in another way as well: they must imagine taking horizontal slices across the stack. The top slice has $4 \times 3$ cubes; the second slice has $4 \times 5$ cubes; the third slice has $4 \times 6$ cubes. Now add up all the cubes in the three slices.

Answers
4. 36 cubes
5. 56 cubes
6. (a) 27 cubes (b) 64 cubes (c) 216 cubes (d) 125 cubes
### Position and movement

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**Mathematical background**

Square grids are used in Mathematics as well as Geography to represent positions and movements. Each cell on a square grid has an “address” that is specified in terms of its position in relation to the so-called horizontal and vertical axes (in yellow), as demonstrated below.

The grid on the left shows **alpha-numeric addresses**, which are used in Geography and Intermediate Phase Mathematics.

The grid on the right shows **Cartesian coordinate addresses**, such as used in Mathematics from Grade 7 onwards.

**Resources**

Grid paper (see Addendum, page 412) or photocopies of a 10×10 grid (see Addendum, page 425)
7.1 Moving between positions on a grid map

**Teaching guidelines**

Ideally you should draw a copy of the grid map on the board; the colour is not needed. Tell learners that “moving back” as indicated in red on the left below is not allowed. Allow learners to come to the board and indicate some other ways to get from A1 to C4 by moving only left or right, and up or down. Two ways are shown below, in the middle and on the right. There are several more ways.

Keep the above on the board for the explanations that you may need to do after question 2 on the next page.

To save time, you could provide learners with photocopies the grid provided on page 425 in the Addendum.

**Answers**

1. Grid map:

![Grid map diagram](image-url)
Teaching guidelines
After learners have done question 2, you will have to explain to them what is meant by 1 unit of distance, as described in the tinted passage.

Answers

2. 5
   (a) Possibilities:
   2 units to the right and 3 units up;
   1 unit right, 3 units up, 1 unit right;
   3 units up, 2 units to the right;
   2 units up, 1 unit right, 1 unit up, 1 unit right.
   There are several more possibilities.

   (b), (c), (d): Many possibilities in each case, similar to (a) but more.

3. (a) 5 units  (b) 6 units
   (c) 7 units  (d) 12 units

4. There are many possibilities; see answer for question 2.

5. (a) and (b) A10 and J1, also A1 and J10

6. Distance from A1 to J10: 18 units

7. See the red blocks above. A large number of different routes are possible, for example:
   Route 1: B10 to B2, B2 to I2
   Route 2: B10 to F10, F10 to F6, F6 to I6, I6 to I2
   The distance is the same for all routes: 15 units.
Grade 5 Term 4 Unit 8

Transformations

### Learner Book Overview

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### CAPS time allocation

- 4 hours

### CAPS page references

- 23 and 205

### Mathematical background

Artists and graphic designers often use rotations, translations and reflections in their work.

Tessellations are patterns formed by positioning objects (tiles) with the same shape to cover an area, or by repeating shapes when painting a surface. There are no gaps or overlaps in a tessellation. The process of arranging the identical shapes involves transformations: we can imagine each tile in a tessellation to be translated, rotated or reflected compared to the other tiles.

Tessellations occur in nature, for example in honeycombs and on fish and snakes, as well as in man-made structures such as brick walls, pavements, and wall and floor tilings.

Some tessellations are more complex and have two or more different tile shapes or sizes. The extreme is a mosaic where every single tile may be different to all the others.
8.1 Rotations, reflections and translations in art

**Teaching guidelines**
Learners have engaged with rotations, translations and reflections before, but it would be good to quickly refresh their knowledge. You may do so by drawing simple examples on the board, like those on page 244 of the Learner Book.

**Notes on questions**
Allow learners to articulate and describe in their own words the figures and the transformations that they can identify. Developing and confirming the vocabulary to describe a transformation is important. Learners need to have clarity about what constitutes a translation, a rotation and a reflection.

**Answers**
1.

- [Copy](#)
- Reflection

2. Example:

Learners could point out other figures. Consider all learners' drawings.
Teaching guidelines
In answering these questions, learners should focus on the outlines of shapes, not on the decorative detail within shapes.

Answers
3. (a) In the upper right of the part of the artwork shown in question 3, the green pentagon is a rotation of the maroon pentagon.
   (b) A vertical reflection A horizontal reflection

4. (a) and (b)
   The black triangle is a rotation of the blue triangle in each of these three examples.

5. (a) The blue triangles in the upper left and lower right parts of the artwork are rotations of each other (they are also reflections of each other). The same goes for the maroon triangles on the lower left and upper right. The pink arrows in the middle are rotations of each other (they are also reflections of each other). The same goes for the grey arrows.
   (b) At the top, 
   and at the bottom:
8.2 Tessellations

Mathematical notes

Tessellations often involve repeated arrangement of a tile. Since each tile is next to another tile, there may be translation or reflection involved. In cases where tiles must be turned to fit, rotation is involved. Each of the tessellations in this section is made up of a single shape. It is a fact that any triangle will tessellate. This is also true for quadrilaterals.

Teaching guidelines

This section is very brief. There is a great deal more to tessellations than space or time permits here.

If time permits, you may wish to include additional tile shapes to tessellate. Printing and cutting many copies of the same triangle or quadrilateral will provide you with additional tessellation activities. Give each learner his/her own shape (triangle or rectangle), allow them to create their own tessellation through transformation of their shape, and let them describe their tessellation.

Possible misconceptions

It is possible to arrange tiles so that they do not tessellate, i.e. that there are gaps between the tiles. If learners do this, remind them that there are no gaps in a tessellation. Otherwise they may believe that the activities are about arranging tiles in any pattern, including non-tessellating patterns. This will probably force them into trying to rotate or reflect a tile to ensure no gaps occur, which will serve the main focus of this section well.

Answers

1. (a) Practical work
   (b) The statements are true.

2. (a) The red quadrilaterals
   (b) The yellow quadrilaterals
   (c) No

3. Learners’ own work
**Answers**

4. and 5. Practical work

6. (a) Yes

The template in the red position is rotated through half a revolution around point 1, to move it to the yellow position. When the template is in the yellow position, it is rotated through half a revolution around point 2, to move to the green position. These two movements are then made repeatedly to move the template from one position to the next horizontally.

From the yellow position the template can be rotated around point 3 to move it to the grey position.

(b) No

(c) No

7. Yes
Notes on questions
It is important that learners use the terms “translation”, “rotation” and “reflection” to describe how they moved a shape to create a tessellation.

You can ask learners whether they notice anything about the way the shapes are placed in relation to each other. The importance of no open spaces in a tessellation may lead learners to realise that shapes in a tessellation are generally placed with sides of equal lengths alongside each other in order to create a perfect fit, leaving no open spaces. Also, the sides of different shapes are combined to form another side length to place a shape against.

Answers
8. (a) Practical work
   (b) Learners describe their tessellation movements.
9. Learners’ own work
10. Practical work. The pentagon cannot tessellate; all the other shapes can.
Grade 5 Term 4 Unit 9 Geometric patterns

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CAPS time allocation 2 hours
CAPS page references 19 and 206

Continuing sequences or completing tables according to a pattern not only provides opportunities to develop understanding of patterns, but also contributes to the development of the Mental Mathematics section of the CAPS.

Mathematical background

As in Term 2 Unit 7, the approach in this unit is not to reduce the work on geometric patterns to numeric patterns in tables but to use the visual aspects of geometric representations as a method to find rules based on the structure of the geometric figures.

As stated before, this implies that you should help learners to not count the number of dots in a figure one by one but to use “clever counting” instead, by identifying appropriate larger, repeating units. Learners then shouldn’t just count the larger, repeating units – they should also write down a numerical expression (calculation plan or rule) describing the number of dots. It is very important that learners learn to withhold immediate calculation of a numerical expression – what is needed, is to analyse the structure of the expression as an object, and to generalise the structure, not to generalise numbers.

To find a general rule for the pattern requires a second level of pattern recognition, namely recognising the structure in a series of numerical expressions – what doesn’t change (is constant) and what changes (is variable). This process is illustrated below.

“The mathematician’s patterns, like the painter’s or the poet’s, must be beautiful; the ideas, like the colours or the words, must fit together in a harmonious way. Beauty is the first test.”

GH Hardy
9.1 Making a geometric pattern

Teaching guidelines

This section provides learners with an experience of the process of making an interesting geometric pattern (sequence), namely to repeat the same steps (rule) to make each next figure in the pattern (or each next number in the sequence). In this case, the rule is to form a new square by joining the midpoints of the sides of the innermost square.

You should either directly teach the process by letting learners close their books while you dictate “Draw a square and colour it,” etc., or you should make sure that learners understand the process before tackling the questions.

Although the section starts with a geometric pattern, we later transform it into a numeric pattern.

The numeric pattern involves fractions. Learners can find the fractions by drawing appropriate lines to divide each figure into an equal number of parts, as illustrated here.

However, after using the pictures to find the first few fractions, learners should not continue in the geometric context, but rather use the numeric sequence as a model to imitate the geometry.

It should be clear that in the numeric sequence the horizontal pattern is to halve the previous number. Learners have met this before, namely on page 264. They should find it relatively easy to continue halving all the way to the tenth number.

However, instead of continuing the horizontal pattern of halving up to 10, it may be easier to use the vertical pattern (rule) to find the tenth number directly. We emphasise again that we do not generalise the numbers, but the structure, as illustrated here:

<table>
<thead>
<tr>
<th>Figure no.</th>
<th>Fraction of figure that is coloured</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$\frac{1}{2}$</td>
</tr>
<tr>
<td>2</td>
<td>$\frac{1}{4}$</td>
</tr>
<tr>
<td>3</td>
<td>$\frac{1}{8}$</td>
</tr>
<tr>
<td>4</td>
<td>$\frac{1}{16}$</td>
</tr>
<tr>
<td>5</td>
<td>$\frac{1}{32}$</td>
</tr>
</tbody>
</table>

Answers

1. $\frac{1}{2}; \frac{1}{4}$
2. Every new square (the coloured part) is half of the previous one.
   Keep on halving the number to get the next one in the pattern.
9.2 Describing patterns

Teaching guidelines
You should try to let all learners attempt all the pattern designs. If learners have the mindset not to tackle problems in isolation but to always think about the relationship between the patterns, it will help conceptually and timewise.

Notes on questions
There are several important mathematical concepts embedded in the context, including that of constant and variable. These concepts will arise naturally from the identification of “counting units” in the pictures, as illustrated here for Pattern 1 and Pattern 4.

Learners should do and discuss all four questions in this section.
Answers

1. (a) Green: 2\times6 = 12 \quad \text{Purple: 5} \quad \text{Total: } 2\times6 + 5 = 17
(b) Green: 2\times20 = 40 \quad \text{Purple: 5} \quad \text{Total: } 2\times20 + 5 = 45

(c) | Size no. | 1 | 2 | 3 | 4 | 5 | 6 | 20 |
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</tr>
</thead>
<tbody>
<tr>
<td>No. of green beads</td>
<td>2</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>10</td>
<td>12</td>
<td>40</td>
</tr>
<tr>
<td>No. of purple beads</td>
<td>5</td>
<td>5</td>
<td>5</td>
<td>5</td>
<td>5</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>Total no. of beads</td>
<td>7</td>
<td>9</td>
<td>11</td>
<td>13</td>
<td>15</td>
<td>17</td>
<td>45</td>
</tr>
</tbody>
</table>

(d) 7, 8, 9, 10, 15 \rightarrow \quad 19, 21, 23, 25, 35

2. (a) Green: 6\times4 = 24 \quad \text{Purple: 6\times3 = 18} \quad \text{Total: } 6\times7 = 42
(b) Green: 20\times4 = 80 \quad \text{Purple: 20\times3 = 60} \quad \text{Total: } 20\times7 = 140

(c) | Size no. | 1 | 2 | 3 | 4 | 5 | 6 | 20 |
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</thead>
<tbody>
<tr>
<td>No. of green beads</td>
<td>4</td>
<td>8</td>
<td>12</td>
<td>16</td>
<td>20</td>
<td>24</td>
<td>80</td>
</tr>
<tr>
<td>No. of purple beads</td>
<td>3</td>
<td>6</td>
<td>9</td>
<td>12</td>
<td>15</td>
<td>18</td>
<td>60</td>
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<tr>
<td>Total no. of beads</td>
<td>7</td>
<td>14</td>
<td>21</td>
<td>28</td>
<td>35</td>
<td>42</td>
<td>140</td>
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</table>

(d) 7, 8, 9, 10, 15 \rightarrow \quad 49, 56, 63, 70, 105

3. (a) Green: 2\times6 = 12 \quad \text{Purple: 2\times6 + 1 = 13} \quad \text{Total: } 4\times6 + 1 = 25
(b) Green: 2\times20 = 40 \quad \text{Purple: 2\times20 + 1 = 41} \quad \text{Total: } 4\times20 + 1 = 81

(c) | Size no. | 1 | 2 | 3 | 4 | 5 | 6 | 20 |
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<td>6</td>
<td>8</td>
<td>10</td>
<td>12</td>
<td>40</td>
</tr>
<tr>
<td>No. of purple beads</td>
<td>3</td>
<td>5</td>
<td>7</td>
<td>9</td>
<td>11</td>
<td>13</td>
<td>41</td>
</tr>
<tr>
<td>Total no. of beads</td>
<td>5</td>
<td>9</td>
<td>13</td>
<td>17</td>
<td>21</td>
<td>25</td>
<td>81</td>
</tr>
</tbody>
</table>

(d) 7, 8, 9, 10, 15 \rightarrow \quad 29, 33, 37, 41, 61

4. (a) Green: 2\times6 = 12 \quad \text{Purple: 2\times7 + 1 = 15} \quad \text{Total: } 2\times(6+7) + 1 = 27
(b) Green: 2\times20 = 40 \quad \text{Purple: 2\times21 + 1 = 43} \quad \text{Total: } 2\times(20+21) + 1 = 83

(c) | Size no. | 1 | 2 | 3 | 4 | 5 | 6 | 20 |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of green beads</td>
<td>2</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>10</td>
<td>12</td>
<td>40</td>
</tr>
<tr>
<td>No. of purple beads</td>
<td>5</td>
<td>7</td>
<td>9</td>
<td>11</td>
<td>13</td>
<td>15</td>
<td>43</td>
</tr>
<tr>
<td>Total no. of beads</td>
<td>7</td>
<td>11</td>
<td>15</td>
<td>19</td>
<td>23</td>
<td>27</td>
<td>83</td>
</tr>
</tbody>
</table>

(d) 7, 8, 9, 10, 15 \rightarrow \quad 31, 35, 39, 43, 63
9.3 Completing tables

**Mathematical notes**

The geometric pattern in this section introduces two new kinds of numeric patterns, which are different from the usual multiples and common differences we have been studying, namely:

- triangular numbers: 1, 3, 6, 10, 15, ...
- square numbers: 1, 4, 9, 16, 25, ...

These two sequences are different, but they are the same in that they have the same type of **horizontal pattern** of increasing differences:

\[
\begin{align*}
&1 \quad 3 \quad 6 \quad 10 \quad 15 \\
&\quad +2 \quad +3 \quad +4 \quad +5 \quad +6
\end{align*}
\]

These two sequences can be represented as geometric triangles and squares, as illustrated here, and this does explain their names.

The geometric representation of square numbers then gives us an easy **vertical rule** to calculate further-lying values instead of continuing the horizontal pattern, for example \(S_{10} = 10 \times 10\).

The triangular numbers do not have such an easy vertical rule, but the geometric representation helps us to calculate further-lying values in a clever way, for example to calculate the number of yellow tiles in Figure no. 10:

\[
T_{10} = 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10
\]
\[
= (1+10) + (2+9) + (3+8) + (4+7) + (5+6) \ldots \ldots = 5 \times 11 = 55
\]

**Answers**

1. Complete this table. Describe and discuss the methods that you used.

<table>
<thead>
<tr>
<th>Figure no.</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of yellow tiles</td>
<td>1</td>
<td>3</td>
<td>6</td>
<td>10</td>
<td>15</td>
<td>21</td>
<td>55</td>
</tr>
<tr>
<td>No. of white tiles</td>
<td>3</td>
<td>6</td>
<td>10</td>
<td>15</td>
<td>21</td>
<td>28</td>
<td>66</td>
</tr>
<tr>
<td>Total no. of tiles</td>
<td>4</td>
<td>9</td>
<td>16</td>
<td>25</td>
<td>36</td>
<td>49</td>
<td>121</td>
</tr>
</tbody>
</table>

2. There is an increasing difference between consecutive numbers for each row, for example for the yellow tiles: \(1 \rightarrow 3 \rightarrow 6 \rightarrow 10 \rightarrow 15 \rightarrow 20 \rightarrow 25 \rightarrow 30 \rightarrow 35 \rightarrow 40 \rightarrow 45\) = 2 601 triangles

3. How many triangles are there in total in Figure 10?\(51 \times 51\)
Grade 5 Term 4 Unit 10  Number sentences

Learner Book Overview

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>10.1 Solve and complete number sentences</td>
<td>Learning to solve number sentences with the “numerical method”, and doing Mental Mathematics</td>
<td>342 to 343</td>
</tr>
<tr>
<td>by trial and improvement</td>
<td></td>
<td></td>
</tr>
<tr>
<td>10.2 Flow diagrams, number sentences and tables</td>
<td>An investigation in which flow diagrams, number sentences and tables are used to solve a practical problem</td>
<td>344 to 345</td>
</tr>
</tbody>
</table>

CAPS time allocation  3 hours
CAPS page references  20 and 207

Apart from developing the numerical method, Section 10.1 on page 342 of the Learner Book provides for extensive practice in Mental Mathematics.

Mathematical background
Solving number sentences by trial and improvement is a very valuable experience for learners, for at least three reasons:

- It provides them with opportunities to develop a robust understanding of the meaning of open number sentences (equations).
- It provides them with a basic experience of the so-called “numerical solution” of equations, which is of utmost importance in modern mathematical practice.
- It provides computation practice in a meaningful mathematical context.

The first step in solving an open number sentence by trial and improvement is to select a first trial number. For example, when solving $100 - 3 \times \square = 5 \times \square - 4$, you could take 1 as the first trial number.

The second step is to apply the calculation plans in the number sentence to the first trial number. The outcome may or may not be helpful in selecting a second trial number.

For example, $100 - 3 \times 1 = 97$ and $5 \times 1 - 4 = 1$, so it seems that 1 is quite far from the number for which $100 - 3 \times \square$ and $5 \times \square - 4$ will be equal. It hence makes sense to consider a much bigger number.

The third step is to select a second trial number. In this case 20 seems a good choice on the basis of the clue that the number should be much bigger than 1.

The fourth step is to apply the calculation plans in the number sentence to the second trial number. In this case, $100 - 3 \times 20 = 40$ and $5 \times 20 - 4 = 96$.

The fifth step is to reflect on the outcomes of the first and second trials and make a reasoned choice when selecting the third trial number.

In this case, $100 - 3 \times \square$ is bigger than $5 \times \square - 4$ for $\square = 1$, but $100 - 3 \times \square$ is smaller than $5 \times \square - 4$ for $\square = 20$. This suggests that a number between 1 and 20 is required for $100 - 3 \times \square$ to be equal to $5 \times \square - 4$. On the basis of this argument, 10 is an obvious choice as a third trial number.

The process is continued until the solution is found.
10.1 Solve and complete number sentences by trial and improvement

Possible misconceptions
Learners may develop the misconception that when using the trial-and-improvement method, they should correctly guess the solution. If they believe this, they will be inhibited from selecting trial numbers as described on the previous page. It is important that learners develop a “try a number and see what happens” attitude that corresponds to the nature of the trial-and-improvement process.

Notes on questions
It may take learners quite a while to develop the “try a number and see what happens” attitude required for solving number sentences by trial and improvement. Hence questions 1 to 9 all provide some support for their thinking. It is only in questions 10 and 11 (next page) that learners are required to work completely on their own.

Teaching guidelines
Demonstrate the actions in the tinted passage on the board and then let learners continue the process by doing questions 1 and 2. Once they have completed question 2, you may guide them to think as described for the fifth step on the previous page of this Teacher Guide. Some learners may quickly adopt the method and will be able to do question 3 on their own, and then proceed through questions 4 to 11.

Identify learners who get stuck with question 4. Support them (individually or in a group) by taking them through similar steps like those in the tinted passage, and through questions 1 and 2.

Answers
1. \(100 - 3 \times \text{the missing number} = 5 \times \text{the same number} - 4\)
   
   \[
   \text{Left-hand side} = 100 - 3 \times 10 = 100 - 30 = 70; \quad \text{Right-hand side} = 5 \times 10 - 4 = 50 - 4 = 46
   \]
   
   Therefore, 10 cannot be the missing number because the answers on the right-hand side and left-hand side differ.

2. Similar investigations for 20 and 15

3. 13

4. 13

5. (a) \(4 \times 20 + 7 = 87\) and \(6 \times 20 - 9 = 111\) (not true)
   
   \[
   4 \times 10 + 7 = 47 \quad \text{and} \quad 6 \times 10 - 9 = 51 \quad \text{(not true)}
   \]
   
   \[
   4 \times 5 + 7 = 27 \quad \text{and} \quad 6 \times 5 - 9 = 21 \quad \text{(not true)}
   \]
   
   (b) 10
   (c) 5
   
   (d) \(4 \times 8 + 7 = 39\) and \(6 \times 8 - 9 = 39\) (true)
   
   (e) Various numbers > 8, e.g. 11; 15; 17; 18
   (f) Numbers < 8, e.g. 7; 6; 4

Here is a puzzle to think about:

Hundred minus three times a certain number is equal to four less than five times the number. What is this number?

Can this number be 5?

Mpho investigated:

\[
\begin{align*}
100 - 3 \times 5 &= 100 - 15 = 85 \\
5 \times 5 &= 25 \text{ and } 4 \text{ less than } 25 \text{ is } 21.
\end{align*}
\]

No, 21 is far less than 85!

1. Investigate whether the missing number in the puzzle can be 10.
2. Investigate whether it can be 20, or maybe 15.
3. Find out what the number is!
4. Find the number that will make this number sentence true:
   
   \[
   100 - 3 \times \Box = 5 \times \Box - 4
   \]

5. (a) Investigate whether any of the numbers 20, 10 or 5 will make this number sentence true:
   
   
   \[
   4 \times \Box + 7 = 6 \times \Box - 9
   \]
   
   4 \times 10 + 7 = 47 and \(6 \times 10 - 9 = 51\) (not true)
   
   4 \times 5 + 7 = 27 and \(6 \times 5 - 9 = 21\) (not true)
   
   (b) 10
   (c) 5
   
   (d) \(4 \times 8 + 7 = 39\) and \(6 \times 8 - 9 = 39\) (true)
   
   (e) Various numbers > 8, e.g. 11; 15; 17; 18
   (f) Numbers < 8, e.g. 7; 6; 4

Write three different numbers for which \(4 \times \Box + 7 > 6 \times \Box - 9\).
Teaching guidelines
Recording the different trial numbers and outcomes in a table like the one at the top of the Learner Book page is a very useful way to keep track of the search process.

Mathematical notes
The numerical method (trial-and-improvement method) for solving open number sentences is of substantial mathematical importance: it is the dominant method of solving open number sentences (equations) in modern mathematical practice.

Answers
6. (a) The difference increased again.
   (b) The difference decreased.

7. An example (learners’ trial numbers may differ):

<table>
<thead>
<tr>
<th>Number investigated</th>
<th>5</th>
<th>10</th>
<th>20</th>
<th>15</th>
<th>9</th>
<th>8</th>
<th>7</th>
</tr>
</thead>
<tbody>
<tr>
<td>40 + 3 × □</td>
<td>55</td>
<td>70</td>
<td>100</td>
<td>85</td>
<td>67</td>
<td>64</td>
<td>61</td>
</tr>
<tr>
<td>10 × □ − 9</td>
<td>41</td>
<td>91</td>
<td>191</td>
<td>141</td>
<td>81</td>
<td>71</td>
<td>61</td>
</tr>
<tr>
<td>Difference</td>
<td>14</td>
<td>21</td>
<td>91</td>
<td>56</td>
<td>14</td>
<td>7</td>
<td>0</td>
</tr>
</tbody>
</table>

8. An example (learners’ trial numbers may differ):

<table>
<thead>
<tr>
<th>Number investigated</th>
<th>1</th>
<th>5</th>
<th>10</th>
<th>. . .</th>
<th>. . .</th>
<th>. . .</th>
<th>. . .</th>
<th>24</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 × □ − 12</td>
<td>−7</td>
<td>13</td>
<td>38</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>108</td>
</tr>
<tr>
<td>4 × □ + 12</td>
<td>16</td>
<td>32</td>
<td>52</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>108</td>
</tr>
<tr>
<td>Difference</td>
<td>23</td>
<td>19</td>
<td>14</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>0</td>
</tr>
</tbody>
</table>

9. An example (learners’ trial numbers may differ):

<table>
<thead>
<tr>
<th>Number investigated</th>
<th>2</th>
<th>100</th>
<th>50</th>
<th>. . .</th>
<th>. . .</th>
<th>. . .</th>
<th>. . .</th>
<th>60</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 × □ + 50</td>
<td>56</td>
<td>350</td>
<td>200</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>230</td>
</tr>
<tr>
<td>5 × □ − 70</td>
<td>−60</td>
<td>430</td>
<td>180</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>230</td>
</tr>
<tr>
<td>Difference</td>
<td>116</td>
<td>80</td>
<td>20</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>. . .</td>
<td>0</td>
</tr>
</tbody>
</table>

10. (a) 60  (b) 60  (c) 60

11. (a) 18  (b) 32  (c) 1
10.2 Flow diagrams, number sentences and tables

Mathematical notes
A flow diagram is a way of representing a calculation plan that can be applied to many different numbers. For example, the calculation plan $4 + \square \times 8$ can be represented with this flow diagram:

\begin{center}
\begin{tikzpicture}
\node (input) at (0,0) {$\square$};
\node (multiply) at (2,0) {$\times 8$};
\node (add) at (4,0) {+ 4};
\draw (input) -- (multiply);
\draw (multiply) -- (add);
\end{tikzpicture}
\end{center}

or

\begin{center}
\begin{tikzpicture}
\node (input) at (0,0) {input number};
\node (multiply) at (2,0) {$\times 8$};
\node (add) at (4,0) {+ 4};
\draw (input) -- (multiply);
\draw (multiply) -- (add);
\end{tikzpicture}
\end{center}

Instead of using the placeholder $\square$, the flow diagram can be expanded to show that different input numbers are allowed:

\begin{center}
\begin{tikzpicture}
\node (multiply) at (2,0) {$\times 8$};
\node (add) at (4,0) {+ 4};
\draw (multiply) -- (add);
\end{tikzpicture}
\end{center}

Exactly the same information can also be represented with a formula, for example:

\[
\text{output number} = 8 \times \text{input number} + 4
\]

Answers
1. Flow diagram A: $5 \rightarrow 3\,280$  $2 \rightarrow 1\,480$  $3 \rightarrow 2\,080$
2. Flow diagram B: $5 \rightarrow 171\,000$  $2 \rightarrow 169\,200$  $3 \rightarrow 169\,800$
3. R1 480
4. 3 nights
5. Number of nights $\rightarrow 600 \rightarrow + 280 \rightarrow \text{Cost}$

At the private hospital Careplace you have to pay R280 to be admitted, and then R600 for each night that you sleep there.
For example, Thabile was admitted to Careplace and stayed for three nights. She had to pay $R280 + 3 \times R600$ which is $R280 + R1\,800 = R2\,080$.

3. How much do you have to pay if you are admitted to Careplace hospital and sleep there for two nights?
4. How long was Ben in the hospital if he had to pay R2 080?
5. Which of these flow diagrams show how the cost of staying at Careplace can be calculated?

\begin{center}
\begin{tikzpicture}
\node (cost) at (4,0) {Cost};
\node (multiply) at (2,0) {$\times 600$};
\node (add) at (4,0) {+ 280};
\draw (cost) -- (multiply);
\draw (multiply) -- (add);
\end{tikzpicture}
\end{center}

Here is another way to describe how you can calculate the cost of staying in the private hospital Careplace:

\[
\text{Cost} = 600 \times \text{the number of nights} + 280,
\]

Cost for $\square$ nights $= 600 \times \square + 280$
Teaching guidelines

The section as a whole comprises an investigation to establish under which circumstances a certain hospital will be cheaper than another hospital. It amounts to answering the following question:

For which values of $c$ is $600 \times c + 280$ smaller than $620 \times c + 100$?

Answers

6. (a) R3 880  (b) R7 480

7. (a) R3 820  (b) R7 540

8. For a longer stay, Careplace is cheaper; for a shorter stay, Goodcare is cheaper.

9. | Number of nights | 1   | 2   | 3   | 4   | 5   |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Careplace</td>
<td>880</td>
<td>1 480</td>
<td>2 080</td>
<td>2 680</td>
<td>3 280</td>
</tr>
<tr>
<td>Goodcare</td>
<td>720</td>
<td>1 340</td>
<td>1 960</td>
<td>2 580</td>
<td>3 200</td>
</tr>
<tr>
<td>Thulare</td>
<td>960</td>
<td>1 460</td>
<td>1 960</td>
<td>2 460</td>
<td>2 960</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
<th>11</th>
<th>12</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 880</td>
<td>4 480</td>
<td>5 080</td>
<td>5 680</td>
<td>6 280</td>
<td>6 880</td>
<td>7 480</td>
</tr>
<tr>
<td>3 820</td>
<td>4 440</td>
<td>5 060</td>
<td>5 680</td>
<td>6 300</td>
<td>6 920</td>
<td>7 540</td>
</tr>
<tr>
<td>3 460</td>
<td>3 960</td>
<td>4 460</td>
<td>4 960</td>
<td>5 460</td>
<td>5 960</td>
<td>6 460</td>
</tr>
</tbody>
</table>

10. For fewer than 9 nights, Goodcare works out cheaper, but for more than 9 nights, Careplace is cheaper.

11. (a) R460
    (b) Cost = 500 \times \text{the number of nights} + 460
Grade 5 Term 4 Unit 11  Probability

<table>
<thead>
<tr>
<th>Sections in this unit</th>
<th>Content</th>
<th>Pages in Learner Book</th>
</tr>
</thead>
<tbody>
<tr>
<td>11.1 A coin-tossing experiment</td>
<td>Investigate what happens for many events if there are two equally likely outcomes</td>
<td>346 to 347</td>
</tr>
<tr>
<td>11.2 Spinner Experiment 1</td>
<td>More experiments with and reflection on events with two equally likely outcomes</td>
<td>347 to 348</td>
</tr>
<tr>
<td>11.3 Spinner Experiment 2</td>
<td>Repeating an event with outcomes that are not equally likely</td>
<td>349</td>
</tr>
</tbody>
</table>

**CAPS time allocation**
2 hours

**CAPS page references**
31 and 208

**Mathematical background**
When a coin is tossed, one of two things can happen. Stated differently, there are two possible outcomes: the coin can come to rest on one side or on the other side. The terms “heads” and “tails” are often used to distinguish the two sides of a coin. When a normal coin is tossed many times, there is no reason to expect that the one outcome (heads) will occur more often than the other outcome (tails). We say the two possible outcomes are “equally likely” – this is a way of saying that one would expect more or less the same number of heads and tails if a coin is tossed many times. The same applies to the rolling of a die, though in this case there are six different equally likely outcomes.

When a coin is tossed (or when a die is rolled) once, it is impossible to predict with any confidence what the outcome of the event will be. Although the range of possible outcomes is known, no grounds exist to predict that one outcome rather than another will occur. Any of the outcomes is exactly as likely to occur as any other. Hence the outcome of the event is **unpredictable**. Such events are called **random events**.

Although the outcome of a random event is completely unpredictable, predictions can be made about approximately how often a particular outcome will occur if the event is repeated many times. For example, if a coin is tossed many, many times, it will end up on one side for about half of the time and on the other side for about half of the time. If an ordinary die is rolled many, many times, the number 4 (or any other number in the range 1, 2, 3, 4, 5, 6) can be expected to occur roughly one sixth of the time. Suppose another die is not marked 1, 2, 3, 4, 5, 6 on its six faces, but red on one face, blue on two faces and yellow on three faces. If such a coloured die is rolled many, many times, red can be safely predicted to come on top about 1 sixth of the time, blue to come on top roughly one third of the time and yellow to come on top roughly half of the time.

The activities in this unit provide learners with experiences of repeated **random events**, with a view for them to experience that the different possible outcomes happen **approximately** the same number of times.

**Resources**
Coins; cardboard for making spinners; scissors; sheets of A4 paper; red and blue colouring pencils or crayons

**Note:** To save classroom time, it will be better if you make the spinners and coloured sheets required for Sections 11.2 and 11.3 for your learners.
11.1 A coin-tossing experiment

**Mathematical notes**

Random events (“probability”) can be investigated **theoretically**, by arguing logically. For example, one may **argue** that if a die is rolled many times, roughly the same number of each of the six different possible outcomes may occur. Random events can also be investigated **empirically**, by **performing** the events repeatedly and analysing the **actual outcomes**. Learners are engaged in both theoretical and empirical investigations of random events in this unit.

In question 1, learners are invited to think theoretically about tossing a coin. In question 2 they engage empirically with the same questions.

**Tallies** are indicated by drawing a line for every occurrence. Every fifth line crosses the four preceding lines so that five lines can easily be counted. Counting the tallies gives the **frequencies**, which are expressed as numbers, for example 11 and 9.

**Teaching guidelines**

It may be necessary to explain the meaning of question 1(a) to learners. It means: “If you toss the coin 20 times, how many times do you think it will land on the one side, and how many times do you think it will land on the other side?”

The purpose of questions 1 and 2 is to allow learners to develop a sense of what happens when a random event is repeated many times: the different outcomes happen approximately the same number of times, but not necessarily exactly the same number of times. Learners are not expected to produce any specific explanations in questions 1(c) and 2(b); the purpose of these questions is only to induce them to think about what may happen when a random event is repeated many times.

**Notes on questions**

The purpose of question 1 is not to assess whether learners know supposedly correct answers. The purpose is to entice the learners into making a prediction (hypothesis), which they will then investigate in questions 2 and 3.

**Answers**

1. (a) to (c) Learners who suggest that heads and tails are equally likely as results and hence that heads and tails should each come up more or less half the time, demonstrate good intuitions about random events.

2. (a) Answers will vary, but the fractions closer to \( \frac{10}{20} \) are more likely.

(b) Individual results. Learners will probably have different results.

No, any specific result is unlikely because any two learners are unlikely to get the same result.

---

**Unit 11**

**11.1 A coin-tossing experiment**

1. Imagine you toss a coin many times. You check every toss to see if it is “heads” or “tails.”

(a) Write down what you think the results will be when you toss a coin 20 times.

(b) How many “heads” do you think you will get if you toss the coin many, many times?

(c) How many “tails” do you think you will get if you toss the coin many, many times? Explain why you say so.

2. Work with a classmate to do the coin-tossing experiment. Record your results in a tally table.

Each of you must toss the coin 20 times. At the end you should have the result of your 20 tosses, and your classmate should have the result of his or her 20 tosses.

<table>
<thead>
<tr>
<th>Heads</th>
<th>Tails</th>
</tr>
</thead>
</table>

(a) What fraction of your 20 results is “heads” \( \frac{7}{20} \)? Did your experiment work out the way you thought it would? Explain why you say so.

(b) What fraction of your classmate’s 20 results is “heads” \( \frac{3}{20} \)? Do you think there is a problem with the experiment if your results are very different? Explain why you say so.
Answers
3. (a) and (b) Answers will differ. The results will be in eightieths. It should be fairly close to 40 heads and 40 tails. The more times the coin is tossed, the more likely it is that the distribution will be close to 50% heads and 50% tails.
   (c) Individual answers. The purpose of the question is only to induce learners to think about what may happen when a random event is repeated many times.

11.2 Spinner Experiment 1

Teaching guidelines
To save classroom time, it would be best if you make the spinners and colour the sheets beforehand.

Shorter pencils work better. The pencil should be inserted perpendicularly (at 90 degrees) through the centre of the cardboard square. The centre is at the point where the diagonals (lines connecting opposite corners) cross.

During the experiment one of the sides of the cardboard square will end up touching the page. The midpoints of the sides are indicated by dots/marks. The colour on which the dot/mark lands, is the result (outcome) of the spin.

Approximately equal numbers of blue and red landings will be obtained.

A typical tally table for 20 spins will look like this:

<table>
<thead>
<tr>
<th>Red</th>
<th>Blue</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>

3. You recorded 20 tosses and your classmate recorded 20 tosses. Put your results together with those of two other classmates, so that you have the results of 80 tosses altogether.
   (a) What fraction of the results is “heads”?
   (b) What fraction of the results is “tails”?
   (c) Are you surprised by the results? Explain why you say so.
Teaching guidelines
Explain to learners that the phrases “outcomes of Spinner Experiment 1” in question 1(d) and “results of Spinner Experiment 1” in question 2 refer to the combination of all 20 outcomes – one outcome each time the spinner is spun.

The purpose of questions 1 to 3 is again to allow learners to develop a sense of what happens when a random event is repeated many times: the different outcomes happen approximately the same number of times, but not necessarily exactly the same number of times.

Answers
1. (a) Yes. If you put the spinner in the middle of one of the quarters of the page, it might end up in that quarter more often. We put the spinner in the centre to make the chances even.
   
   (b) No, as long as it goes around enough times.
   
   (c) No, it will not matter. The area hasn’t changed, therefore red and blue are still equally likely as results.
   
   (d) Red and blue could be divided respectively 20-0 (very, very unlikely), 19-1, 18-2, 17-3, 16-4, 15-5, 14-6, 13-7, 12-8, 11-9, 10-10, 9-11, 8-12, 7-13, 6-14, 5-15, 4-16, 3-17, 2-18, 1-19 or 0-20 (very, very unlikely).

2. Individual results. The fractions will vary between \( \frac{0}{20} \) (“0 out of 20”) and \( \frac{20}{20} \). Fractions close to \( \frac{10}{20} \), like \( \frac{9}{20}, \frac{11}{20}, \frac{8}{20} \), and \( \frac{12}{20} \), will occur more often than fractions further away from \( \frac{10}{20} \), like \( \frac{10}{20}, \frac{5}{20} \) and \( \frac{16}{20} \).

3. (a) to (c) A typical distribution for 45 learners might look like this:

```
  x
  x x
 x x x x
 x x x x x
```

```
 x x x x x x x
 x x x x x x
```

```
 x x x x x x x x x x
```

```
 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
```

Sometimes people think the number of RED results and the number of BLUE results must be the same in any experiment, because the page is divided into two equal parts. This is not true.

Only when we do an experiment with many, many spins can we expect to see almost the same number of RED and BLUE results if the page is divided into two equal parts. We cannot expect that in small experiments.
11.3 Spinner Experiment 2

**Mathematical notes**
The chances that the spinner will land on any of the four quarters are equal. However, because three of the quarters are now red, one would expect the spinner to land on red approximately 3 out of every 4 times.

**Answers**
1. (a) For every spin, red and blue are the possible outcomes. The possible outcomes for 20 spins range from 0 out of 20 red to 20 out of 20 red (or blue).
   (b) Hopefully learners will argue that since 3 of the 4 equally likely outcomes are now red, the outcome of Spinner Experiment 2 will be different. The spinner can be expected to land on red about 3 times as often as on blue.
2. (a) A group of five will have data of 100 spins.
   (b) Group answer in hundredths
Addendum

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Place value cards for learners
(4 pages = 1 set)
<table>
<thead>
<tr>
<th>2000</th>
<th>3000</th>
</tr>
</thead>
<tbody>
<tr>
<td>4000</td>
<td>5000</td>
</tr>
<tr>
<td>6000</td>
<td>7000</td>
</tr>
<tr>
<td>8000</td>
<td>9000</td>
</tr>
</tbody>
</table>
Place value cards for teachers
(14 pages = 1 set)
600 60
700 70
10000
20000
300000
400000
700000
80000
Square grid paper (1 cm × 1 cm)
Graph paper / Square grid paper (0.5 cm × 0.5 cm)
Graph paper
Dotted paper
A model for teaching conversion of units (TG pp. 117, 162, 235)

“The purpose of this remediation is to provide guidance on minimising errors on conversions. Emphasis should be placed on practical demonstrations to show the relationship between different units of measurement.

The following steps could be used to remedy the problems encountered in conversions of units. When teaching conversions, emphasis must be placed on multiplication by a thousand since ‘kilo’ means thousand and ‘milli’ means one thousandth.

The following model may be used to teach conversion of units:

![Diagram of unit conversion model](image)

The model shows intervals of milli (grams/litres/metres) up to kilo (grams/litres/metres). The intervals range in units of tens, for example converting from centi to milli, one would need to multiply by ten and from milli to centi one would need to divide by ten; thus 1 centimetre = 10 millimetres and 1 millimetre = 0.1 centimetre. Similarly, it is noticeable in the model that from kilo to the basic unit (metre/litre/gram) one needs to multiply by a thousand and vice versa; thus 1 kilogram = 1 000 grams and 1 000 grams = 0.001 kilogram.

The following mnemonic may be used for learners to remember the order of the units of measurement: Kids Have Dreams Making Dad Chocolate Muffins.”

Rulers

Term 1 Unit 6: Section 6.4, question 5    (TG p. 79; LB p. 73)
Term 1 Unit 6: Section 6.4, question 7  (TG p. 79; LB p. 73)
Term 2 Unit 5: Section 5.1, question 1

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(TG p. 171; LB p. 157)
Term 2 Unit 5: Section 5.1, question 3       (TG p. 172; LB p. 158)

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Term 4 Unit 3: Section 3.2, question 2  (TG p. 329; LB p. 294)
Term 4 Unit 3: Section 3.2, question 4  (TG p. 330; LB p. 295)
Term 4 Unit 4: Section 4.2, question 1 (TG p. 340; LB p. 304)
Term 4 Unit 4: Section 4.3, question 1  (TG p. 342; LB p. 306)
Term 4 Unit 5: Section 5.3
Additional learning activity (TG p. 351)
Which of the rectangles below are enlargements or reductions of the shaded rectangle?
In each case, explain why you think it is, or why it is not.

A B C D E

Term 4 Unit 7: Section 7.1, question 1
(TG p. 370, LB p. 331)
Term 4 Unit 6: Section 6.2, question 1  (TG p. 360; LB p. 323)